

Frontogenesis in the Presence of Stokes Forces

Baylor Fox-Kemper (Brown Geo.)

with Jim McWilliams (UCLA), Nobu Suzuki (Brown), and Qing Li (Brown)

Expanding on past work with:

Peter Hamlington (CU-Boulder), Luke Van Roekel (Northland College), Sean Haney (CU)
Adrean Webb (TUMST), Keith Julien (CU-APPM), Greg Chini (UNH),
Peter Sullivan (NCAR), Mark Hemer (CSIRO)

CARTHE Spring 2014 All-Hands Meeting

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http://hvo.wr.usgs.gov/multimedia/archive/2007/2007_Jan-May.html

Dimensionless Boussinesq

Spanning Mesoscale to Stratified Turbulence

following McWilliams (85)

$$\begin{aligned}
 Ro [v_{i,t} + v_j v_{i,j}] + \frac{M_{Ro}}{Ri} w v_{i,z} + \boxed{\epsilon_{izj} v_j} &= -M_{Ro} \pi_{,i} + \frac{Ro}{Re} v_{i,jj} \\
 \frac{\alpha^2}{Ri} \left[w_{,t} + v_j w_{,j} + \frac{M_{Ro}}{Ro Ri} w w_{,z} \right] &= \boxed{-\pi_{,z} + b} + \frac{\alpha^2}{Re Ri} w_{,jj} \\
 b_t + v_j b_{,j} + \frac{M_{Ro}}{Ro Ri} w b_z + w &= 0
 \end{aligned}$$

$$v_{j,j} + \frac{M_{Ro}}{Ro Ri} w_z = 0$$

Plus boundary conditions

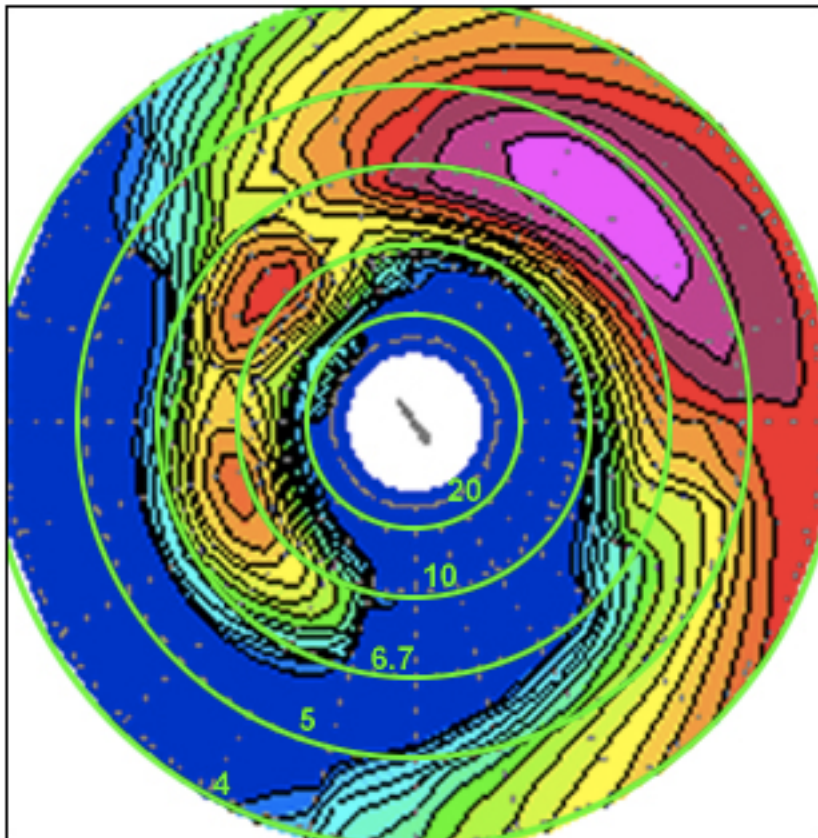
$$Re = \frac{UL}{\nu} \quad Ro = \frac{U}{fL} \quad Ri = \frac{N^2}{(U_{,z})^2} \quad \alpha = H/L$$

$$M_{Ro} \equiv \max(1, Ro) \quad v = \text{horiz. vel.} \quad w = \text{vert. vel.}$$

Surface Waves are...

fast, small, irrotational solutions of the Boussinesq Equations

NWW3 Polar Plot of Wave Energy Spectrum at ILM01



24 hr fcst Valid 0000 UTC 26 Apr 2002

NOAA / NWS / NCEP / MMAB

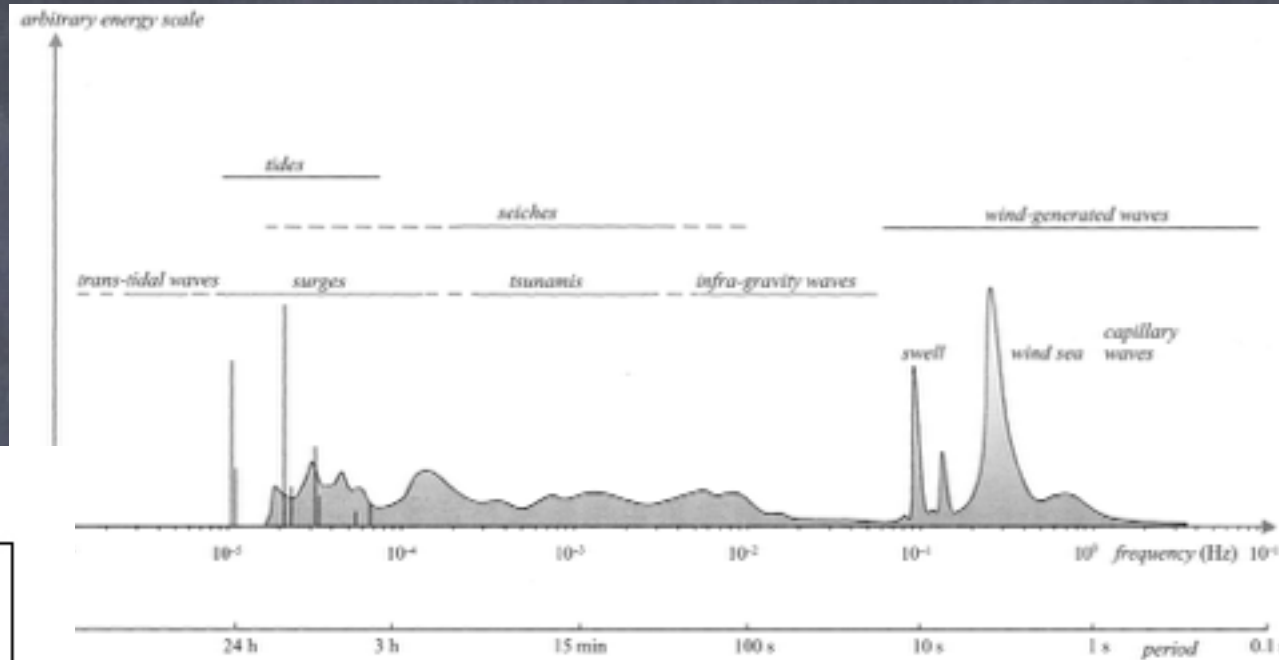


Illustration of wave spectra from different types of ocean surface waves (Holthuijsen, 2007)



Wave-Averaged Equations

$$\varepsilon = \frac{V^s H}{f L H_s}$$

following Lane et al. (07), McWilliams & F-K (13)
and Suzuki & F-K (14)

(for horizontally uniform Stokes drift)

$$Ro [v_{i,t} + v_j^L v_{i,j}] + \frac{M_{Ro}}{Ri} w v_{i,z} + \epsilon_{izj} v_j^L = -M_{Ro} \pi_{,i} + \frac{Ro}{Re} v_{i,jj}$$

$$\frac{\alpha^2}{Ri} \left[w_{,t} + v_j^L w_{,j} + \frac{M_{Ro}}{Ro Ri} \right] = -\pi_{,z} + b + \boxed{\varepsilon v_j^L v_{j,z}^s} + \frac{\alpha^2}{Re Ri} w_{,jj}$$

$$b_t + v_j^L b_{,j} + \frac{M_{Ro}}{Ro Ri} w b_z + w = 0$$

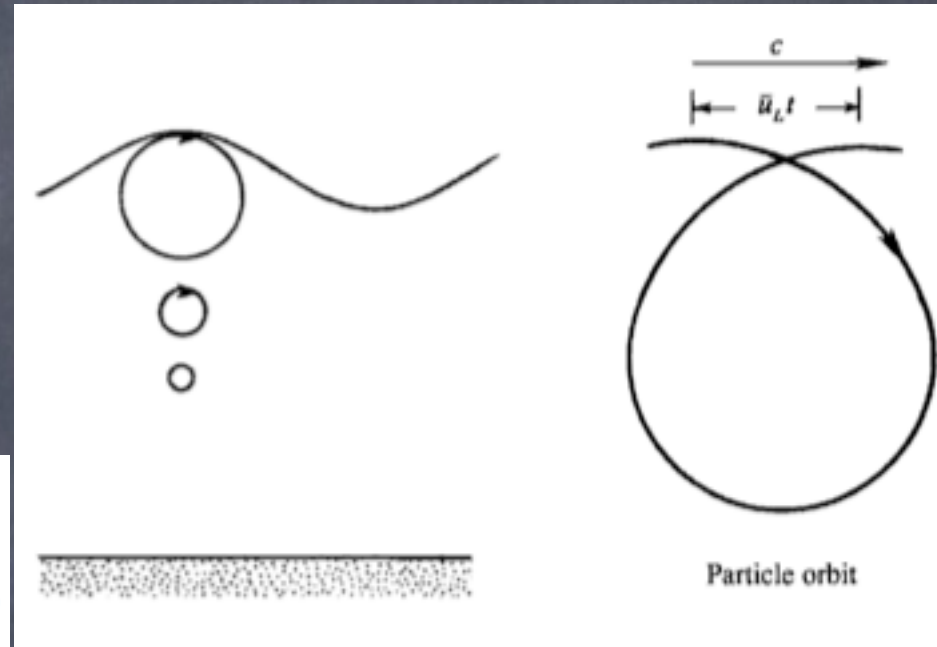
$$v_{j,j} + \frac{M_{Ro}}{Ro Ri} w_z = 0$$

Plus boundary
conditions

LAGRANGIAN (Eulerian+Stokes) advection & Coriolis
Stokes shear force is NEW *nonhydrostatic* term in Vert. Mom.

Stokes driftin' away

Take wave solns, compare the velocity of trajectories vs. Eulerian velocity, Taylor
Expand, calculate:



$$\begin{aligned} \mathbf{u}^L(\mathbf{x}_p(t), t) - \mathbf{u}^E(\mathbf{x}_p(t_0), t) &\approx [\mathbf{x}_p(t) - \mathbf{x}_p(t_0)] \cdot \nabla \mathbf{u}^E(\mathbf{x}_p(t_0), t) \\ &\approx \left[\int_{t_0}^t \mathbf{u}^E(\mathbf{x}_p(t_0), s') ds' \right] \cdot \nabla \mathbf{u}^E(\mathbf{x}_p(t_0), t). \end{aligned}$$

Monochromatic:

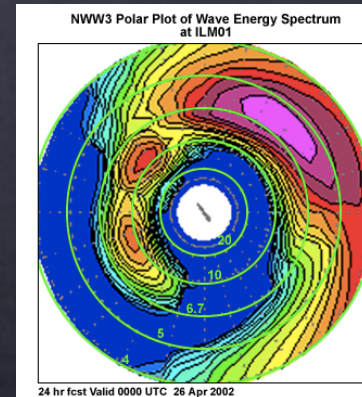
$$\mathbf{u}^S = \hat{\mathbf{e}}^w \frac{8\pi^3 a^2 f_p^3}{g} e^{\frac{8\pi^2 f_p^2}{g} z} = \hat{\mathbf{e}}^w a^2 \sqrt{gk^3} e^{2kz}.$$

Spectrum:

$$\mathbf{u}^S = \frac{16\pi^3}{g} \int_0^\infty \int_{-\pi}^\pi (\cos \theta, \sin \theta, 0) f^3 S_{f\theta}(f, \theta) e^{\frac{8\pi^2 f^2}{g} z} d\theta df.$$

Depth-Integrated:

$$\mathbf{u}_*^{S-int} = \int_{-\infty}^0 \mathbf{u}_*(z) dz = 2\pi \int_0^\infty \mathbf{H}_*(f) f S_f(f) df$$



The Character of the Langmuir Scale

- Near-surface

- Langmuir Cells & Langmuir Turb.

- $Ro \gg 1$

- $Ri < 1$: Nonhydro

- 1-100m ($H=L$)

- 10s to 1hr

- $w, u = O(10\text{cm/s})$

- Stokes drift

- Eqtns: Craik-Leibovich

- Params: McWilliams & Sullivan, 2000, Van Roekel et al. 2011

- Resolved routinely in 2170

image:
Thorpe, 04

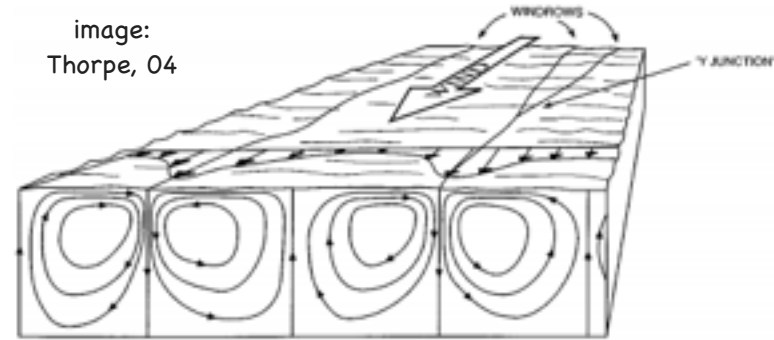
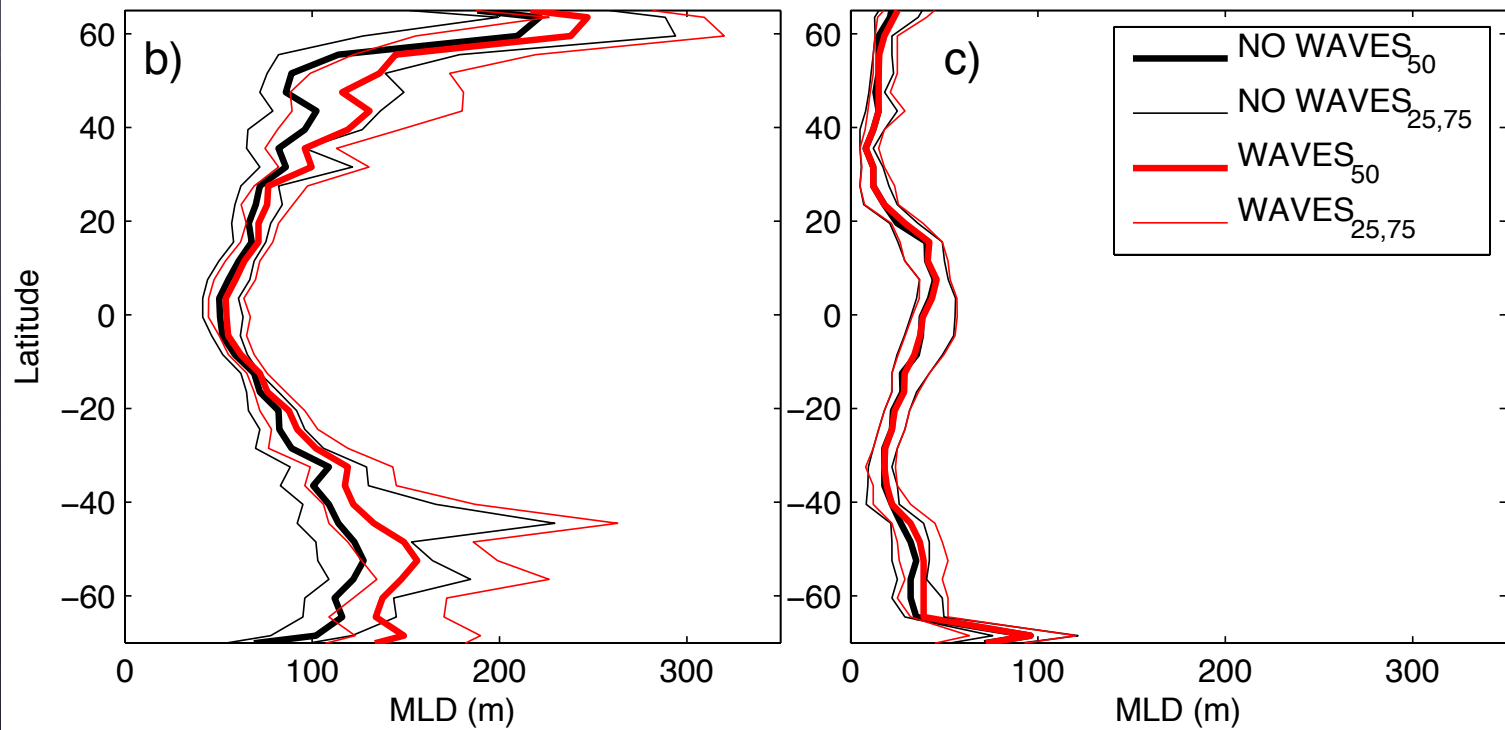
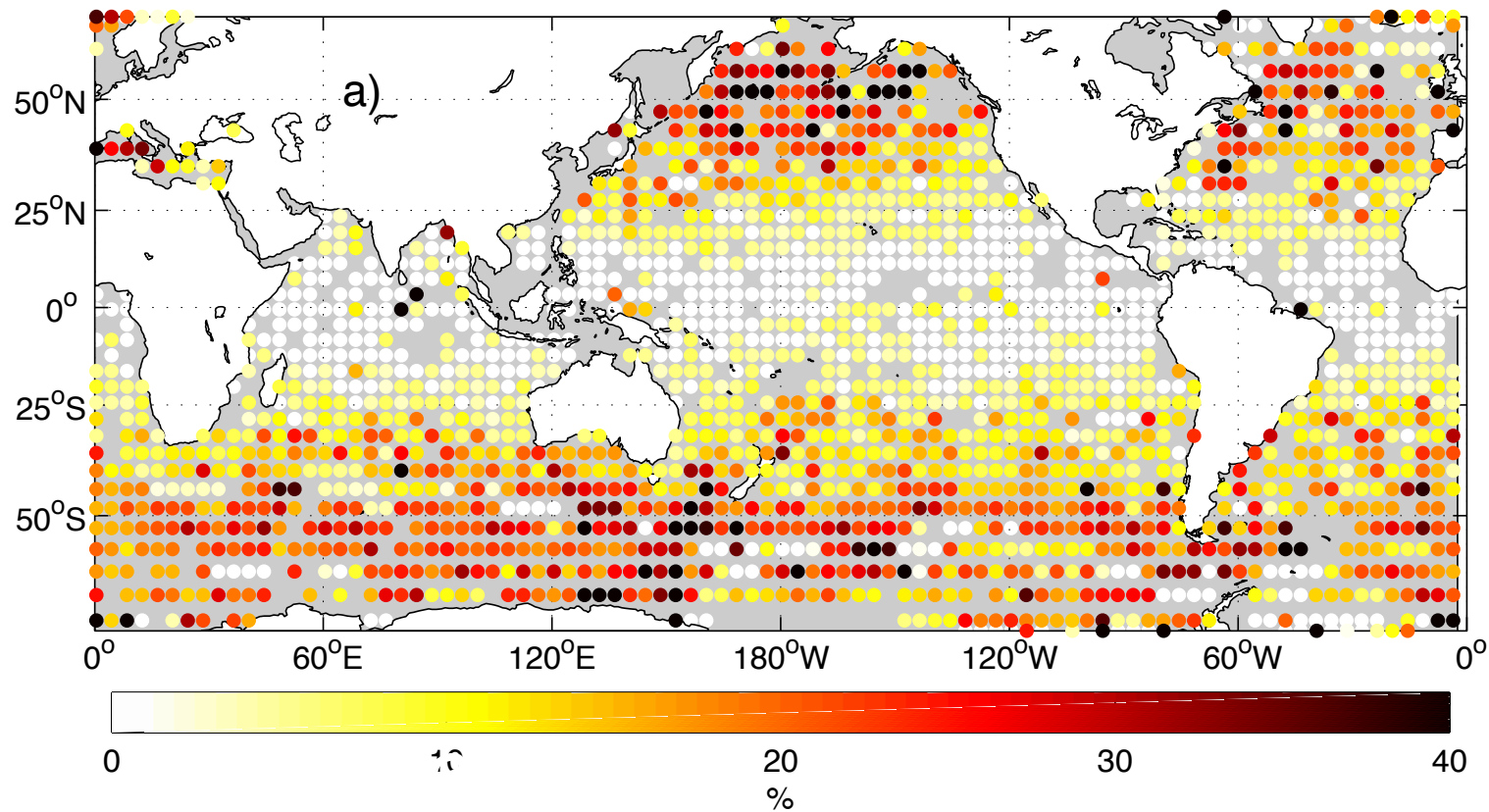


Figure 1 Sketch showing the pattern of mean flow in idealized Langmuir circulation. The windrows may be 2 m to 300 m apart, and the cell form is roughly square (as shown). In practice the flow is turbulent, especially near the water surface, and the windrows (Figure 2) amalgamate and meander in space and time. Bands of bubbles or buoyant algae may form within the downward-going (or downwelling) flow (see Figure 3).

Offline
obs-driven
parameterization:

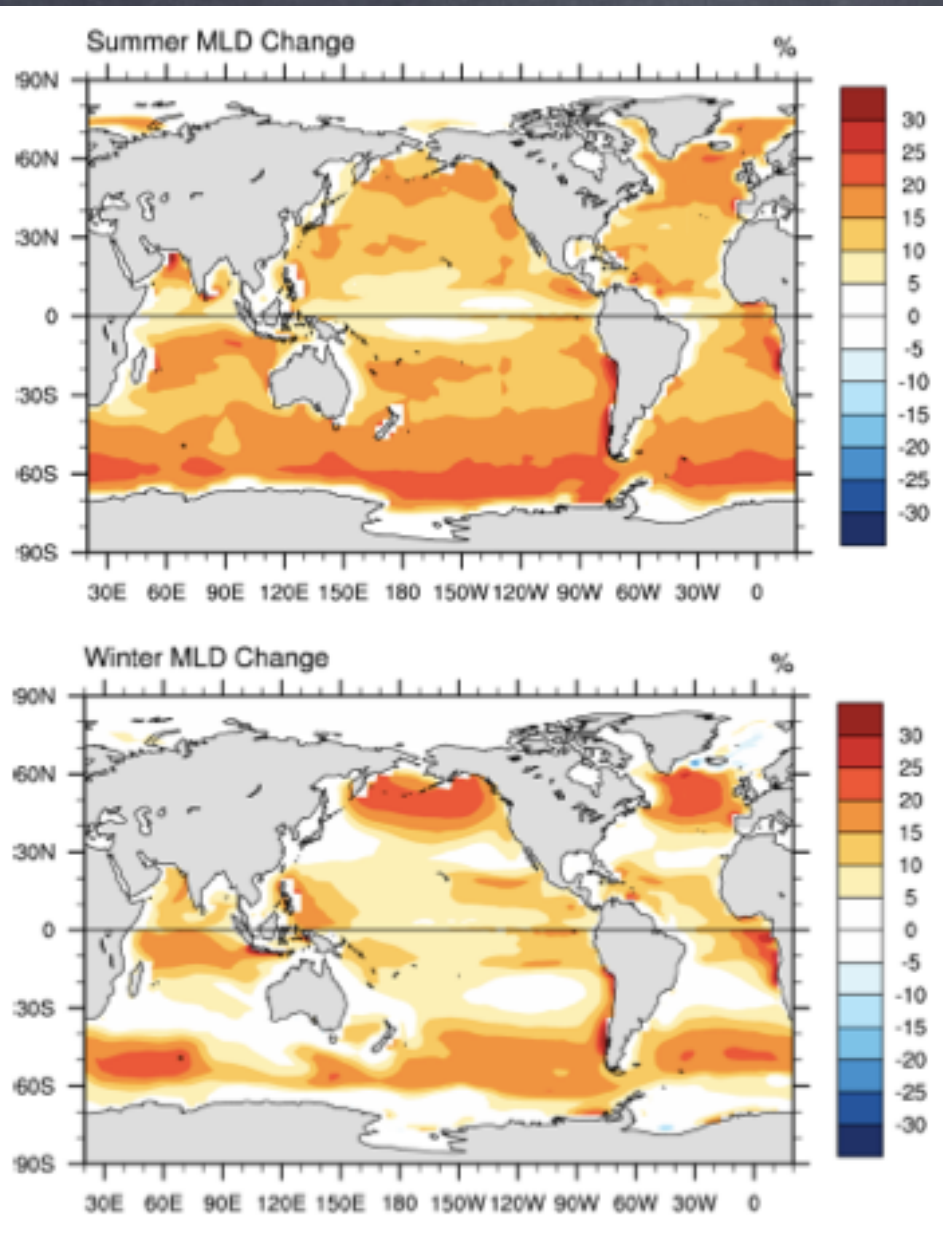
Including
Stokes-driven
Mixing
(Harcourt 2013)
Deepens the
Mixed Layer!

E. A. D'Asaro, J. Thomson, A.
Y. Shcherbina, R. R. Harcourt,
M. F. Cronin, M. A. Hemer,
and B. Fox-Kemper.
Quantifying upper ocean
turbulence driven by surface
waves. *Geophysical
Research Letters*, 41(1):
102-107, January 2014.



Including Stokes-driven Mixing in CESM, too!

(Harcourt & D'Asaro, 2008; Van Roekel et al, 2012)

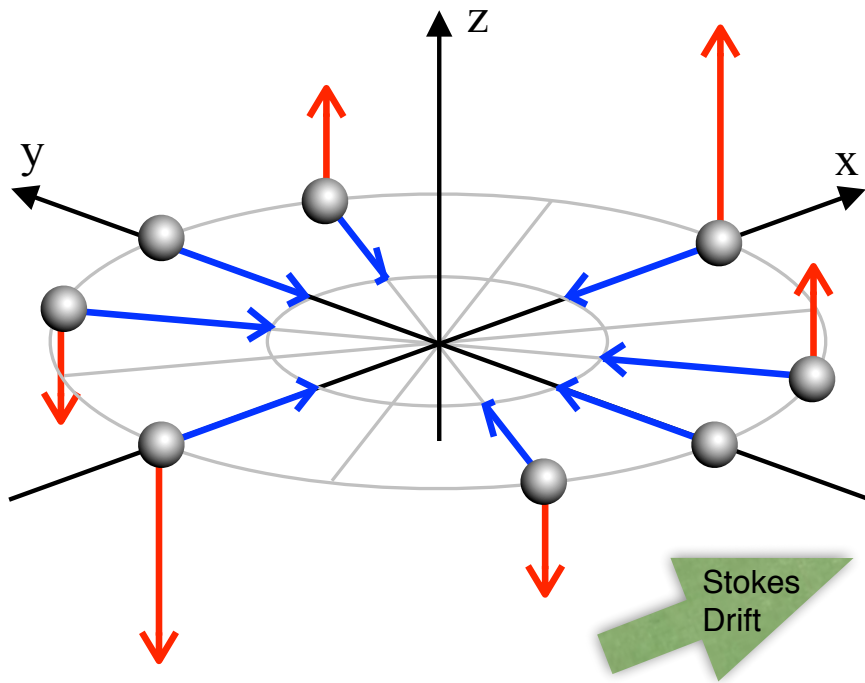


RMSE (m)		
Summer	Global	South of 30S
CTRL	15.42	20.52
MS2K	26.92	20.15
VR12a	15.67	16.66
VR12g	15.26	16.72
Winter	Global	South of 30S
CTRL	59.82	64.22
MS2K	135.16	181.88
VR12a	54.94	53.90
VR12g	56.63	57.57

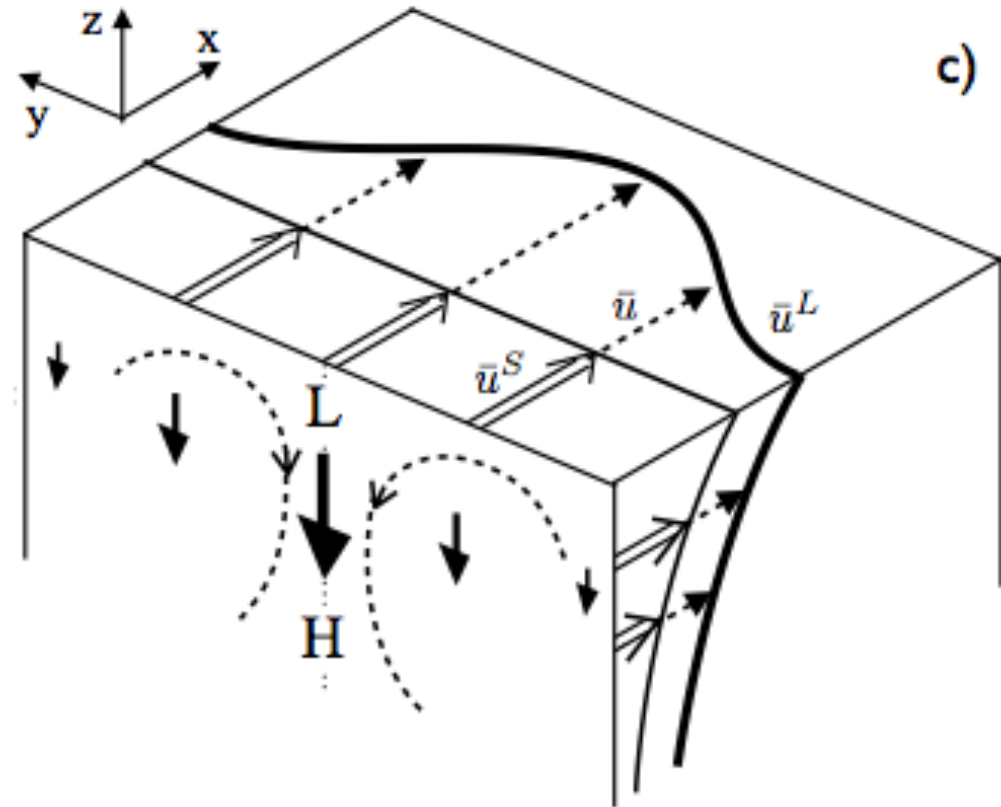
Remains to be co-tuned with mixed layer eddy, mesoscale, and near-inertial mixing parameterizations

Stokes Shear Force

and the CL2 mechanism for Langmuir circulations
 Flow directed along Stokes shear=downward force

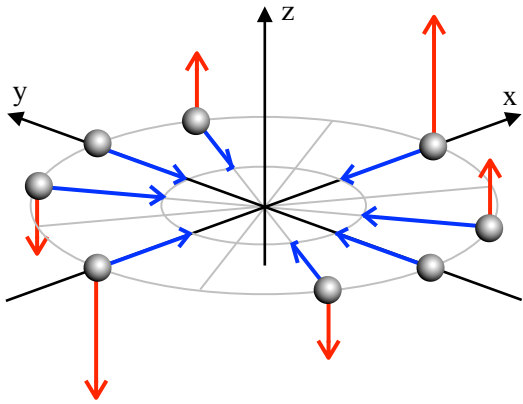


← : Stokes-shear force ● : water parcel
← : turbulent velocity

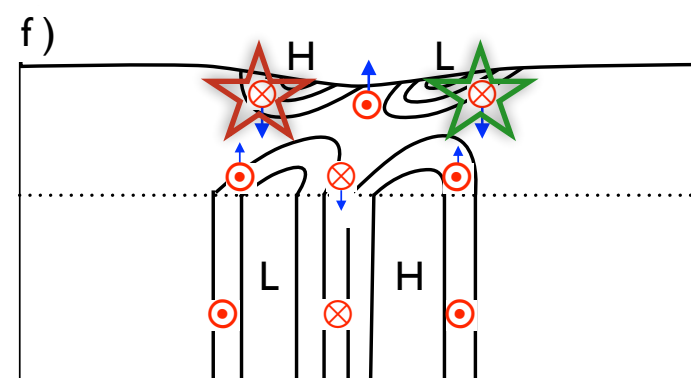
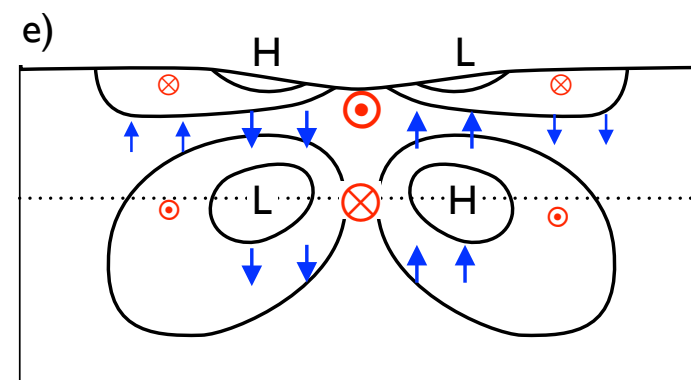
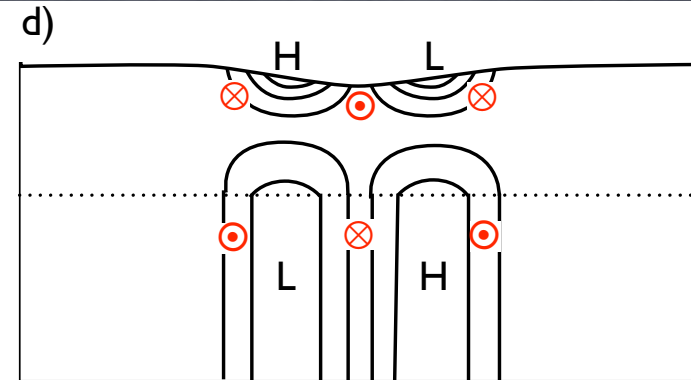
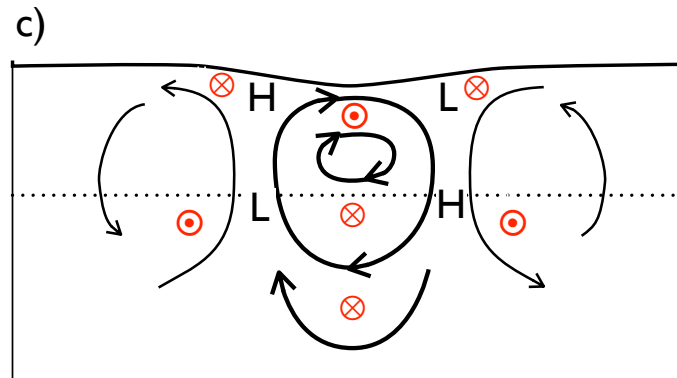
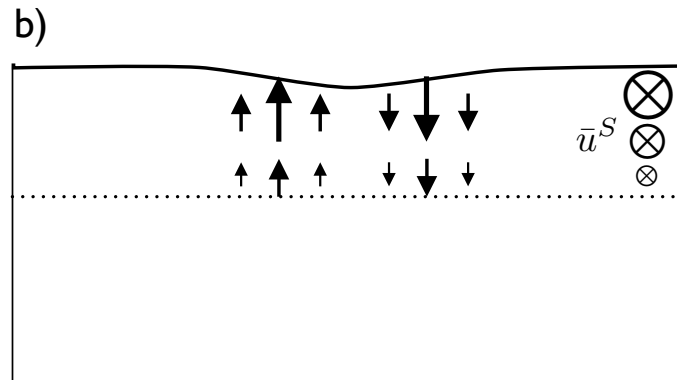
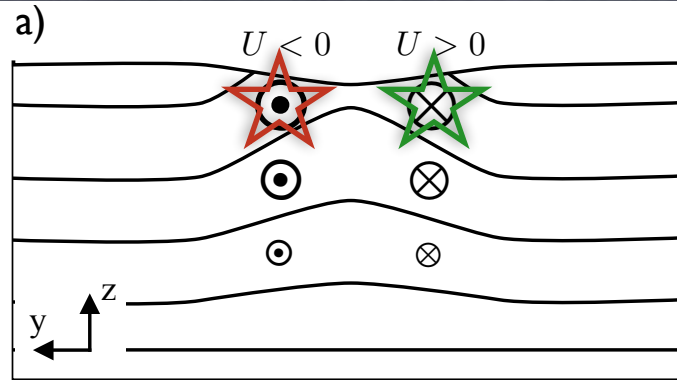


$$\frac{\alpha^2}{Ri} \left[w_{,t} + v_j^L w_{,j} + \frac{M_{Ro}}{Ro Ri} \right] = -\pi_{,z} + b + \epsilon v_j^L v_{j,z}^S + \frac{\alpha^2}{Re Ri} w_{,jj}$$

Stokes Shear Force on Submesoscale Cold Filament



←: Stokes-shear force ●: water parcel
←: turbulent velocity



J. C. McWilliams and B. F-K.
 Oceanic wave-balanced surface
 fronts and filaments. *Journal of Fluid
 Mechanics*, 730:464-490, 2013.

N. Suzuki and B. Fox-Kemper.
 Understanding Stokes Forces in the
 Wave-Averaged Equations, *JPO*, in
 prep, 2014.

Enhances Frontogenesis for Down-Front Stokes
Opposes Frontogenesis for Up-Front Stokes

Importance of Stokes shear force versus finite Rossby on (sub)mesoscale: McWilliams & F-K (13)

466

J. C. McWilliams and B. Fox-Kemper

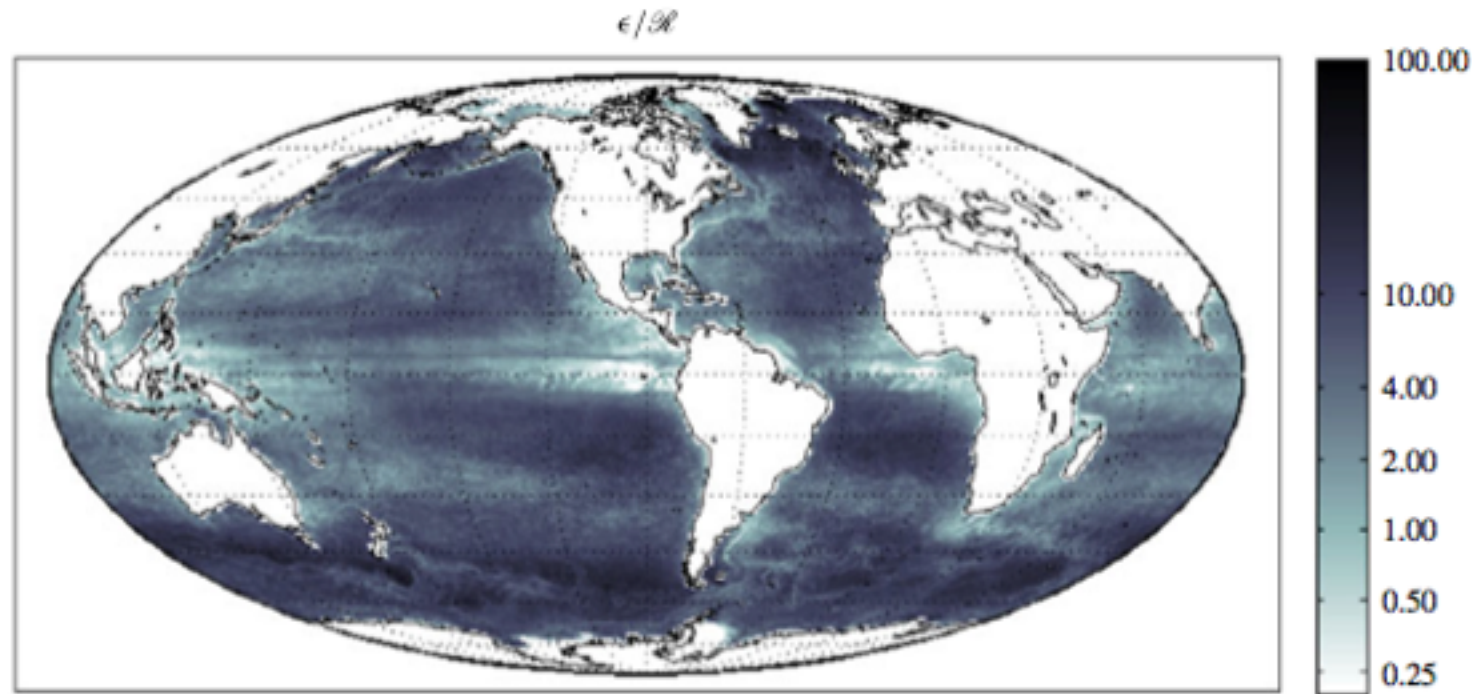


FIGURE 1. (Colour online) Estimated ratio $\epsilon/\mathcal{R} \approx (|\mathbf{u}_s \cdot \mathbf{u}|h) / (|\mathbf{u}|^2 h_s)$ governing the relative importance of Stokes effects versus nonlinearity. Eulerian velocity (\mathbf{u}) is taken as the AVISO weekly satellite geostrophic velocity or $-\mathbf{u}_s$ (for anti-Stokes flow) if $|\mathbf{u}_s| > |\mathbf{u}|$. The front/filament depth (h) is estimated as the mixed layer depth from the de Boyer Montégut *et al.* (2004) climatology. An exponential fit to the Stokes drift of the upper 9 m projected onto the AVISO geostrophic velocity provides $\mathbf{u}_s \cdot \mathbf{u}$ and h_s . Stokes drift is taken from the Wave Watch 3 simulation described in Webb & Fox-Kemper (2011). \mathbf{u} , \mathbf{u}_s , and h_s are all for the year 2000, while h is from a climatology of observations over 1961–2008. The year 2000 average of ϵ/\mathcal{R} is shown.

$$\epsilon = \frac{V^s H}{f L H_s}$$

$$Ro = \frac{U}{f L}$$

LES of Langmuir-Submeso Interactions?

Perform large eddy simulations (LES) of Langmuir turbulence with a submesoscale temperature front using wave-averaged equations

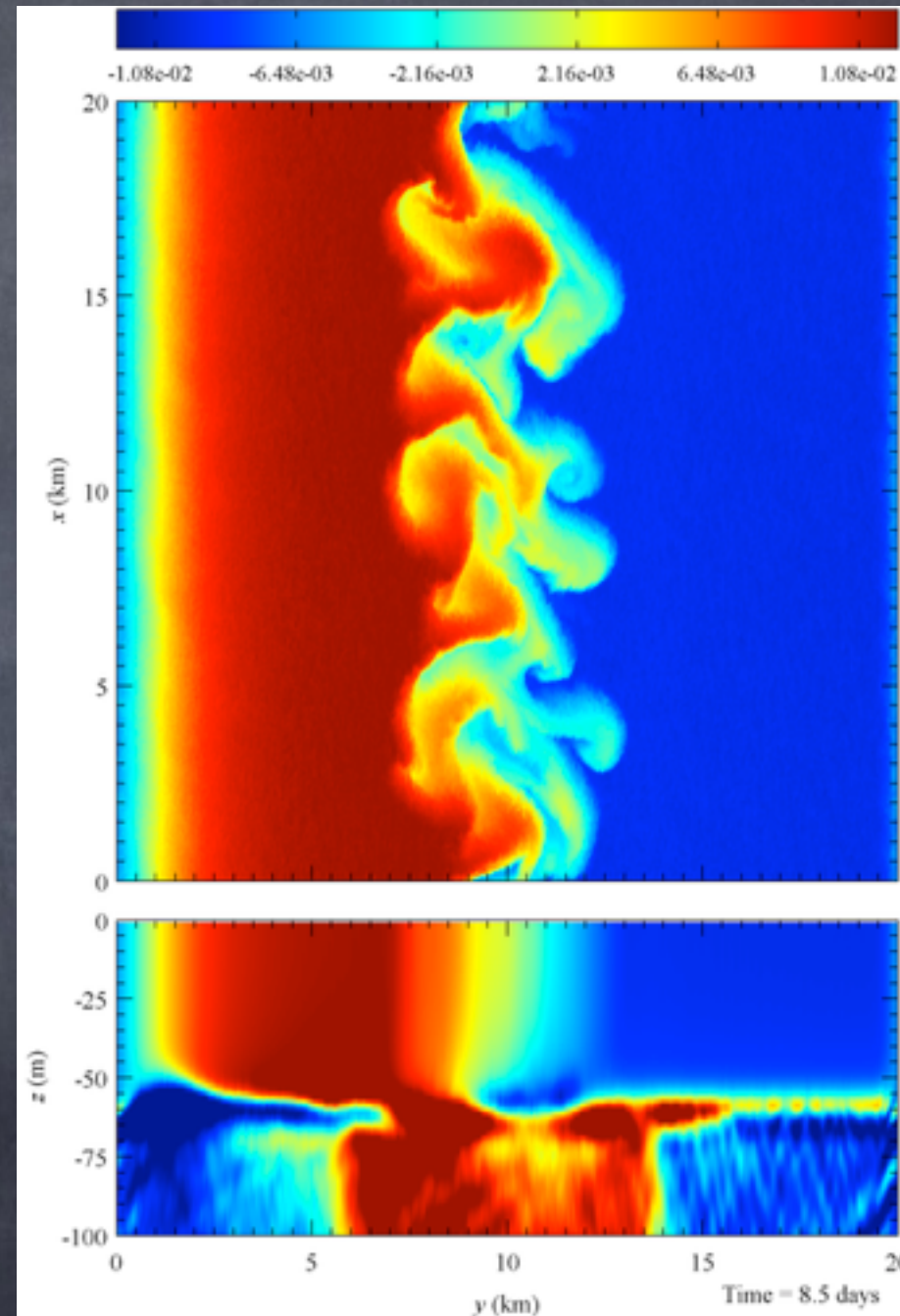
Computational parameters:

Domain size: 20km x 20km x -160m

Grid points: 4096 x 4096 x 128

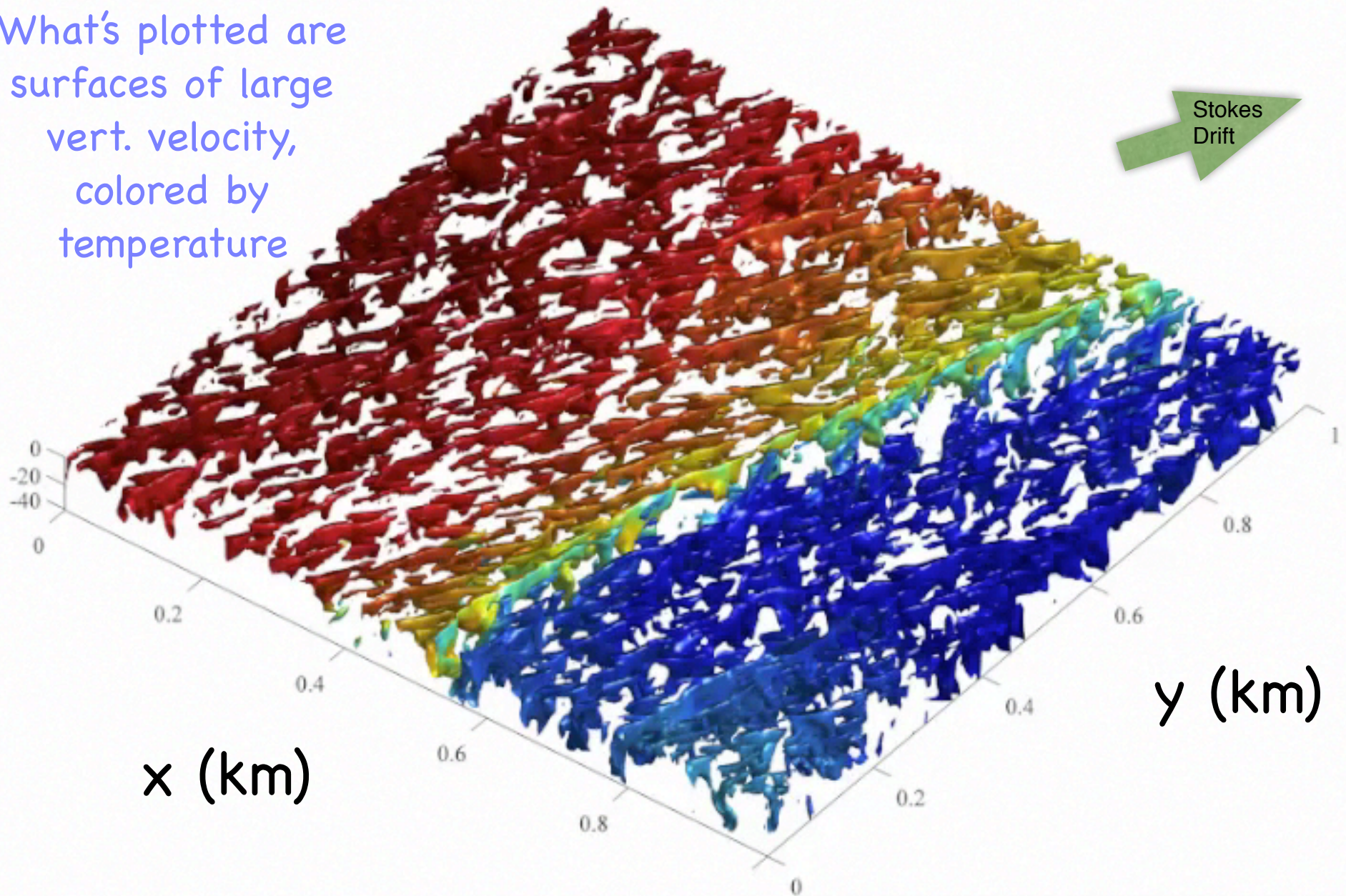
Resolution: 5m x 5m x -1.25m

1000x more gridpoints than CESM

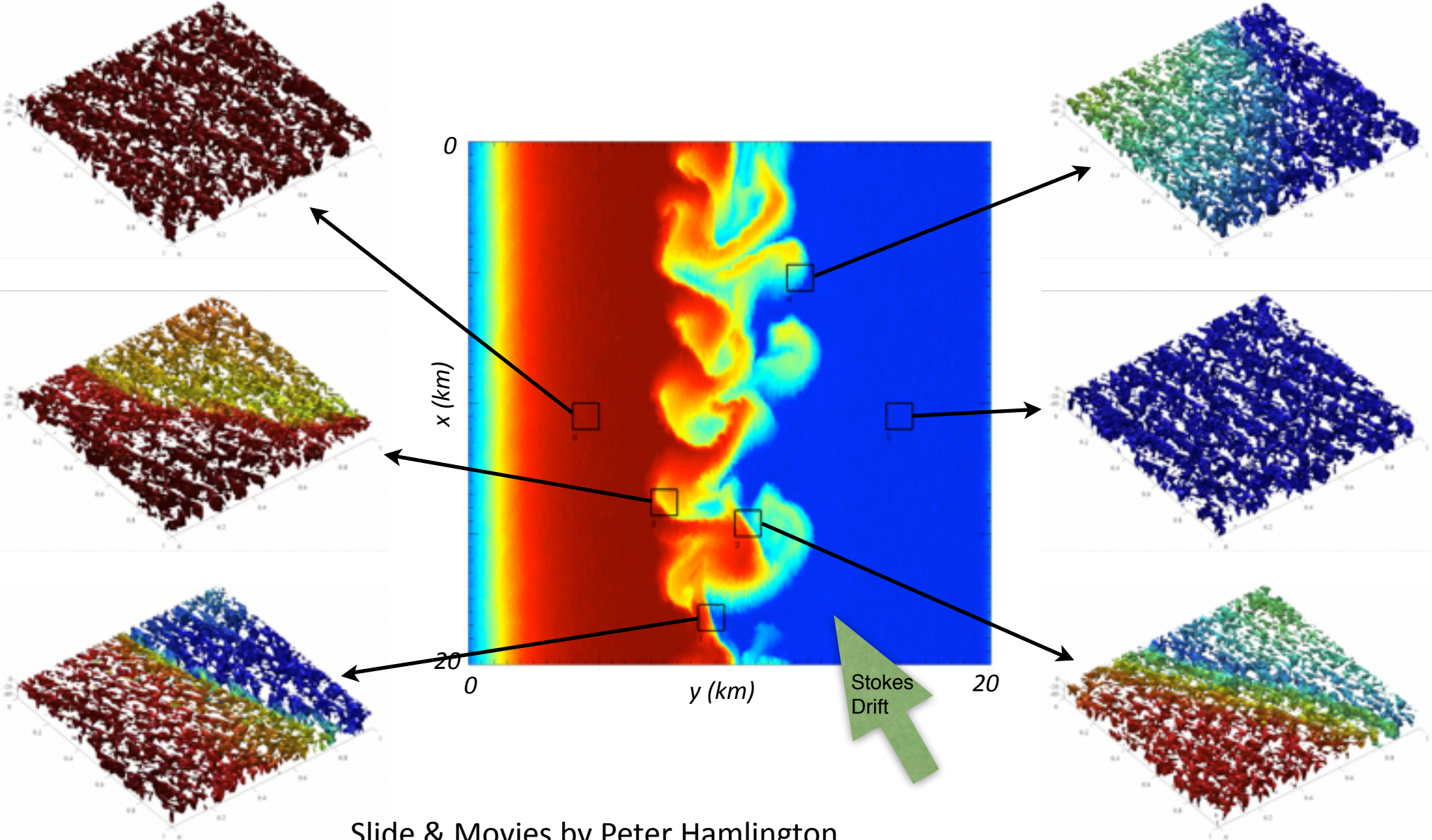


Zoom: Submeso-Langmuir Interaction!

What's plotted are
surfaces of large
vert. velocity,
colored by
temperature



Diverse types of interaction

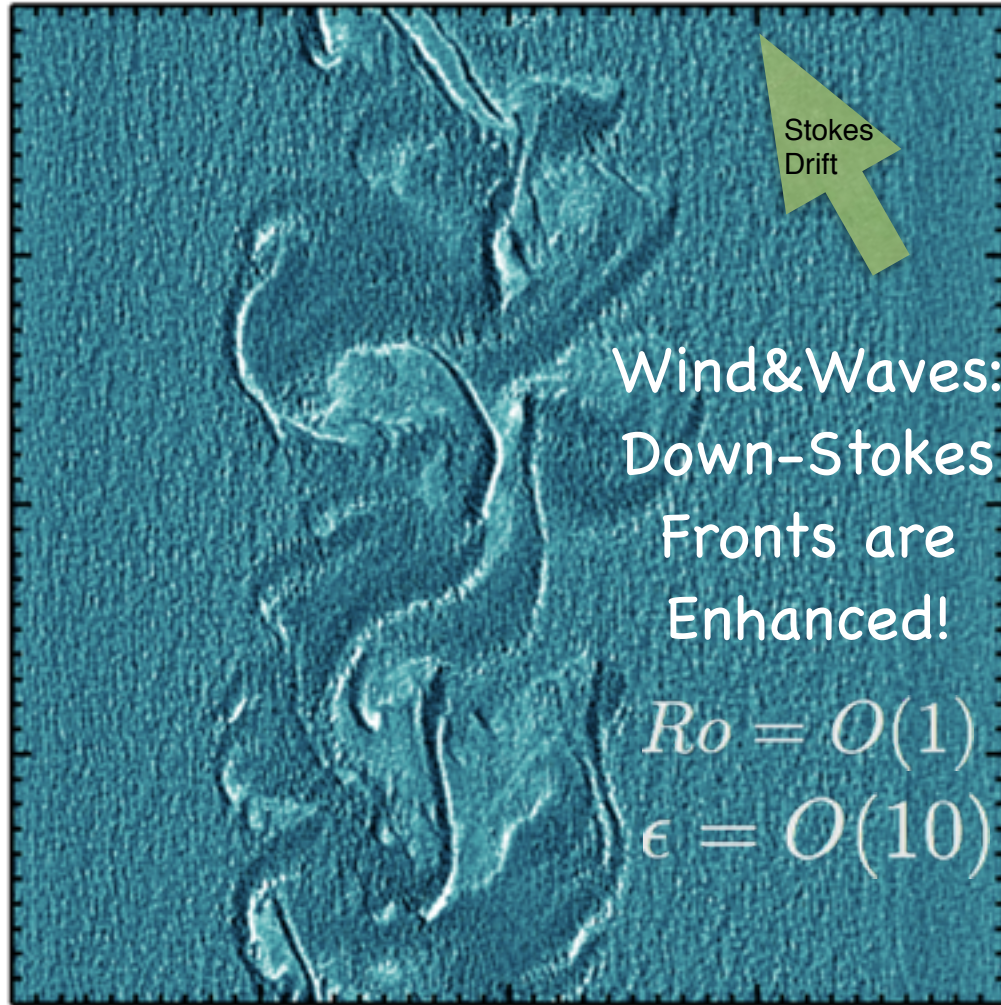


Slide & Movies by Peter Hamlington

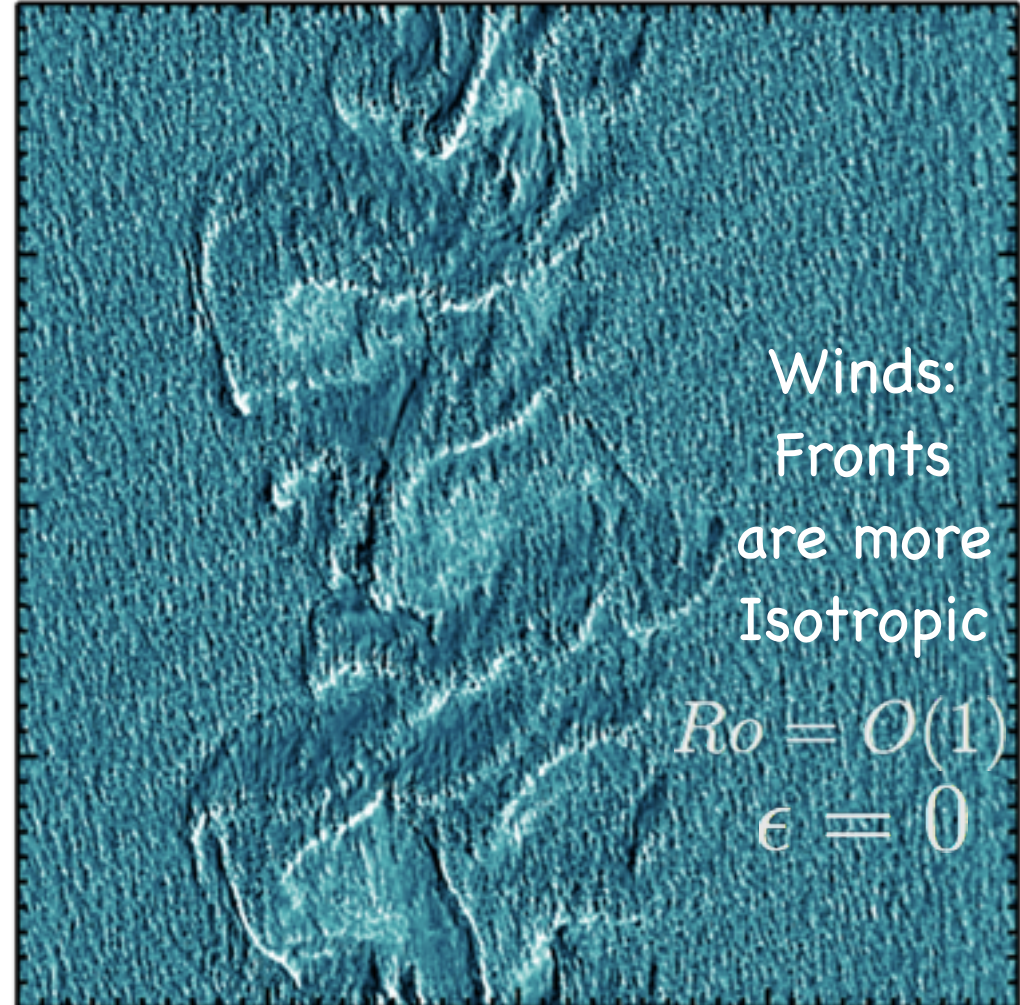
Are Fronts and Filaments different with Stokes shear force?

$$\frac{\alpha^2}{Ri} \left[w_{,t} + v_j^L w_{,j} + \frac{M_{Ro}}{Ro Ri} \right] = -\pi_{,z} + b + \epsilon v_j^L v_{j,z}^s + \frac{\alpha^2}{Re Ri} w_{,jj}$$

(b) LT, ω_z/f Wind & Waves



(d) ST, ω_z/f Wind Only



N. Suzuki and B. Fox-Kemper. Surface Wave Stokes Forces Influence Frontogenesis, JPO, in prep, 2014.

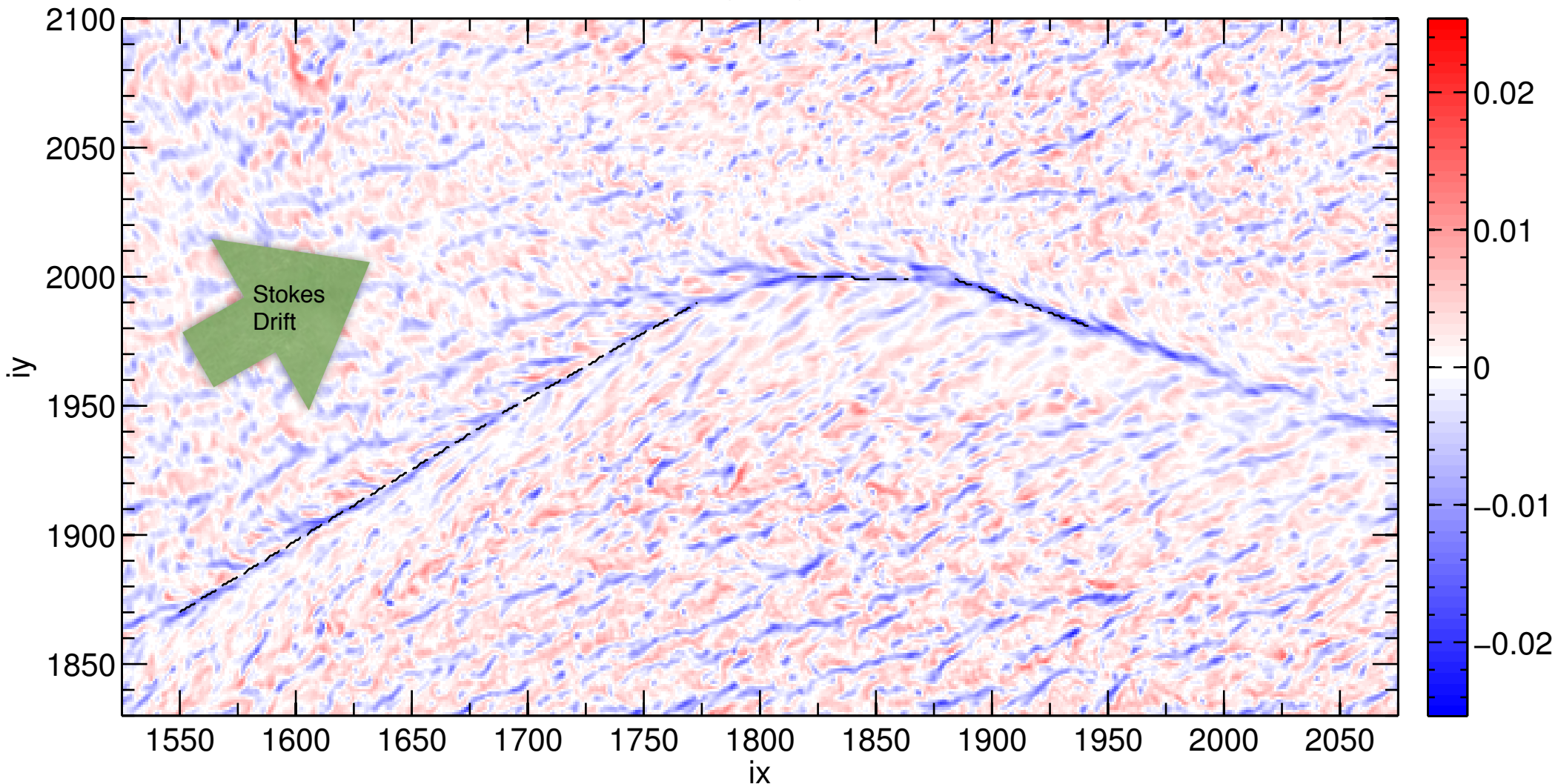
J. C. McWilliams and B. F-K. Oceanic wave-balanced surface fronts and filaments. Journal of Fluid Mechanics, 730:464-490, 2013.

P. E. Hamlington, L. P. Van Roekel, B. Fox-Kemper, K. Julien, and G. P. Chini. Langmuir-submesoscale interactions: Descriptive analysis of multiscale frontal spin-down simulations. Journal of Physical Oceanography, 2014. In press.

Let's examine 1 particular front

$$\epsilon = \frac{V^s H}{f L H_s} \approx 20$$

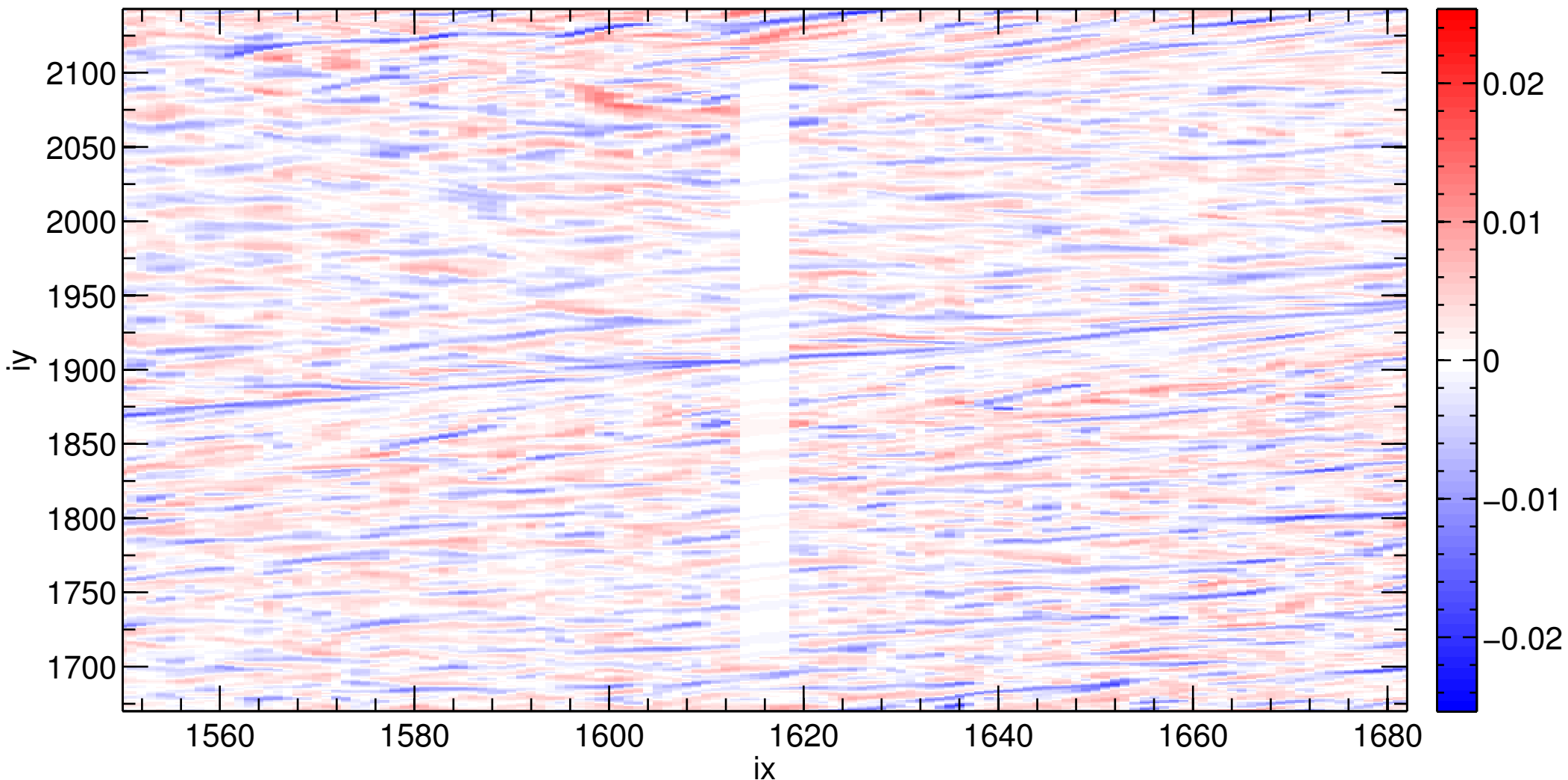
10min-ave. w (ms^{-1}) at $z = -12.5\text{m}$



Along-Front and 10min Average

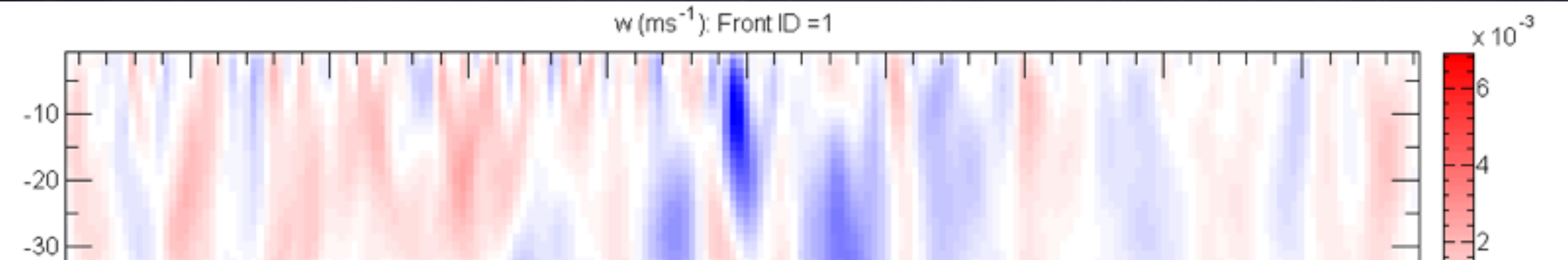
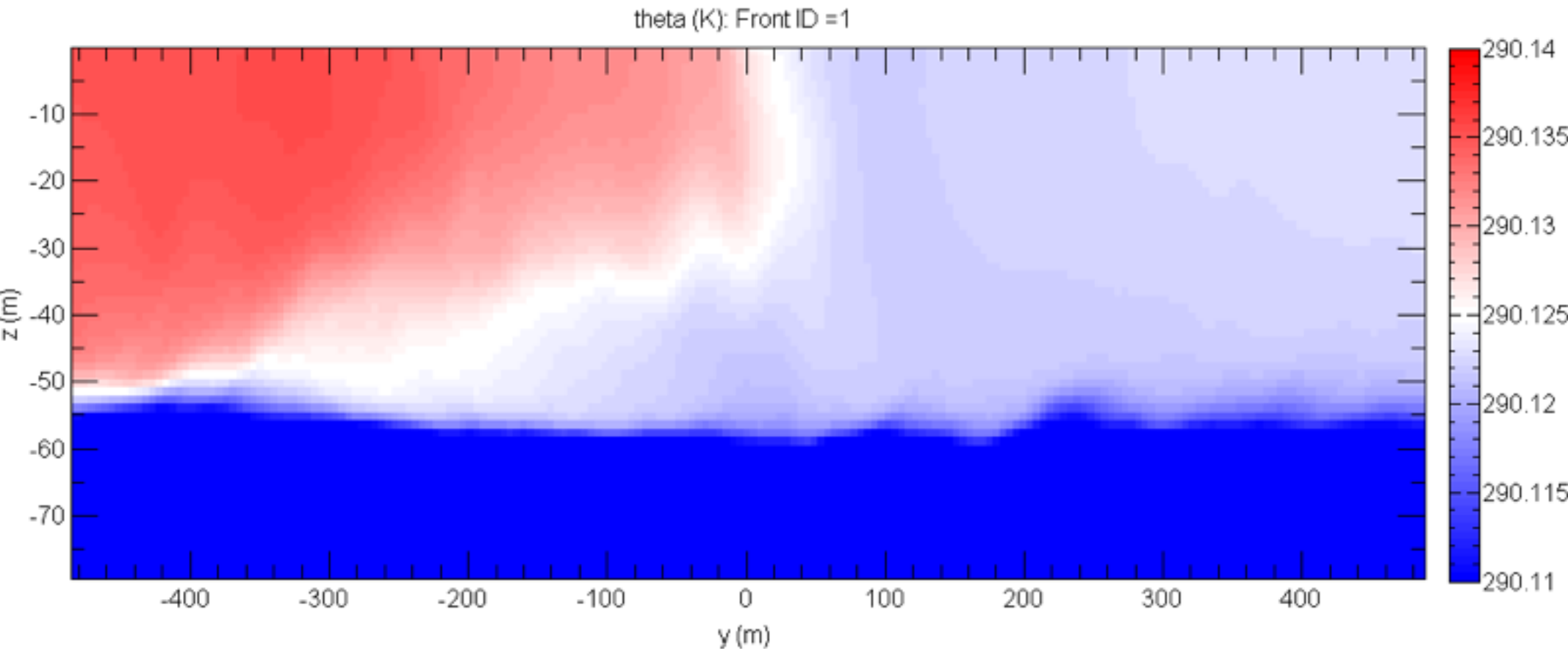
$$\epsilon = \frac{V^s H}{f L H_s} \approx 20$$

10min-ave w (ms^{-1}); Front ID = 1



Along-Front and 10min Average

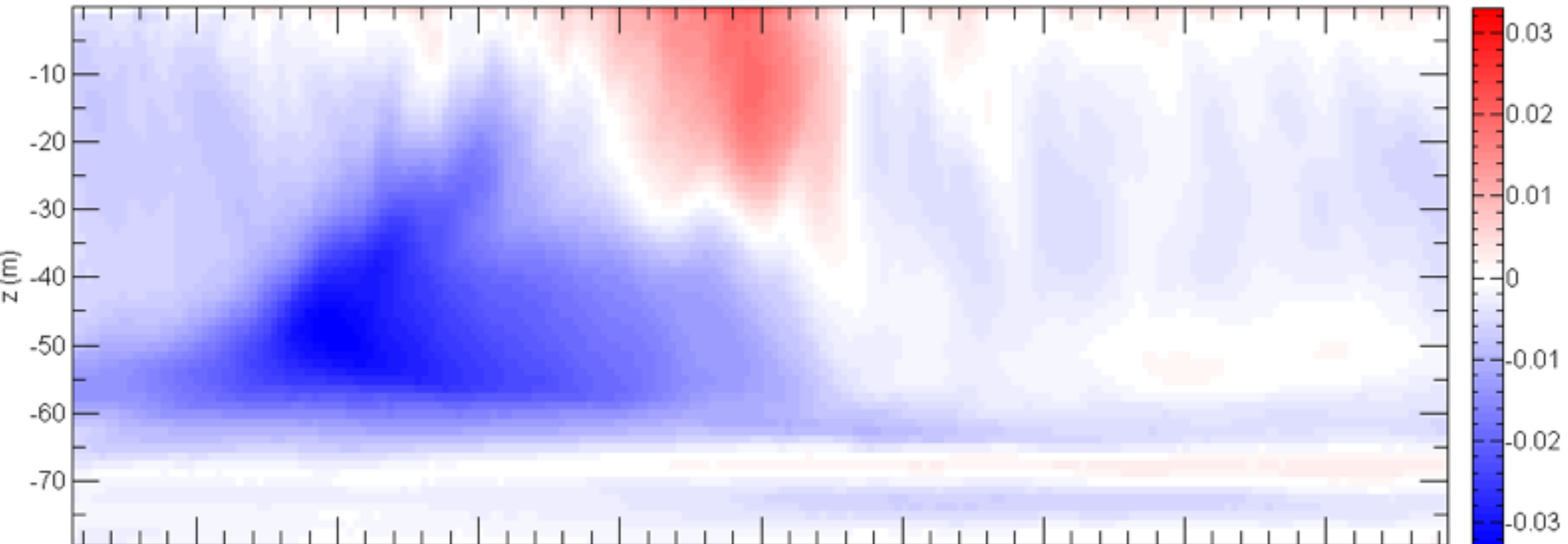
$$\epsilon = \frac{V^s H}{f L H_s} \approx 20$$



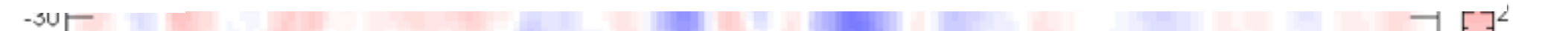
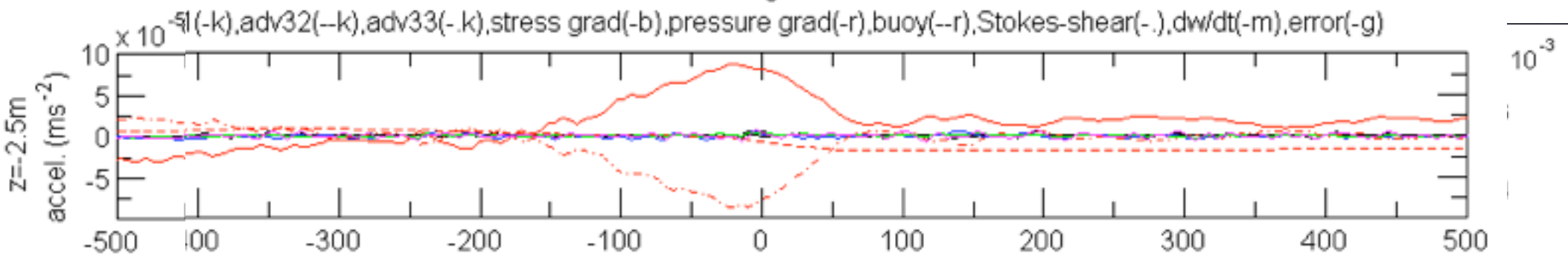
Along-Front and 10min Average

$$\epsilon = \frac{V^s H}{f L H_s} \approx 20$$

Eulerian u (ms⁻¹): Front ID = 1

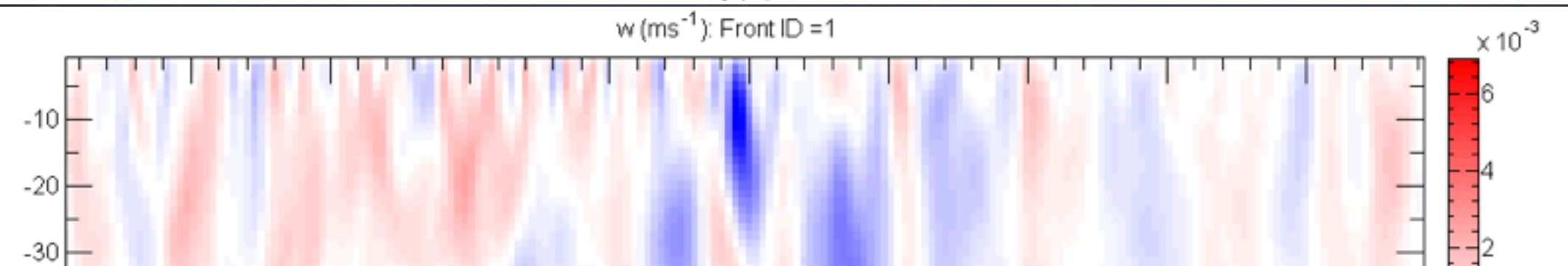
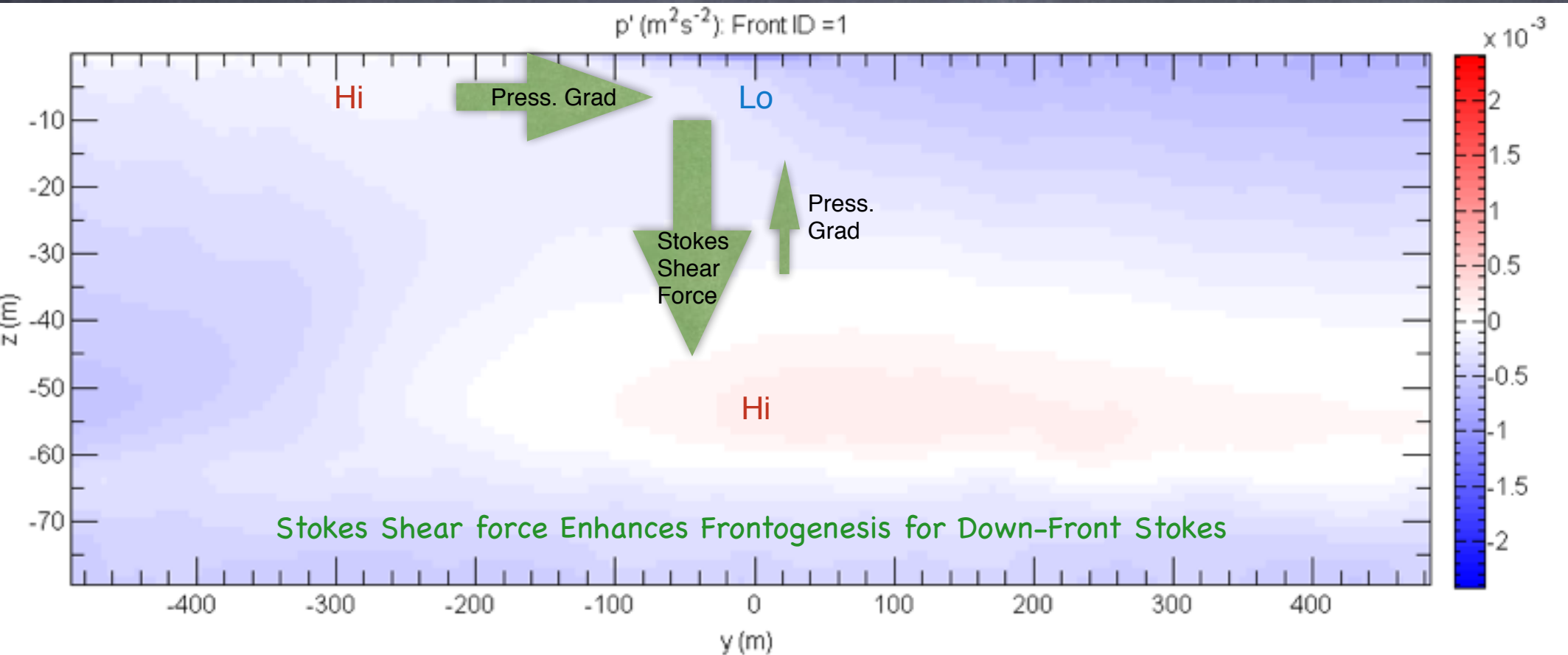


z-momentum budget: Front ID = 1



Along-Front and 10min Average

$$\epsilon = \frac{V^s H}{f L H_s} \approx 20$$



Conclusions

All papers at: fox-kemper.com/pubs

- Stokes shear force affects frontogenesis. Add/subtract 30–40% of frontal KE production for downfront/upfront Stokes drift
- The controlling parameter, ϵ , measures nonhydrostatic frontal effects. It can dominate other nonlinear effects, such as $O(1)$ Rossby, and is $O(20)$ in these simulated submesoscale fronts.
- Down–Stokes fronts are sharper than those directed across or esp. against Stokes and have horizontal velocity and pressures that are not antisymmetric about the max w .
- Future/Present: Cross-frontal transport pathways, wave–mean interaction, and frontal instabilities will be different
- Overall: Stokes force can affect submesoscale dynamics as well as Langmuir turbulence.

Along-Front and 10min Average

$$\epsilon = \frac{V^s H}{f L H_s} \approx 20$$

10min-ave along-front velocity (ms^{-1}); Front ID = 1

