

# The Surface Wave Influence on Mixed-Layer Frontal Currents and Multi-scale Turbulence

## Nonhydrostatic, Ageostrophic, Submesoscale Frontogenesis under Wave and Wind Forcing

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A new form of the Boussinesq Craik-Leibovich eq.

$$\frac{\partial \mathbf{u}}{\partial t} + \underbrace{(\mathbf{u}^L \cdot \nabla) \mathbf{u}}_{\text{Lagrangian advection: responsible for the MKE-TKE conversion}} = -\nabla p - \mathbf{f} \times \mathbf{u}^L + b\hat{z} - \underbrace{u_j^L \nabla u_j^S}_{\text{Stokes-shear force: The wave energy transfers via this term}}$$

Lagrangian advection:  
responsible for the MKE-TKE  
conversion

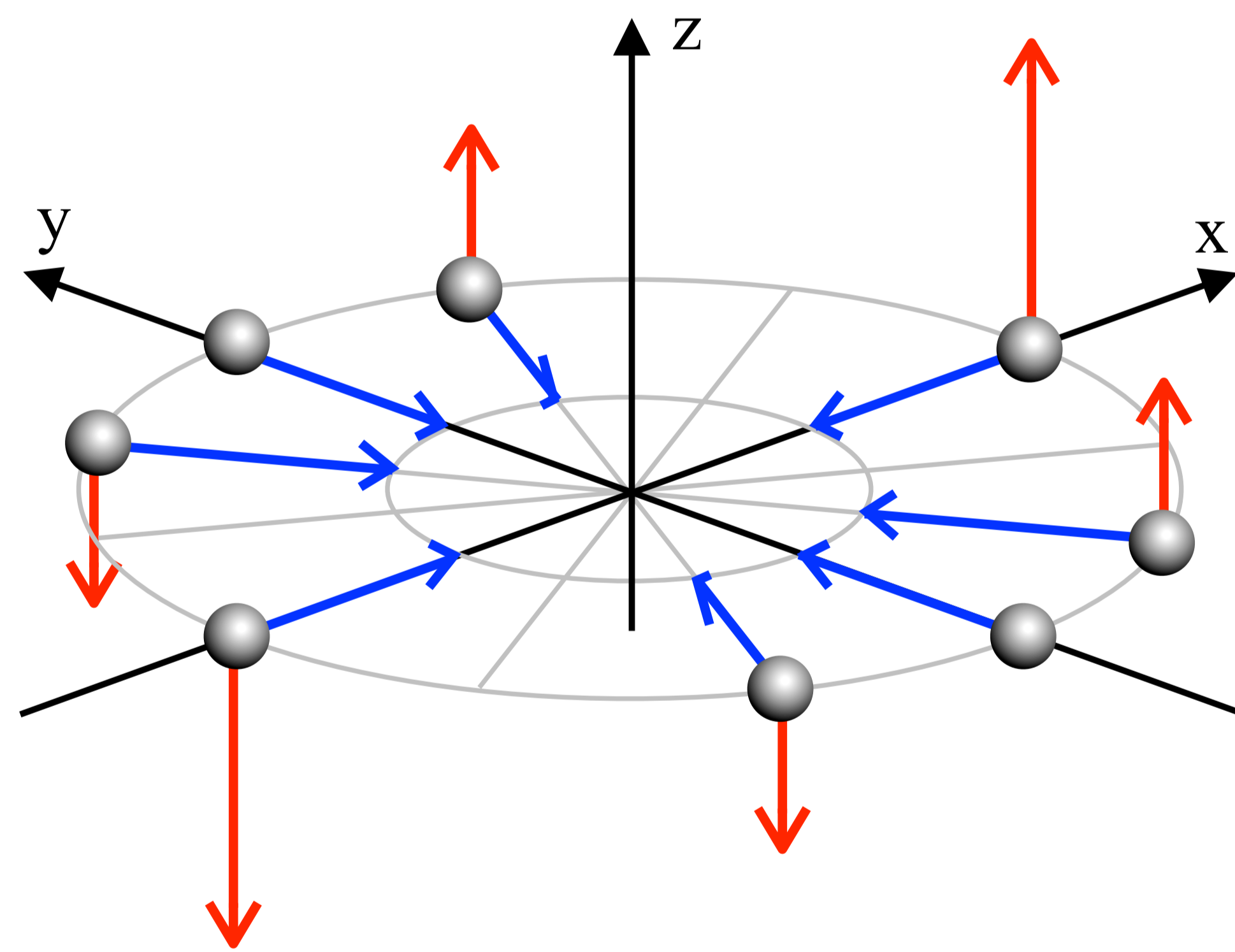
Stokes-shear force:  
The wave energy  
transfers via this term.

For horizontally uniform Stokes drift with  $w^L = 0$

$$\frac{\partial u}{\partial t} + u^L \frac{\partial u}{\partial x} + v^L \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z} = -\frac{\partial p'}{\partial x} + f v^L$$

$$\frac{\partial v}{\partial t} + u^L \frac{\partial v}{\partial x} + v^L \frac{\partial v}{\partial y} + w \frac{\partial v}{\partial z} = -\frac{\partial p'}{\partial y} - f u^L$$

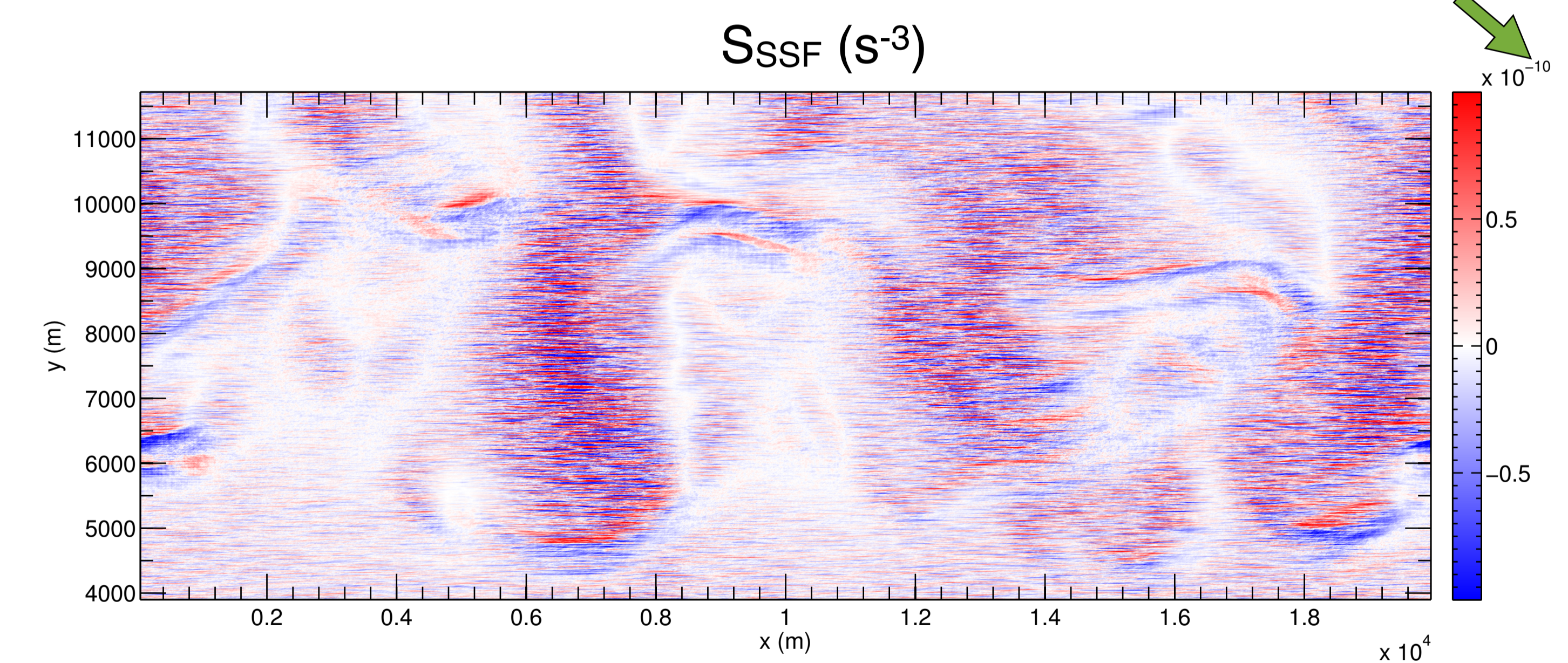
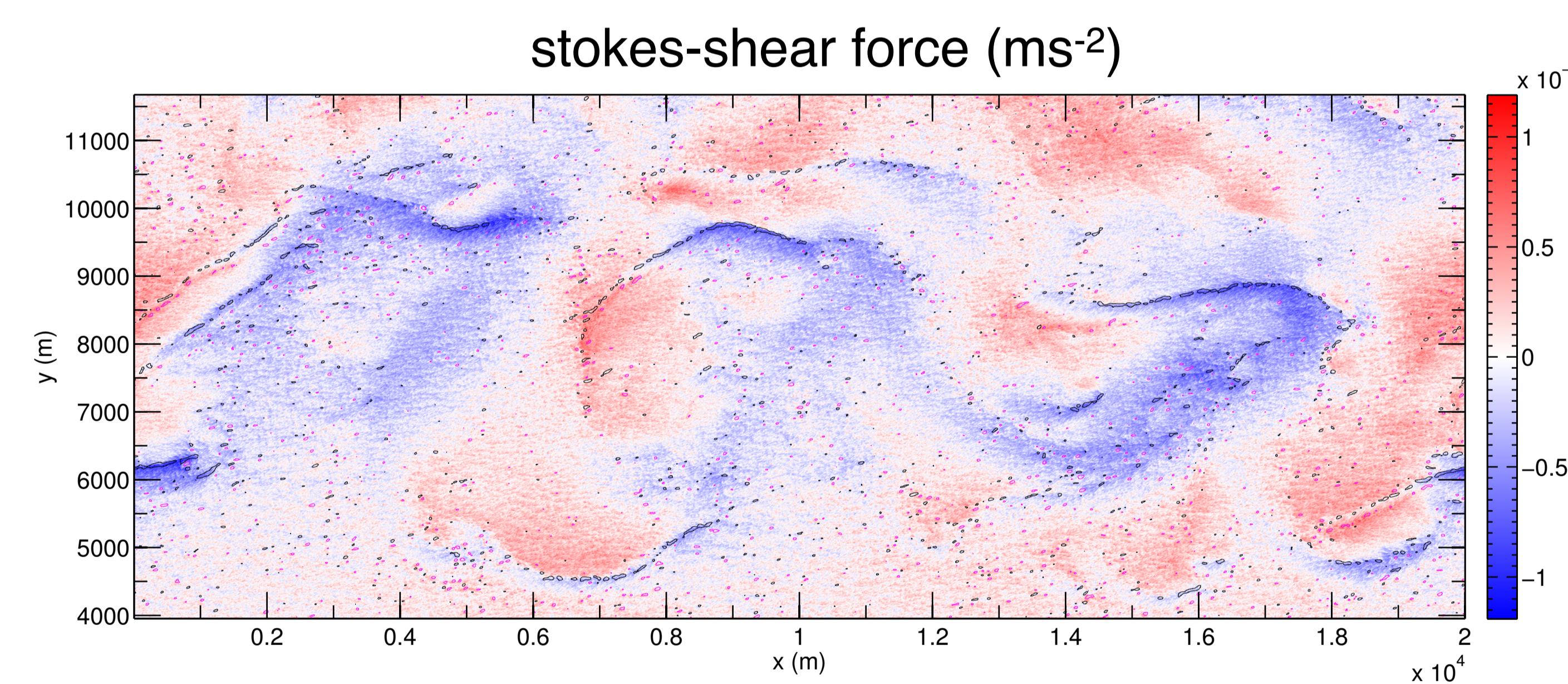
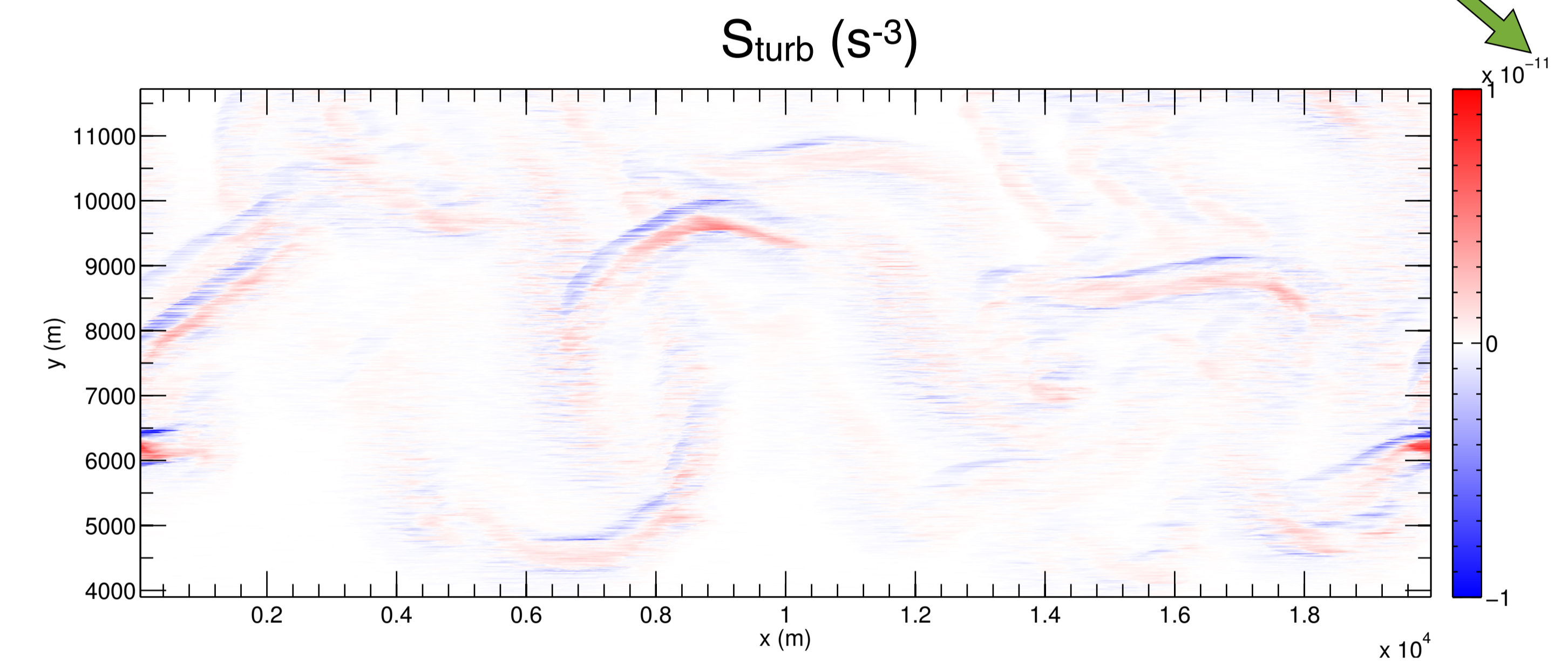
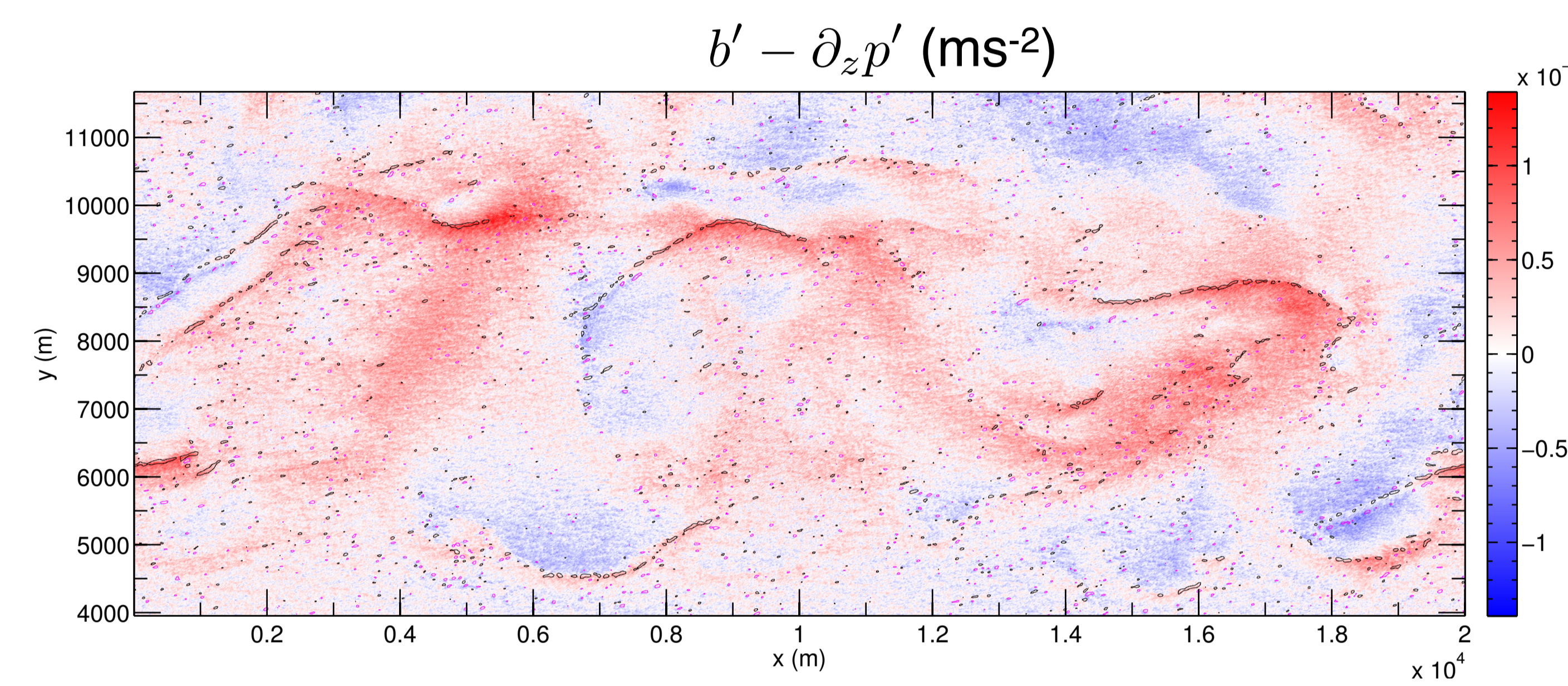
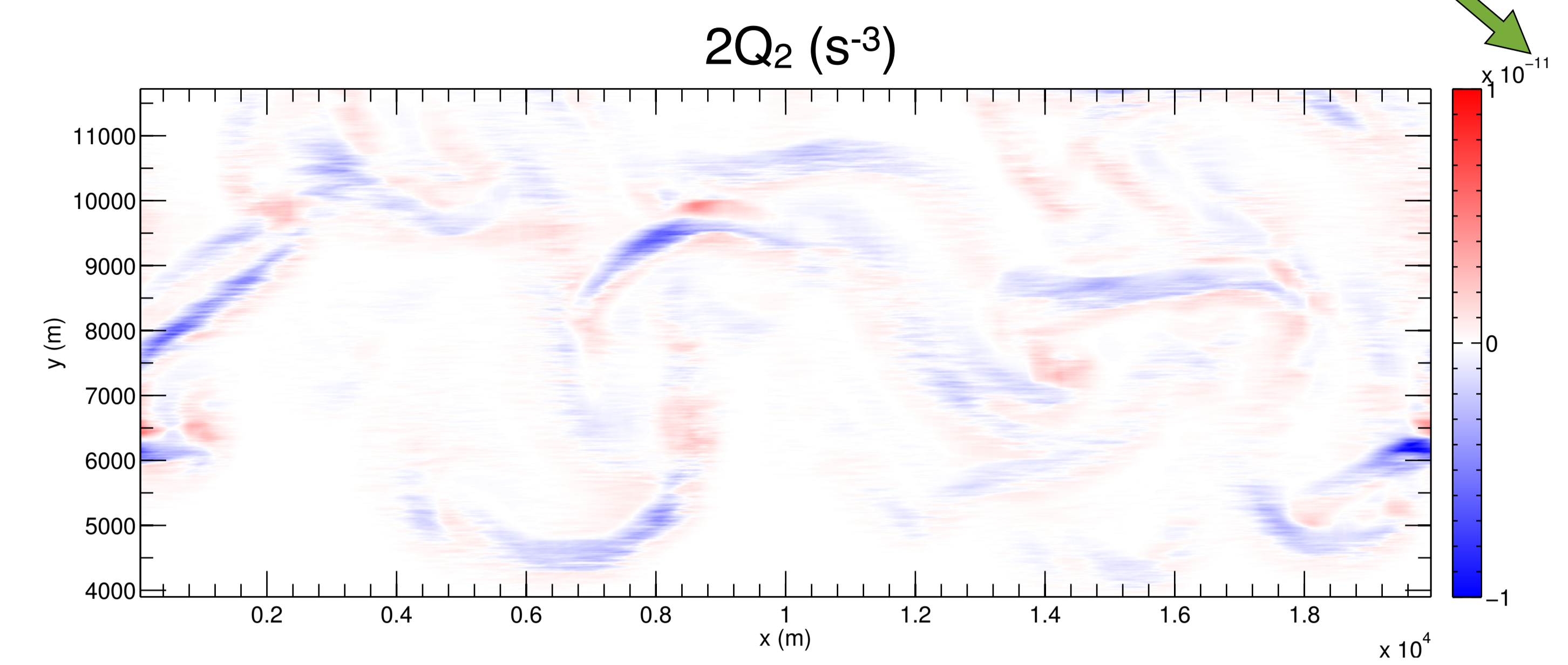
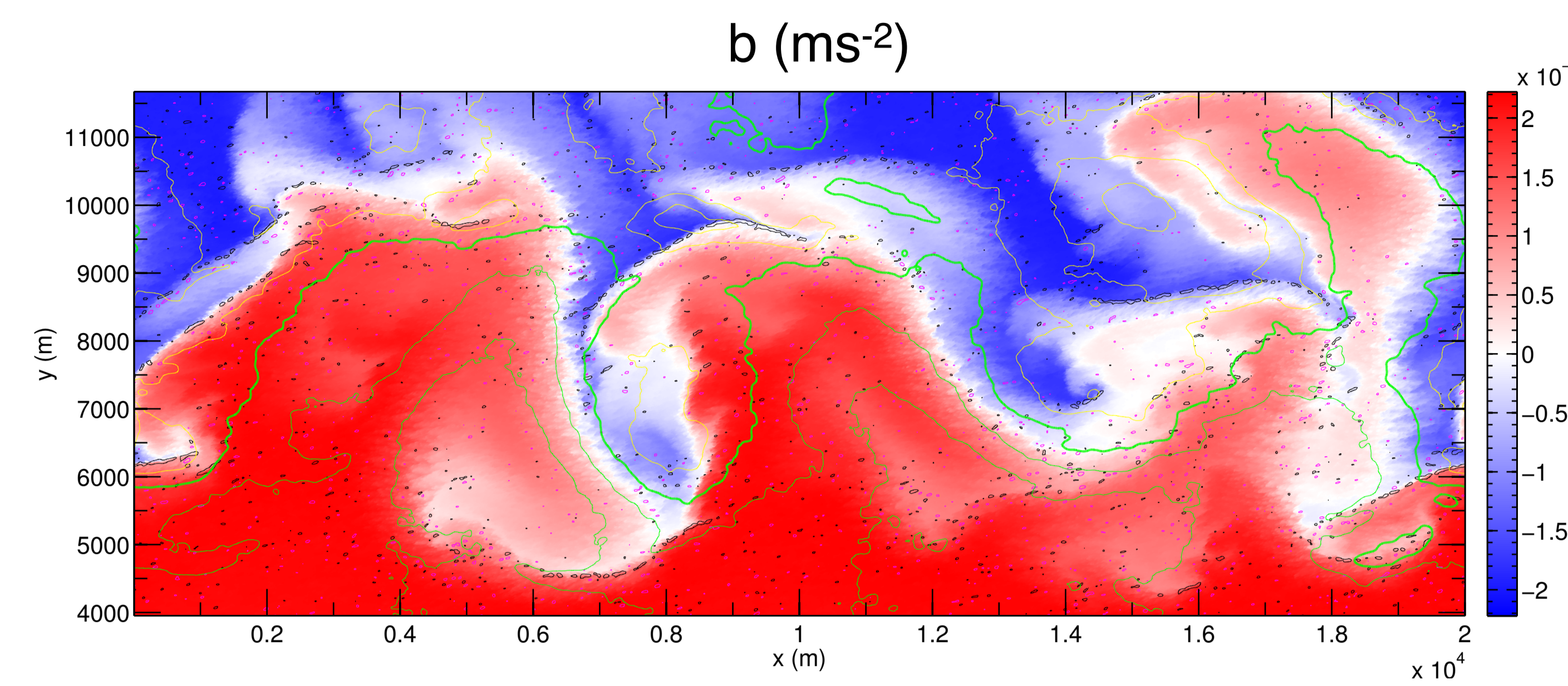
$$\frac{\partial w}{\partial t} + u^L \frac{\partial w}{\partial x} + v^L \frac{\partial w}{\partial y} + w \frac{\partial w}{\partial z} = -\frac{\partial p'}{\partial z} + b' - u' \frac{\partial u^S}{\partial z} - v' \frac{\partial v^S}{\partial z}$$



↕ : Stokes-shear force    ● : water parcel  
↖ : turbulent velocity

Wave-influenced Sawyer-Eliassen eq.

$$N_*^2 \frac{\partial^2 \psi}{\partial y^2} + F_*^2 \frac{\partial^2 \psi}{\partial z^2} + 2M_*^2 \frac{\partial^2 \psi}{\partial y \partial z} = 2Q_2 + S_{turb} + S_{SSF}$$



across-front structure of  $b$  ( $\text{ms}^{-2}$ ) and velocity

