



Geophysics from Kolmogorov to Climate

Baylor Fox-Kemper
Brown University

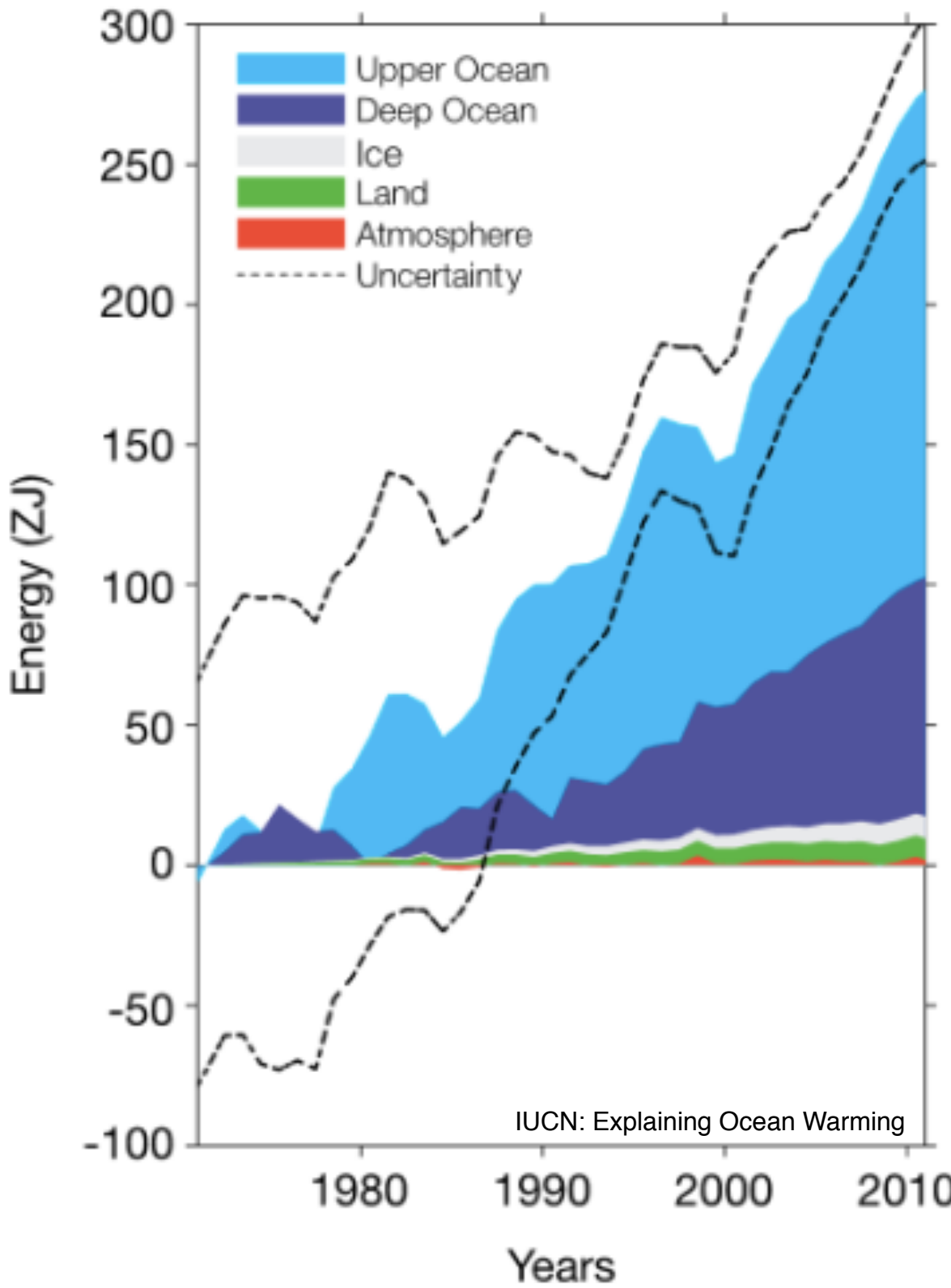
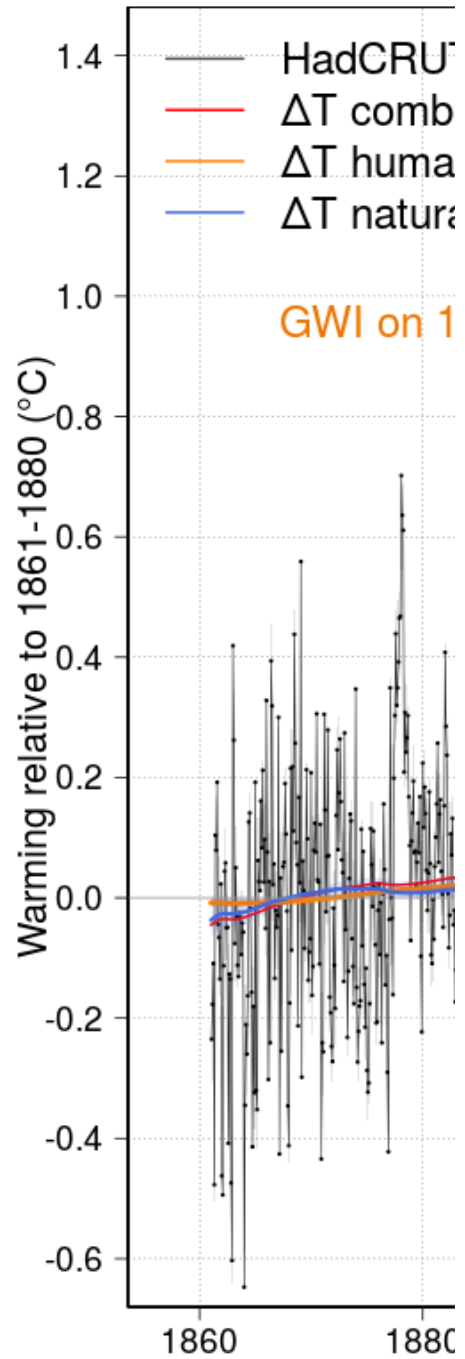
DEEP [Dept. of Earth, Environmental, and Planetary] Sciences

Climate Fluctuations and Non-equilibrium Statistical
Mechanics: an interdisciplinary dialogue

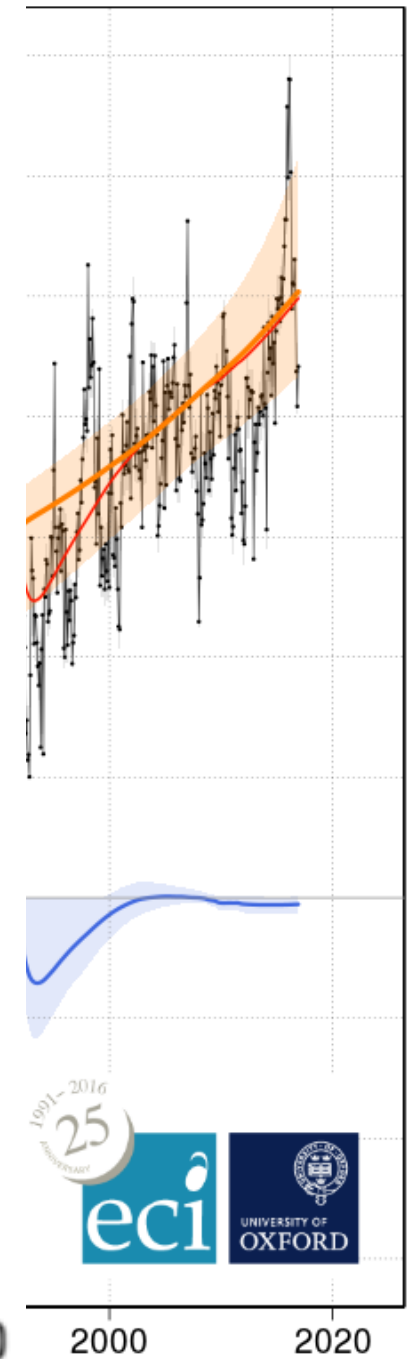
Dresden 7/17/17, 11-11:50

Sponsors: NSF 1245944, 1258907, 1350795, Gulf of Mexico
Research Initiative, and the Office of Naval Research

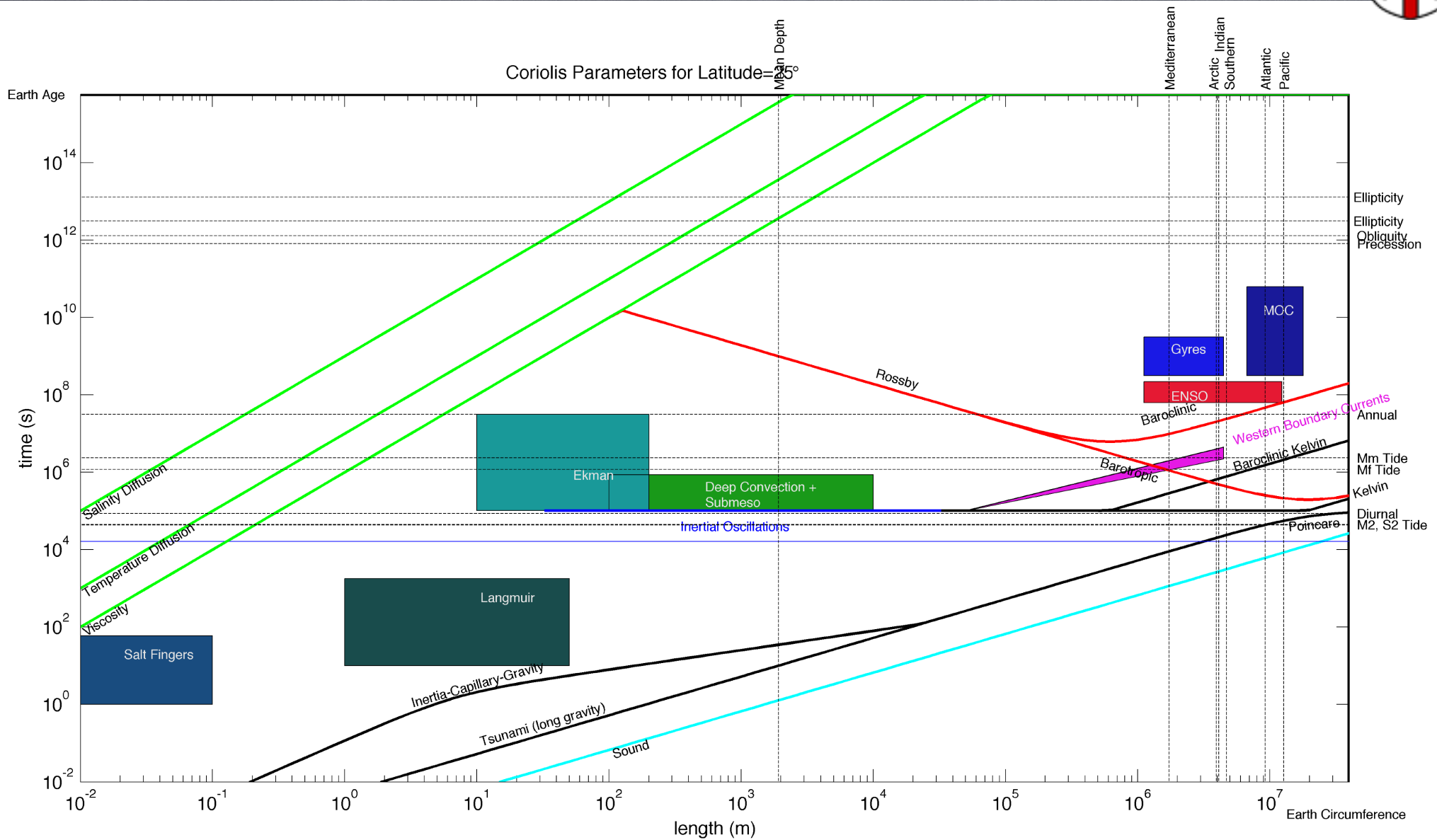
Global



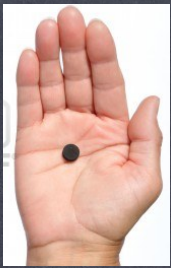
ec 2016



The Ocean is Vast & Diverse



The climate also depends on atmosphere, cryosphere, biosphere, pedosphere, lithosphere & coupled modes!

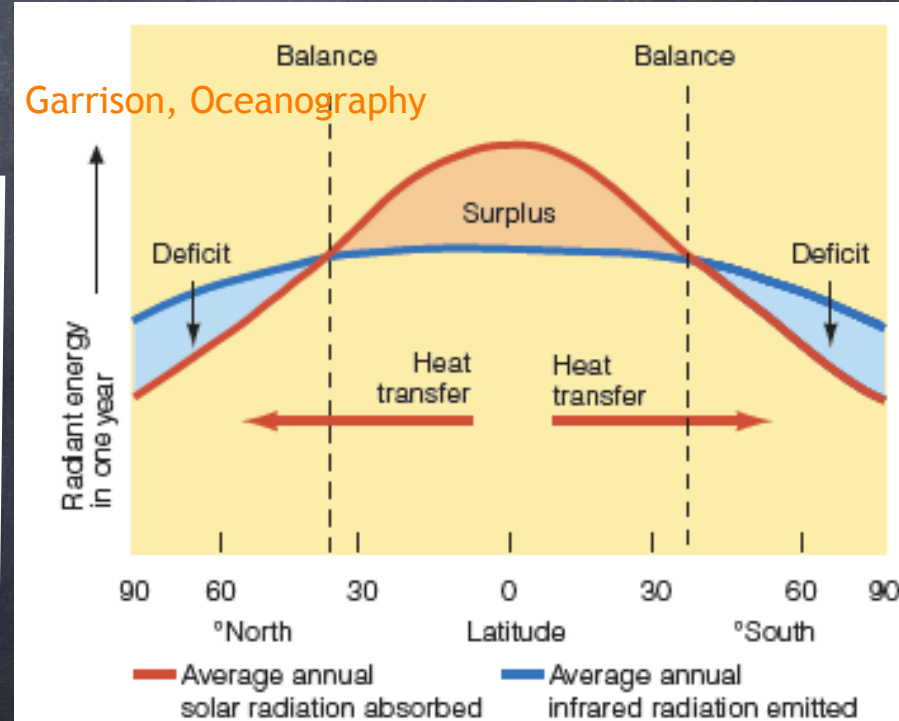
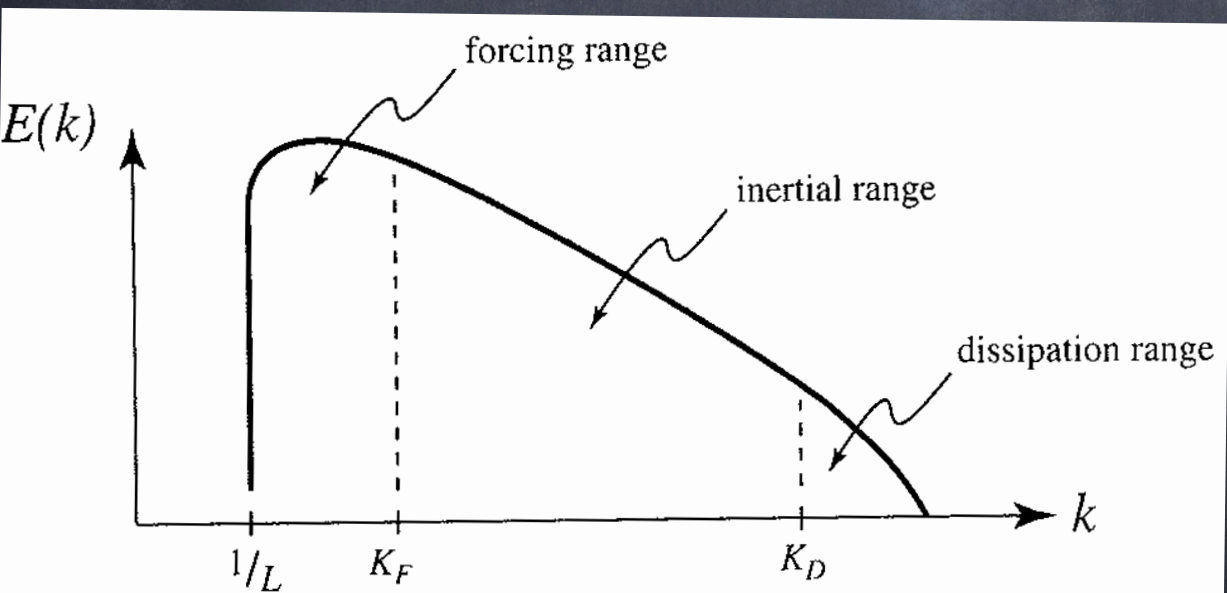
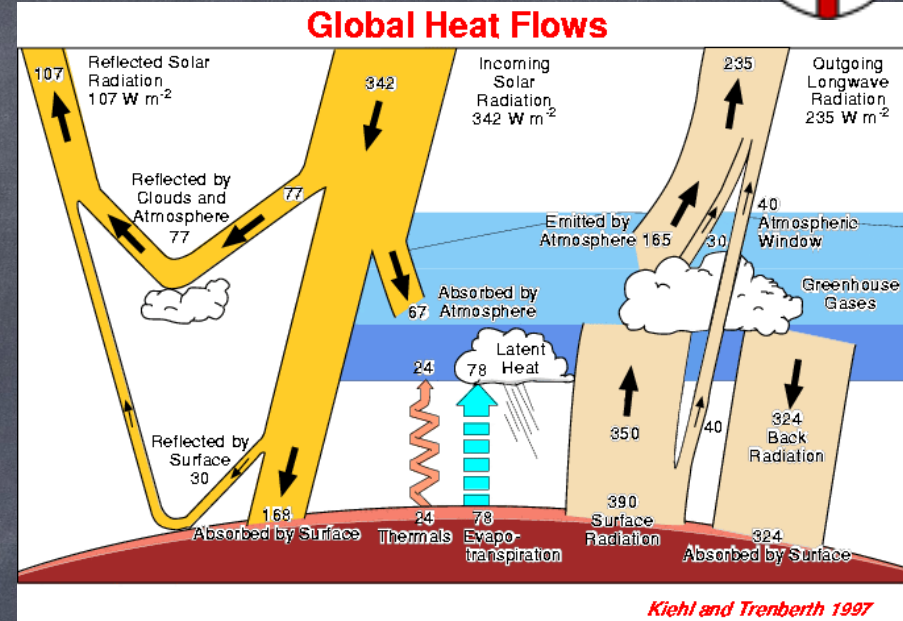


The Earth's Climate System is driven by the Sun's light

(minus outgoing infrared) on a global scale



KE dissipation concludes turbulence cascades to scales about a billion times smaller



CLIMATE

Thermal Energy Budget



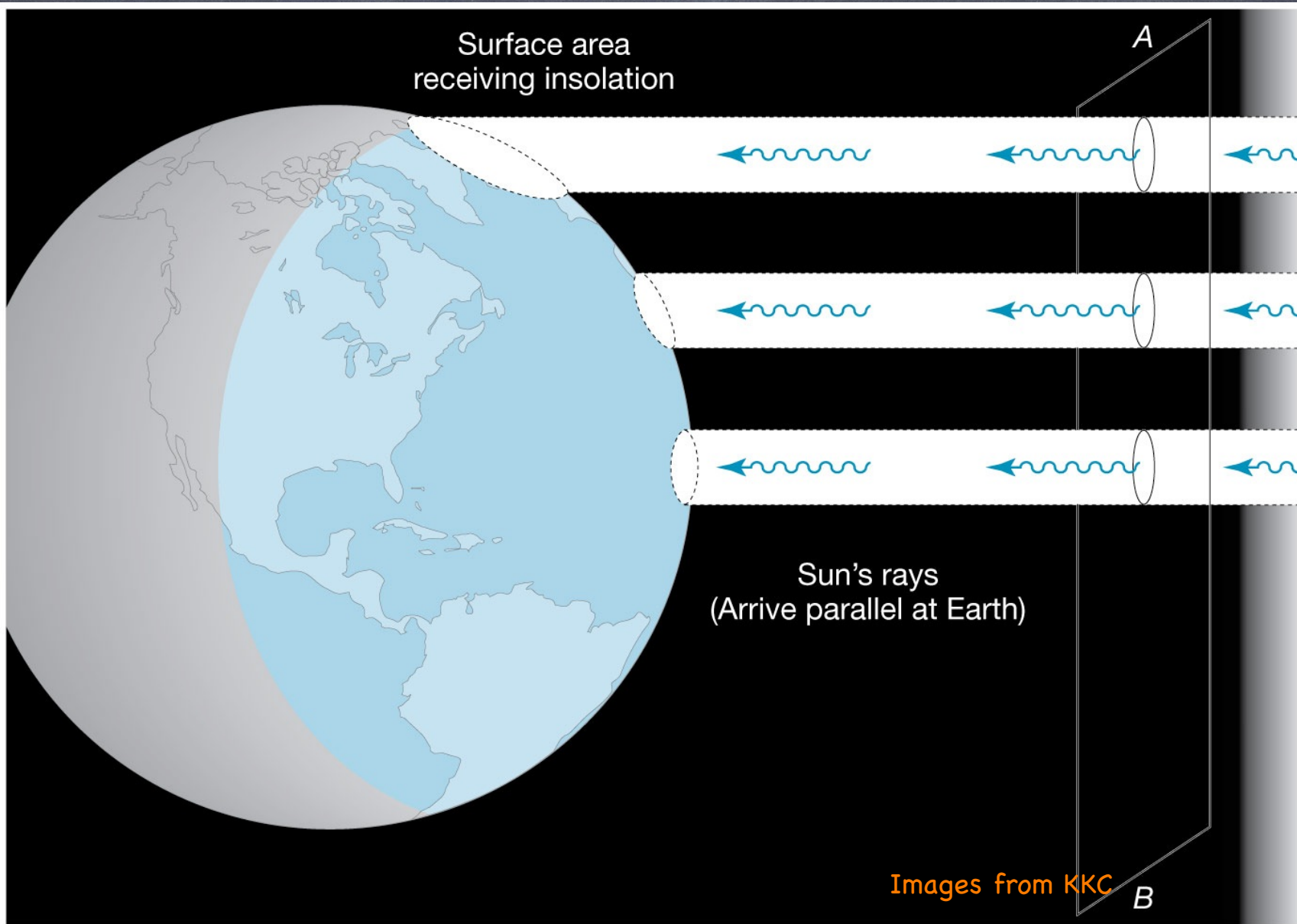
Insolation: The amount of energy per unit time in arriving electromagnetic radiation that through a unit surface area.

Dimensions $(\text{Energy}/\text{T}/\text{L}^2 = \text{Power}/\text{L}^2) = S_0/4 = 1370 \text{ W/m}^2/4 = 342 \text{ W/m}^2$

Away from tropics, the Sun's light does not arrive perp. to the Earth's surface (sun not directly overhead)

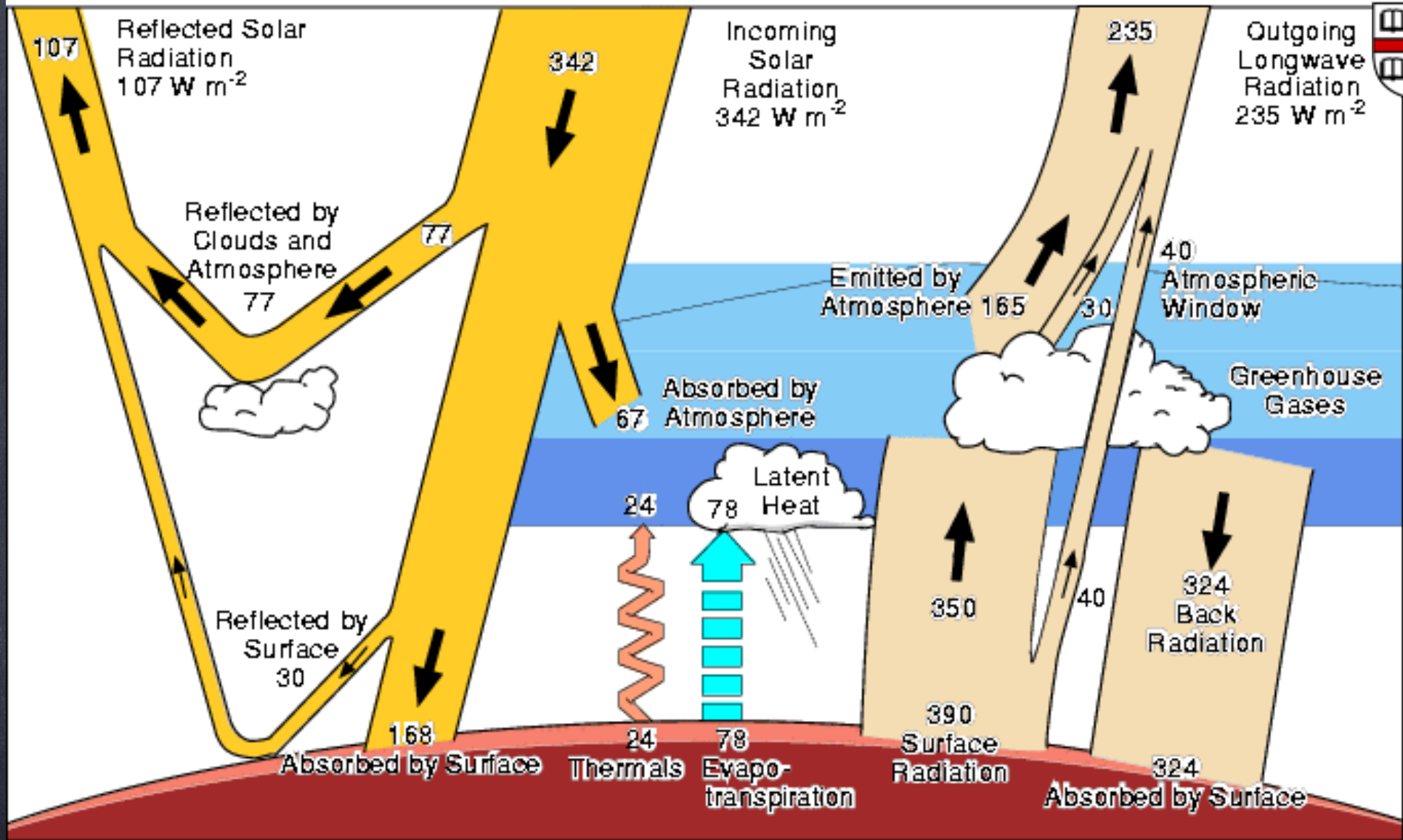
So poles have shorter days, increased albedo, decreased perp. component

Reduced Polar Power!



Images from KKC **B**

Global Heat Flows



Kiehl and Trenberth 1997

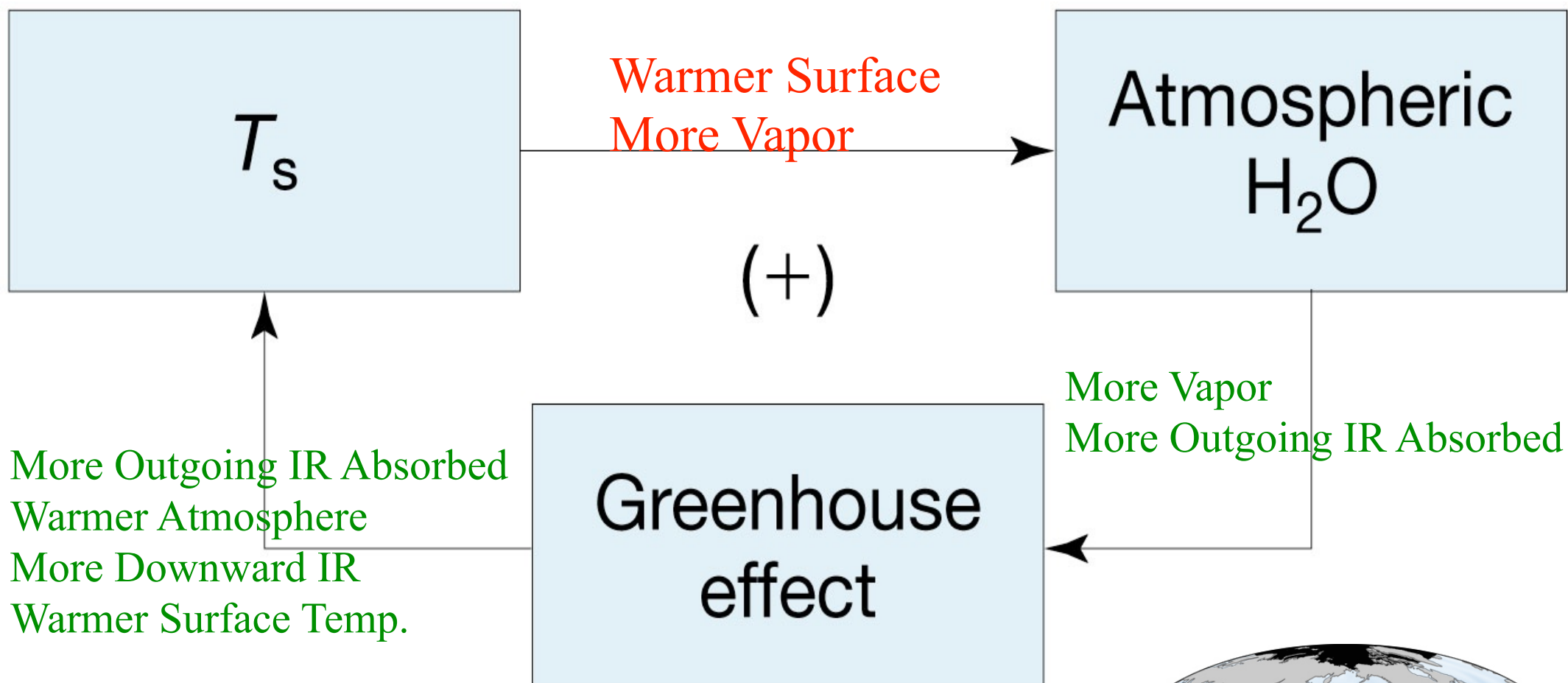
Simple: Planetary Energy Balance

$$c \frac{dT}{dt} = R_{\text{incoming}}(T) - R_{\text{outgoing}}(T)$$

E.g., Water Vapor Feedback & $R_{\text{outgoing}}(T)$:

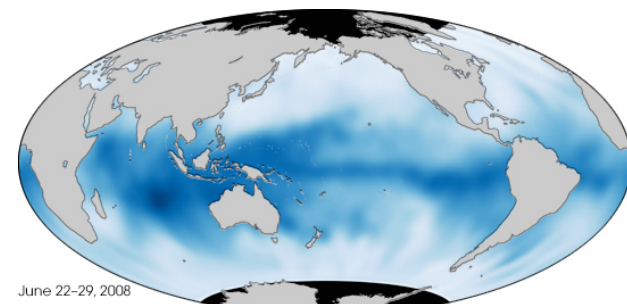
Water Vapor is the most important GHG on Earth, not only because it absorbs most of the outgoing IR, but also because it responds to surface temperature changes

8



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07-Energy3



earthobservatory.nasa.gov

Water Vapor
dry moist



Surface, Mixed Layer, Seasons?

0.7 W/m²

=

Atmosphere:

1.5K/yr

=

3.4m Ocean:

1.5K/yr

=

34m Ocean:

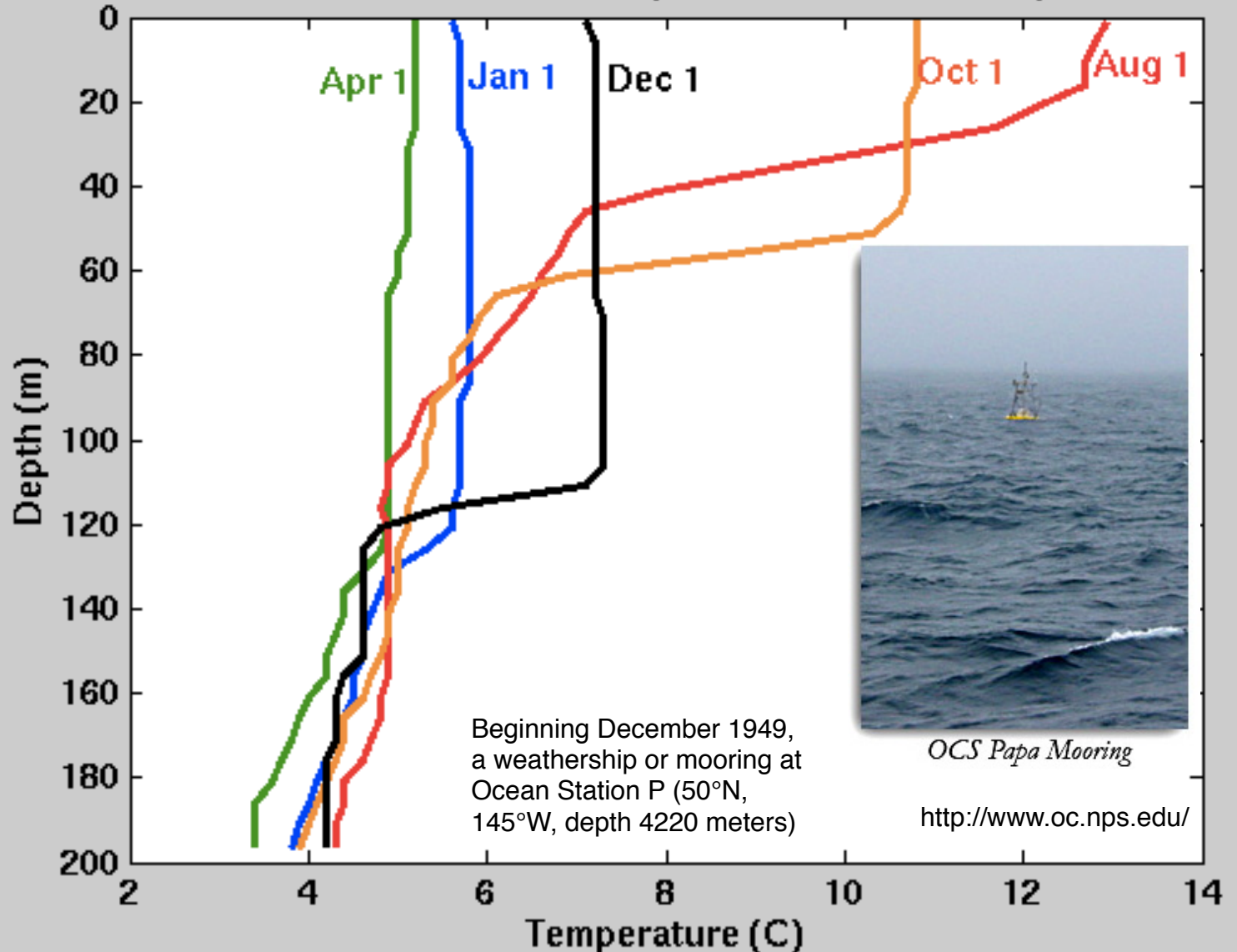
0.15K/yr

=1% of

mixed layer seasonality

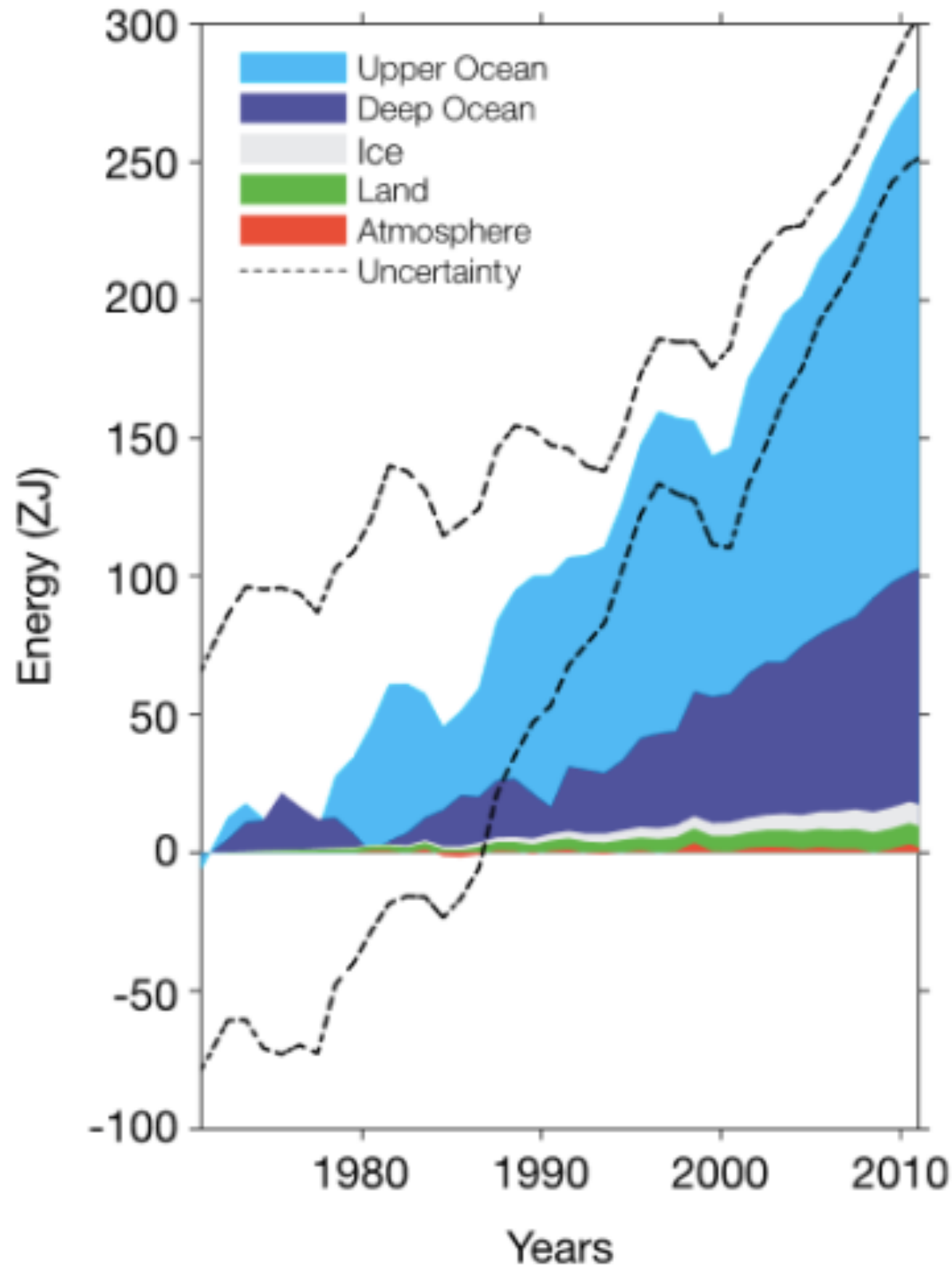


Annual Cycle of Temperature at OWS Papa

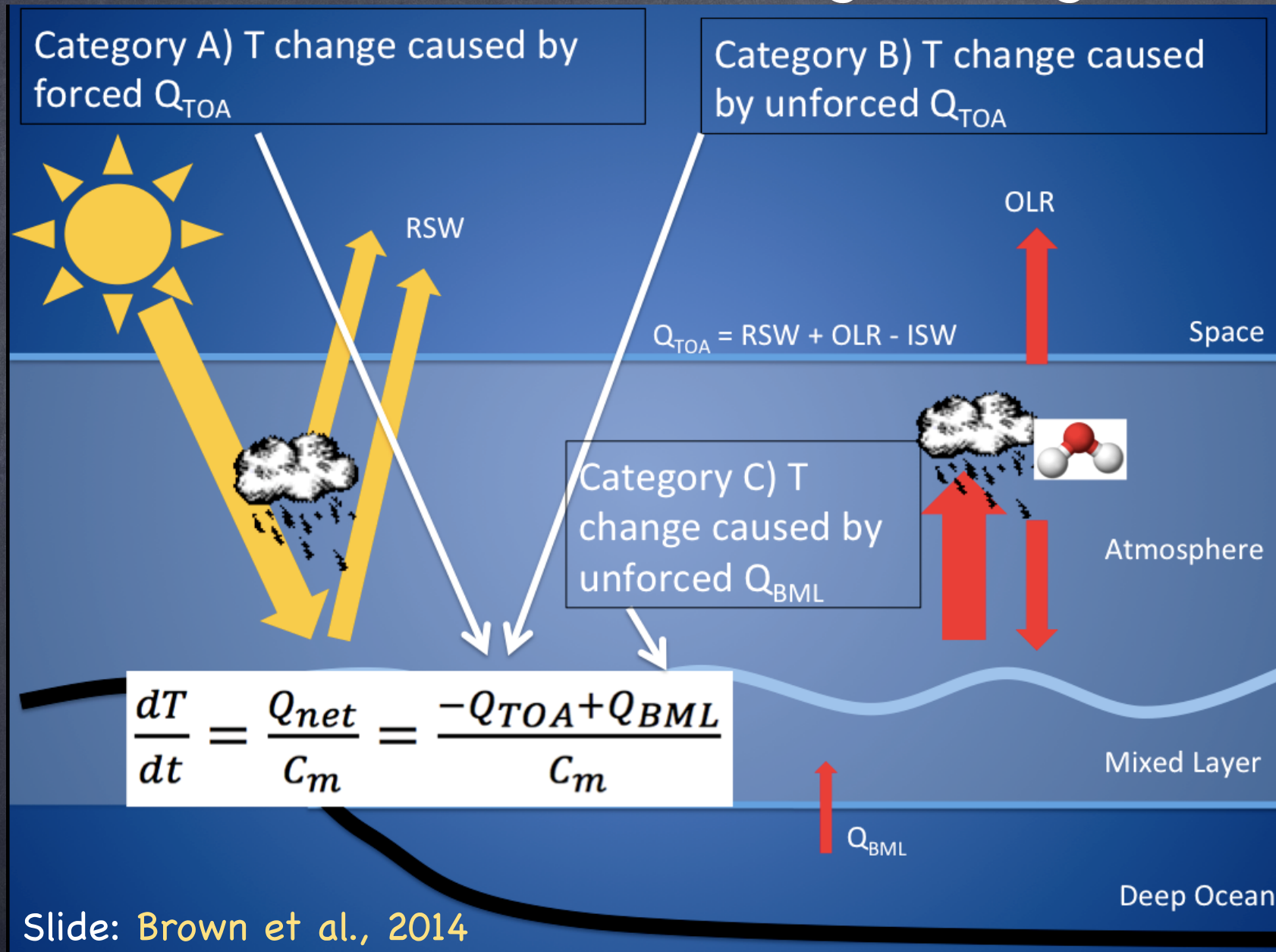


Air-Sea Exchanges

- Ocean heat capacity, even just mixed layer, is vastly larger than the atmosphere
- Air-sea heat fluxes are sensitive to air-sea temperature differences (and wind—i.e. momentum differences)
- Thus heat anomalies end up in the ocean



GMST: Surface Energy Budget

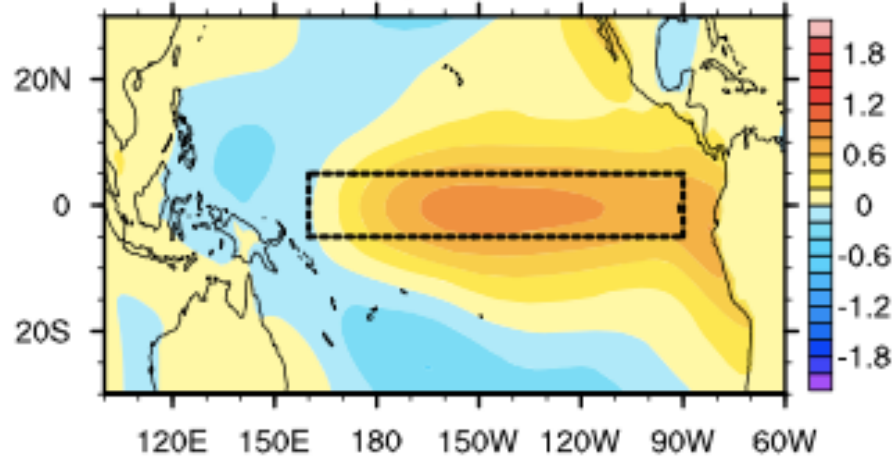


Slide: Brown et al., 2014

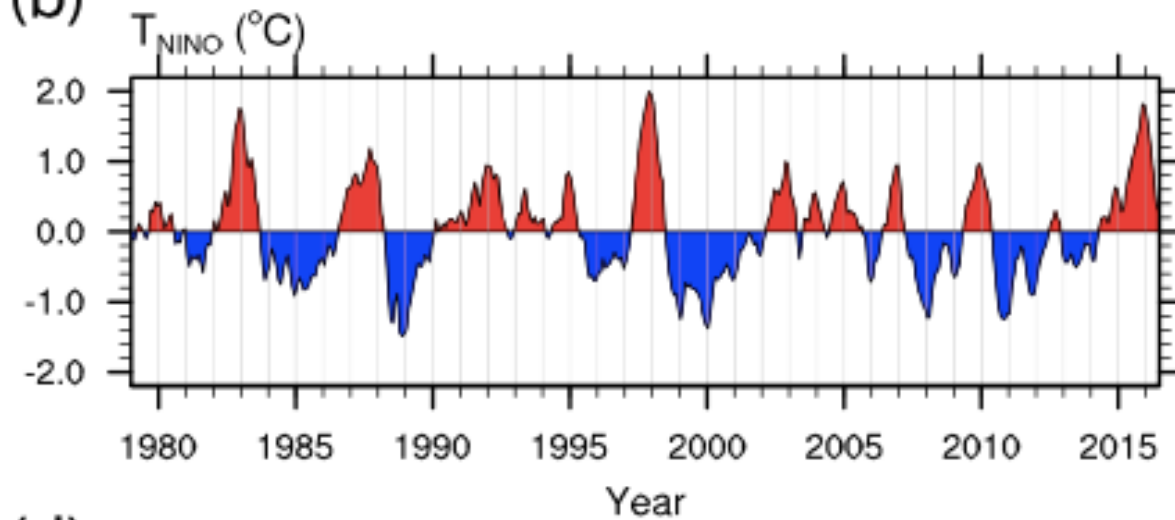
- 3.4m of ocean has heat capacity of whole atmosphere
- Ocean Mixed Layer is about 100m deep.

Effect of Climate Modes, e.g., Hu & Fedorov (2017)

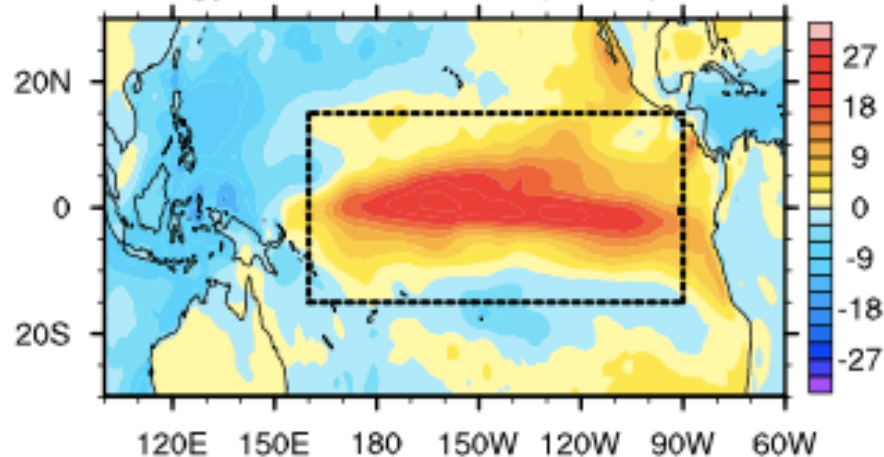
(a) Sea surface temperature (°C)



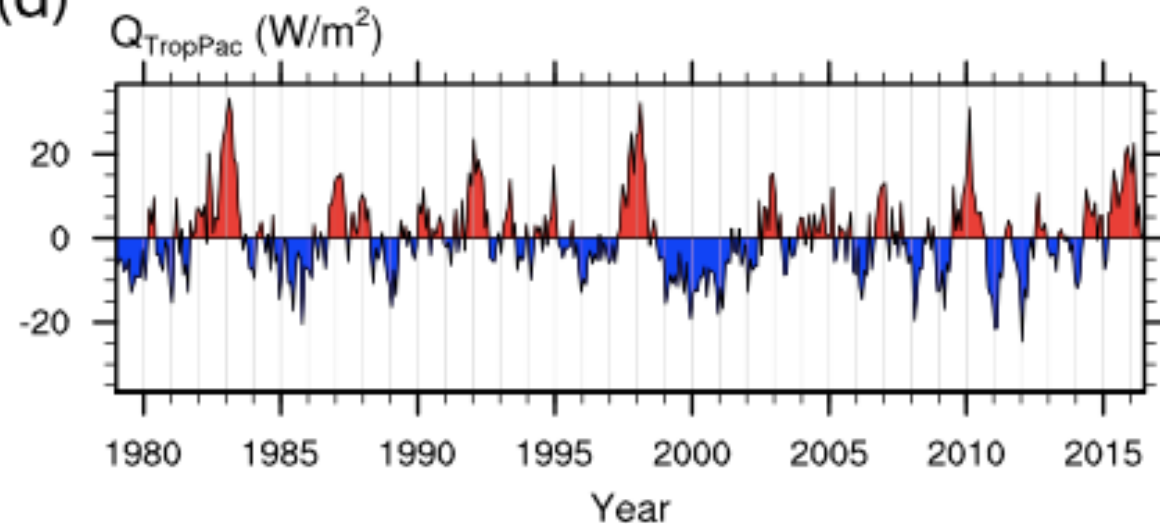
(b)



(c) Energy flux into atmos. (W/m^2)

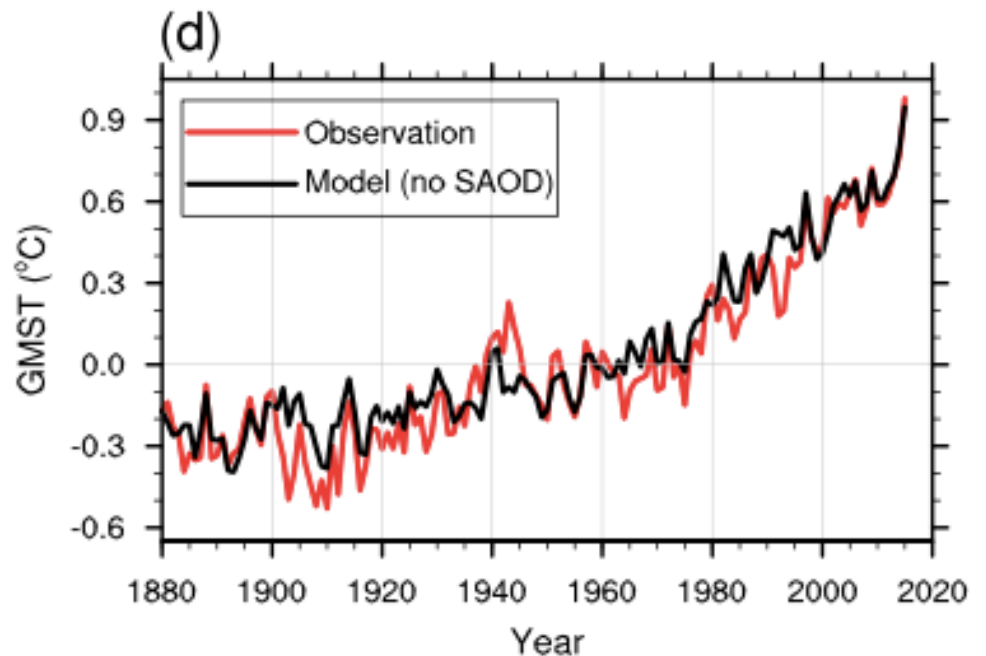
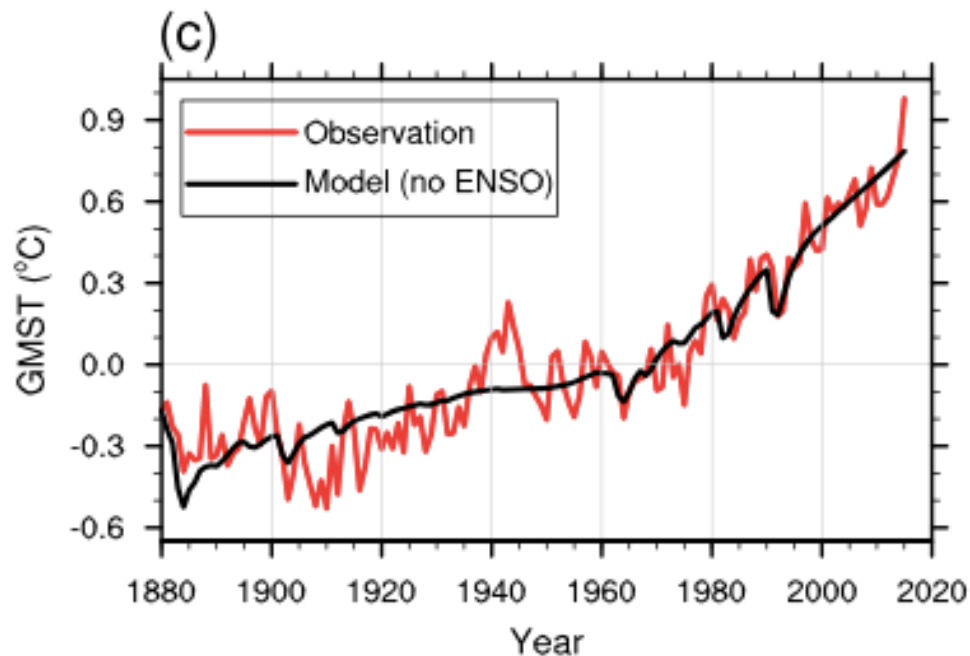
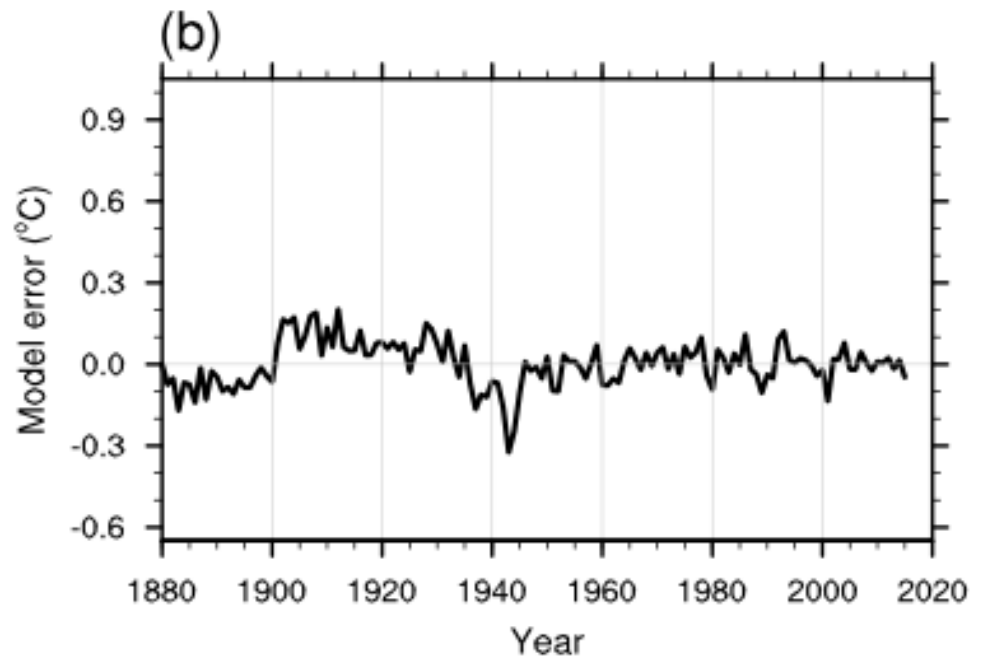
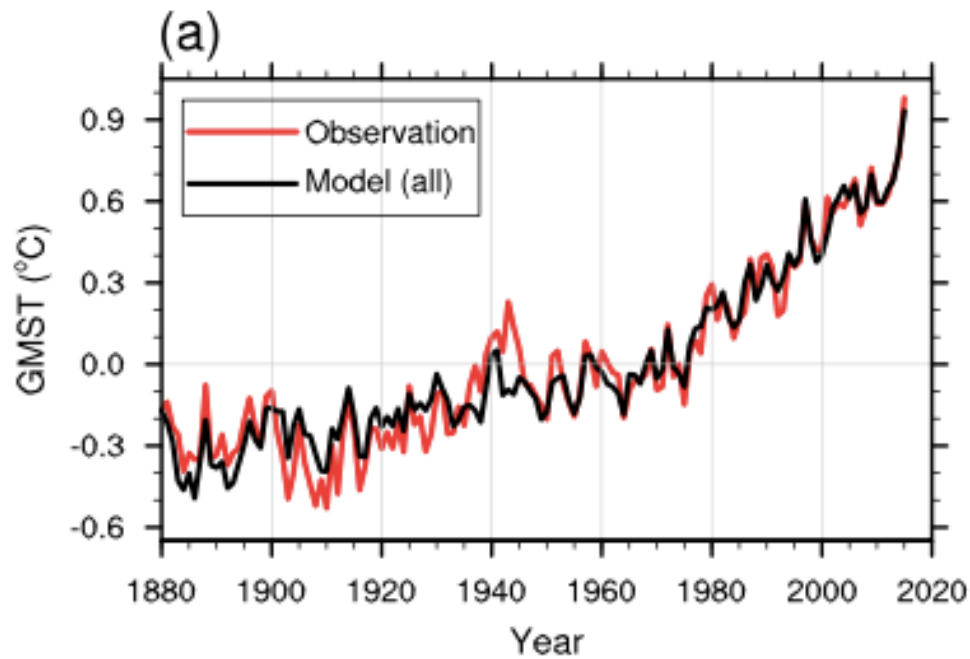


(d)

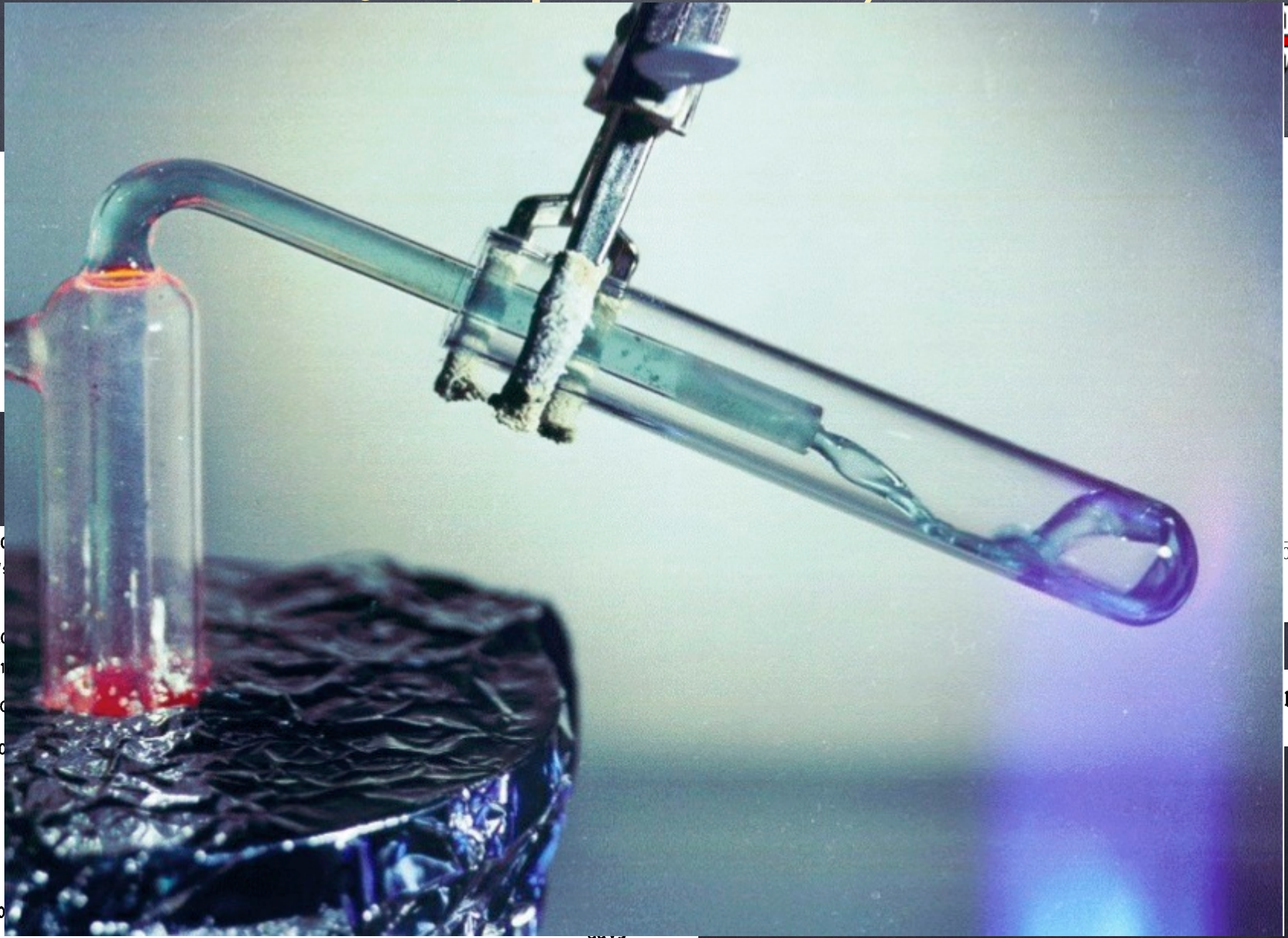


$$\frac{dT_g}{dt} = -\frac{T_g}{\tau} + a \cdot \log(\text{CO}_2/\text{CO}_{2,\text{ref}}) + b \cdot T_{\text{NiNO}} + c \cdot \text{SAOD} + d,$$

Effect of Climate Modes, e.g., Hu & Fedorov (2017)



Modeling of variability



0.0
ly/s
0.0
1
°C
0
-0

5
1

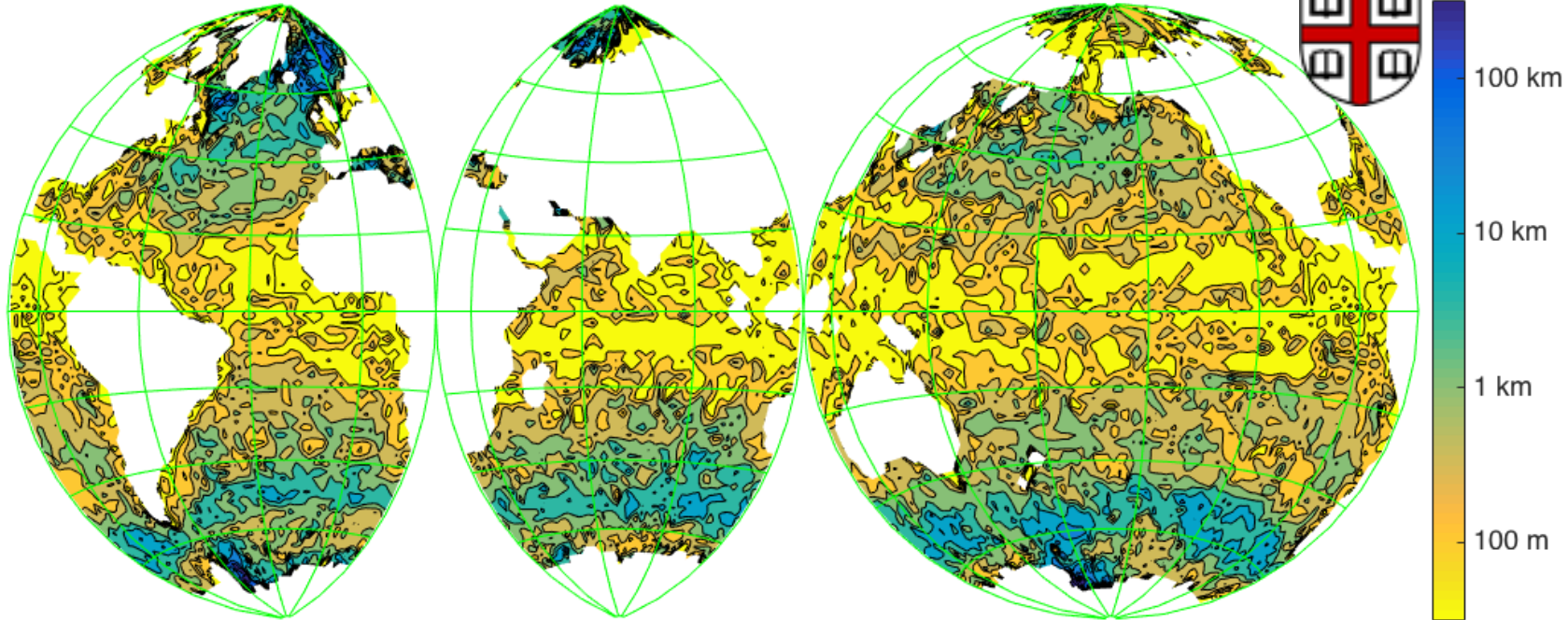
days

Still, these are systems in thermodynamic equilibrium

- These toy models are interesting and useful, but they have only one temperature.
- The real system is inherently unable to achieve a (thermodynamic) equilibrium state.
- However, we do normally assume that “infinitesimal parcels” of air or water can be described with a single temperature, entropy, etc., and thus yield to standard thermodynamics.



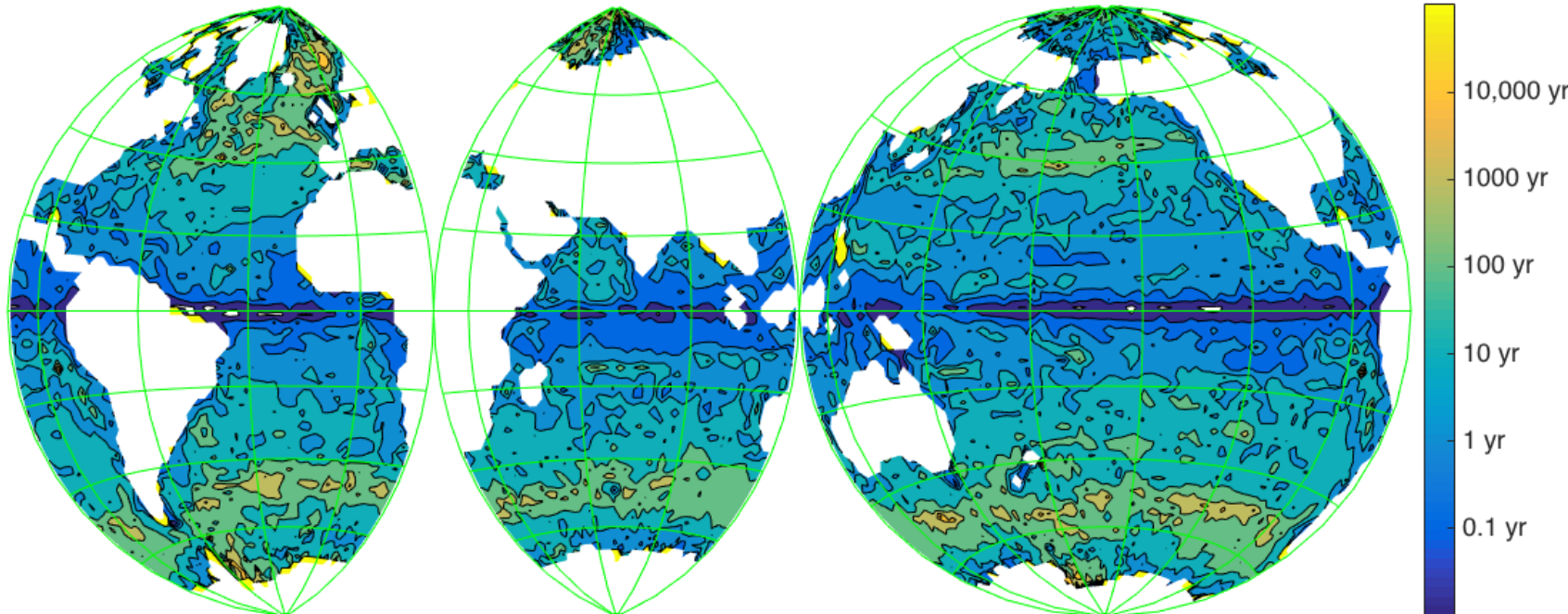
Equivalent Depths of Watermasses by Source (Gebbie & Huybers, 2011)



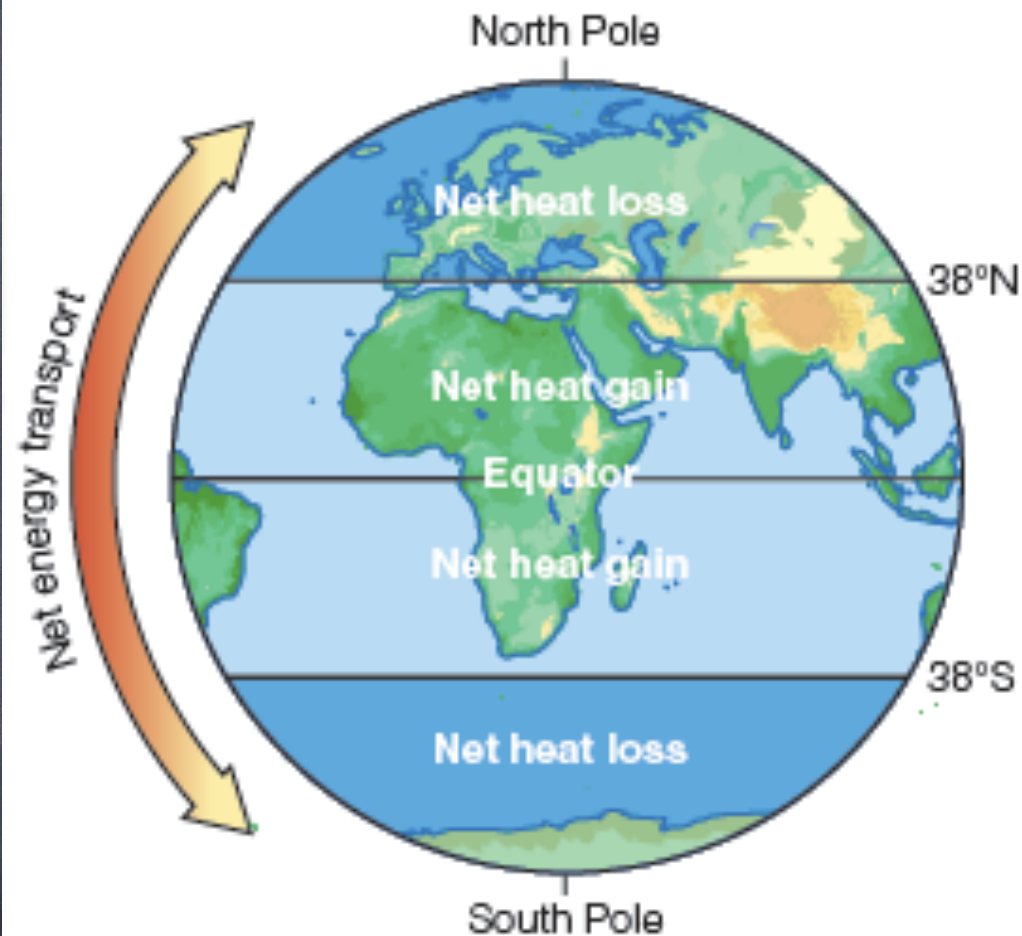
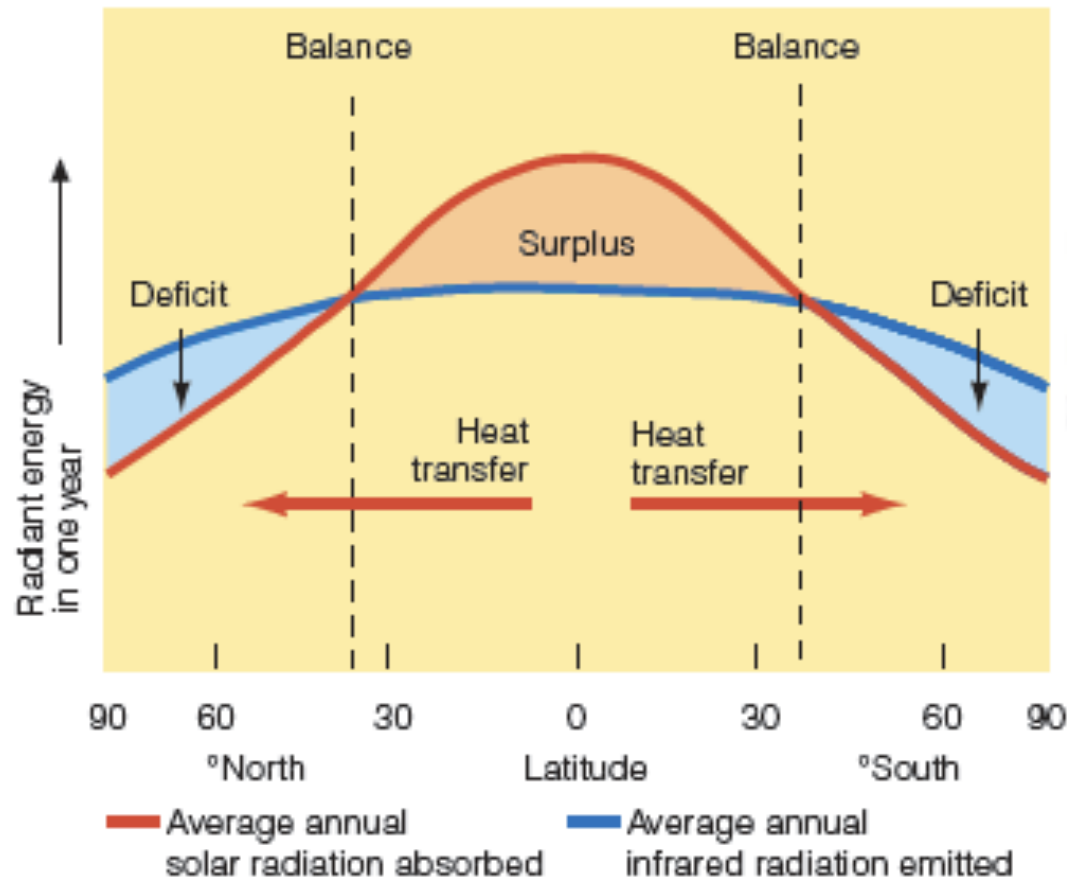
Consider lots of 1D Oceans: one per watermass

Wind (Ekman) flushing gives upper limit to λ^{-1} timescale

Ekman Flushing Timescale (ECCOv4 + Gebbie & Huybers, 2011)



But what if heating is uneven (but steady state)?

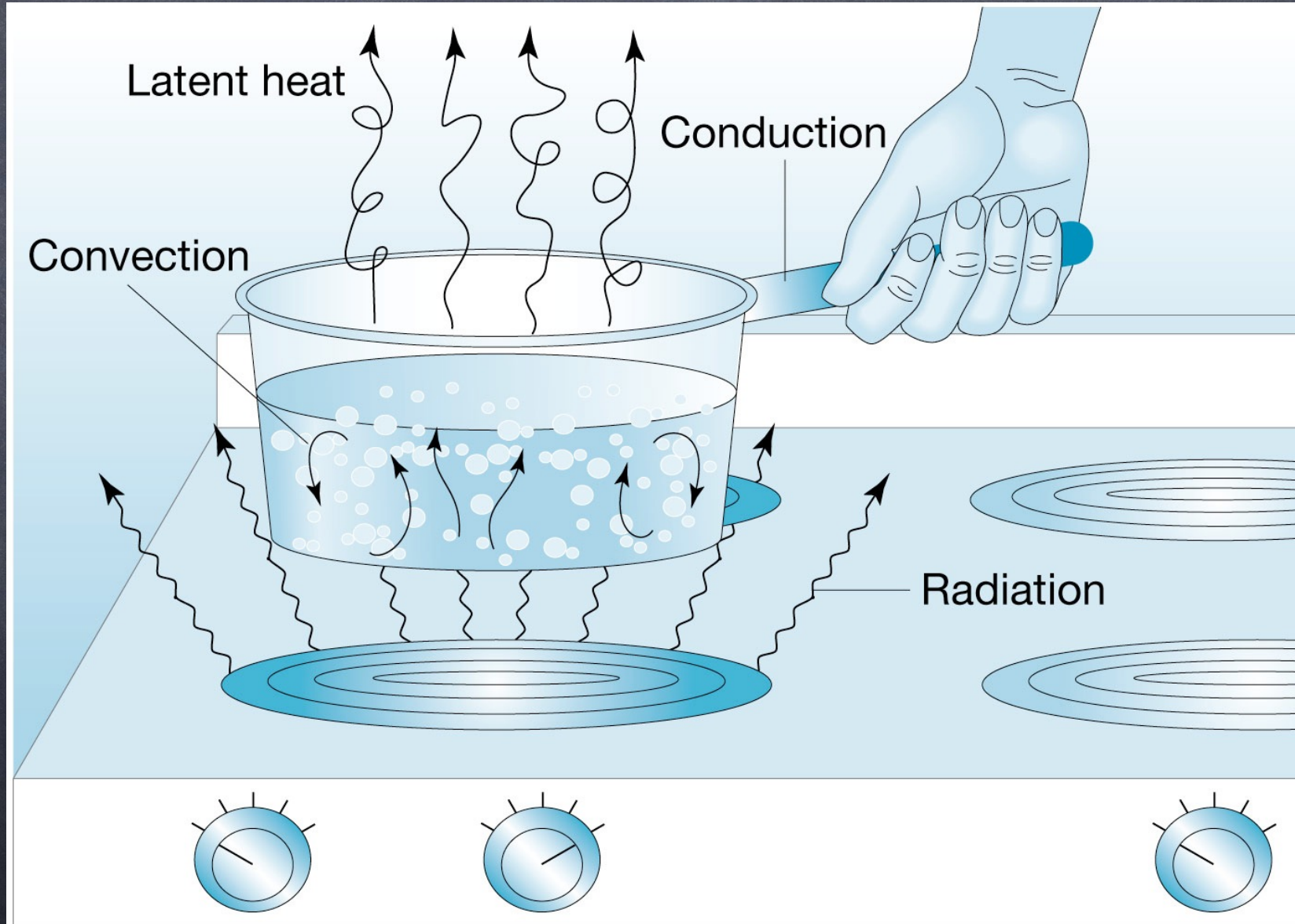


Incomplete Redistribution!—A Nonequilibrium Steady-State

How does Energy Flow?:

Energy may flow by Conduction, Radiation, and Convection of Sensible and Latent Heat (vapor & ice transport).

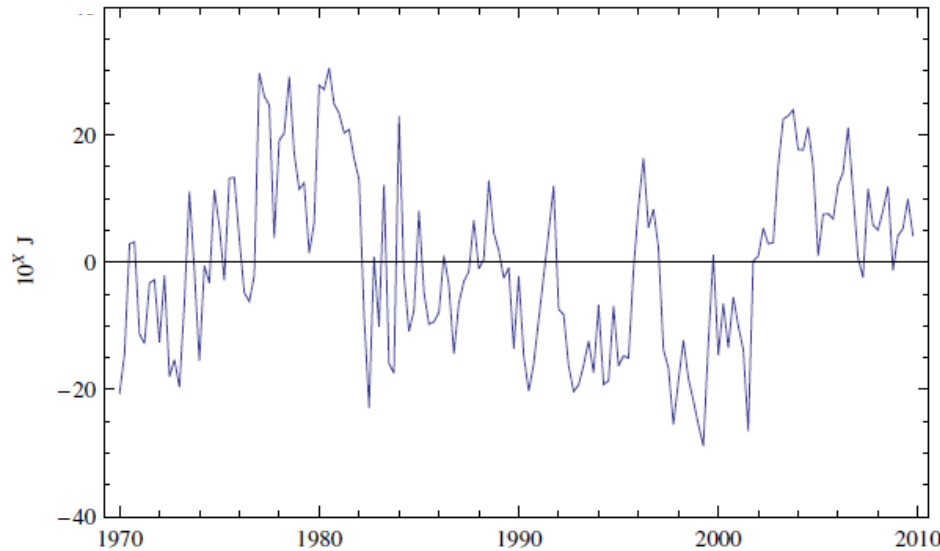
- Convection:** transfer of energy by fluid motion when heated from below
- Conduction:** transfer of energy by direct contact between molecules (not fluid motion)
- Radiation:** transfer of energy by electromagnetic waves, or by transfer through other force fields



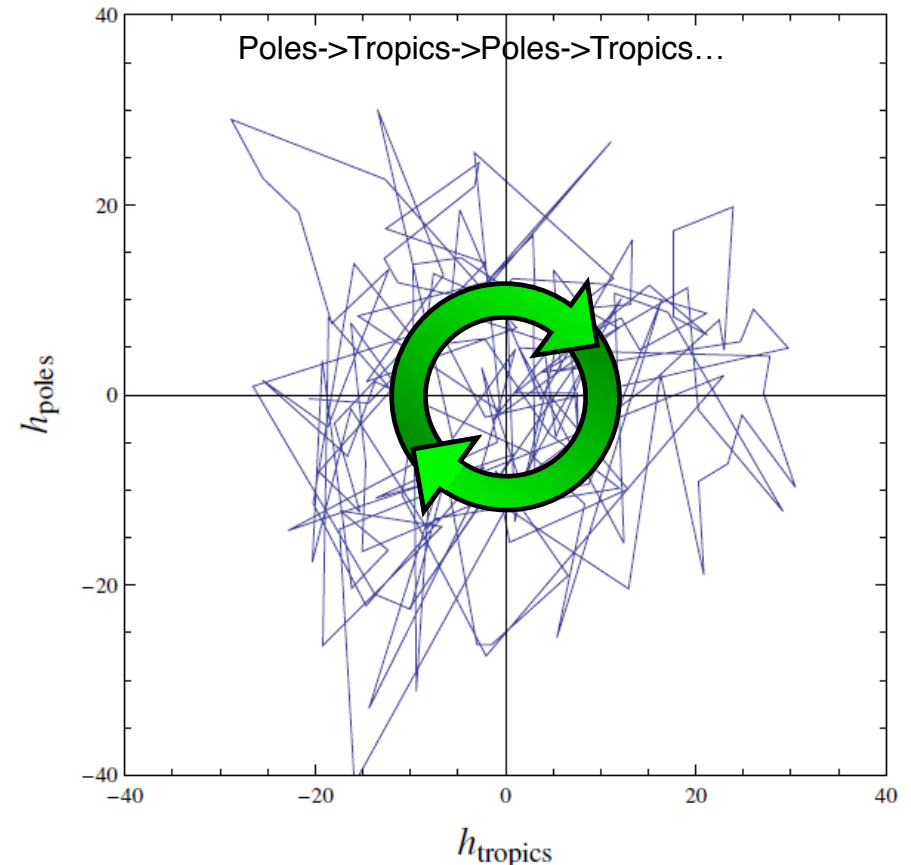
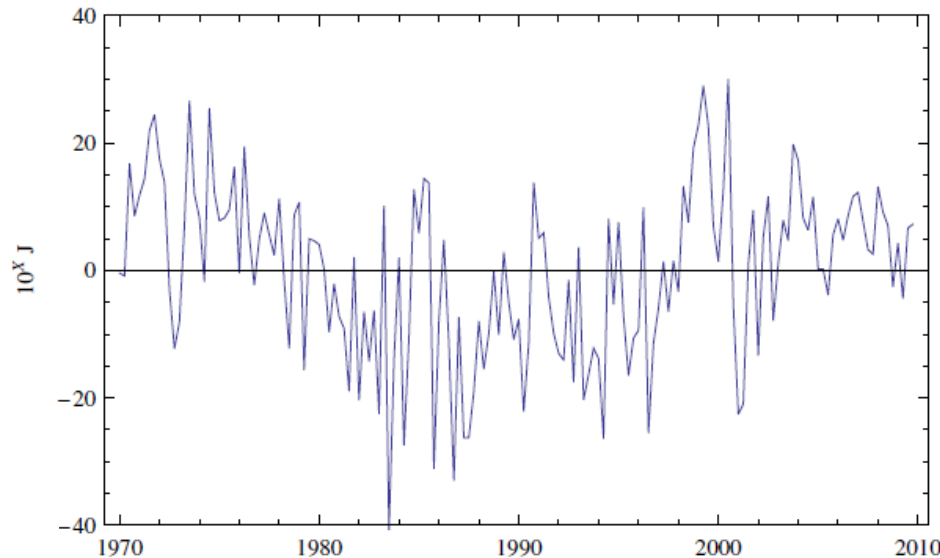
If Connections Occur Between Regions— Probability Currents Can Arise.



Tropical Ocean Heat Content h_{tropics}



Polar Ocean Heat Content h_{poles}



This is the root of
most stochastic model
predictability beyond persistence

R. Zia, J. B. Weiss, D. Mandal, and BFK, 2016: Manifest and subtle cyclic behavior in nonequilibrium steady states. In Journal of Physics: Conference Series, volume 750, page 012003. IOP Publishing.

KOLMOGOROV

Mechanical Energy Budget
and

Nonequilibrium Mechanisms

Atmospheric Redistribution/Heat Engine might be like this:

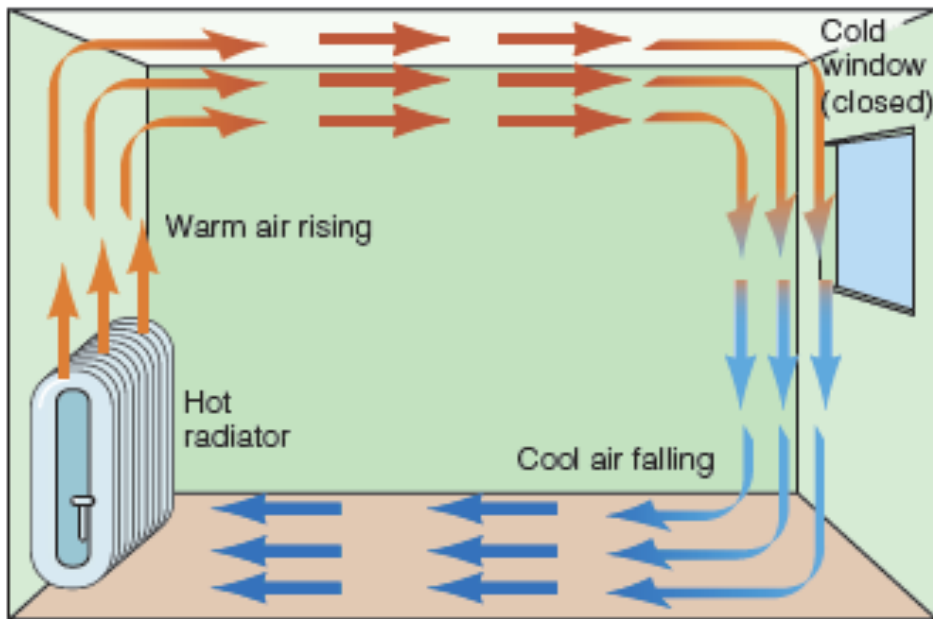


Figure 8.7 A convection current forms in a room when air flows from a hot radiator to a cold closed window and back. (For a practical oceanic application of this principle, look ahead to Figure 8.17.)

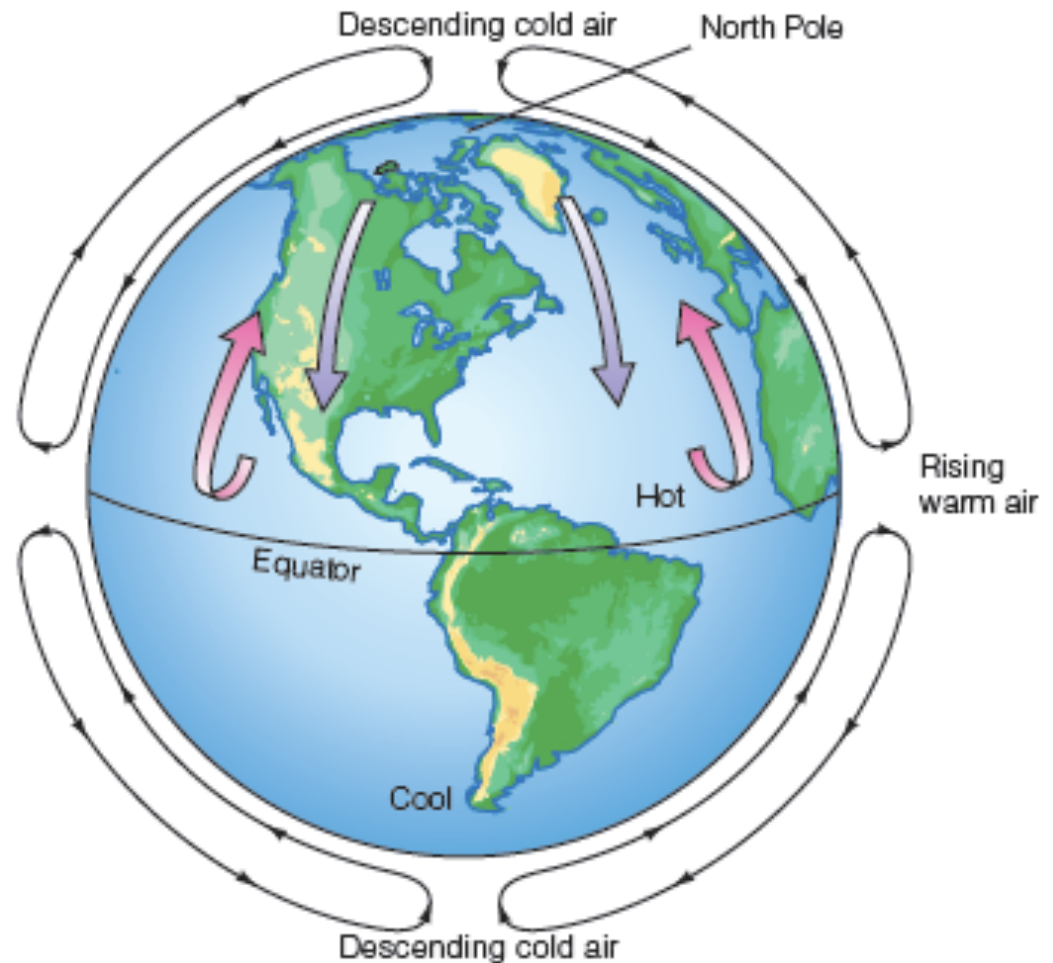
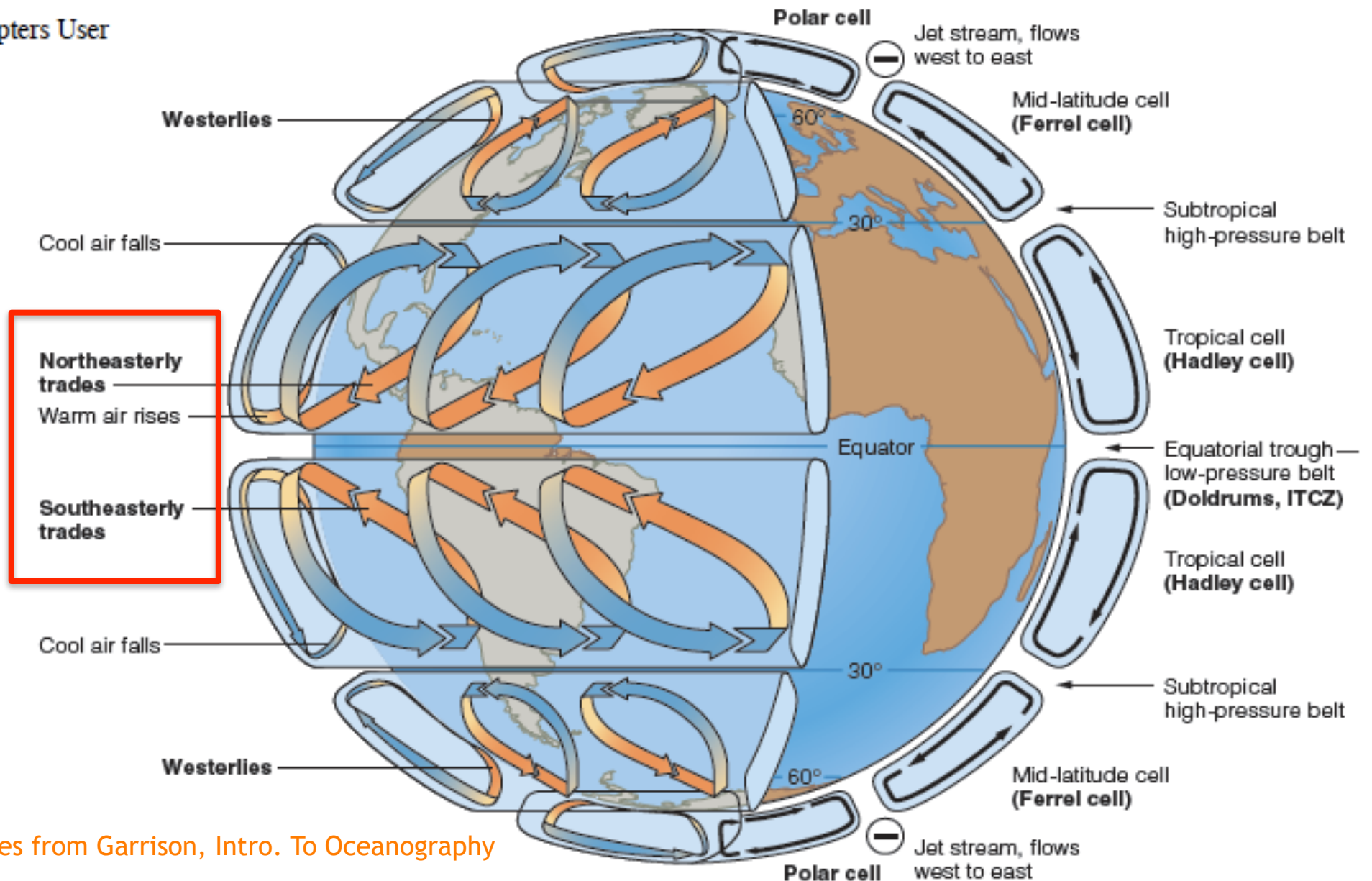


Figure 8.8 A hypothetical model of Earth's air circulation if uneven solar heating were the only factor to be considered. (The thickness of the atmosphere is greatly exaggerated.)

Halley's Idea, essentially
Except, the planet is
rotating! (Hadley's idea)

With the Coriolis Force, the winds are more zonal... and considerably less efficient.

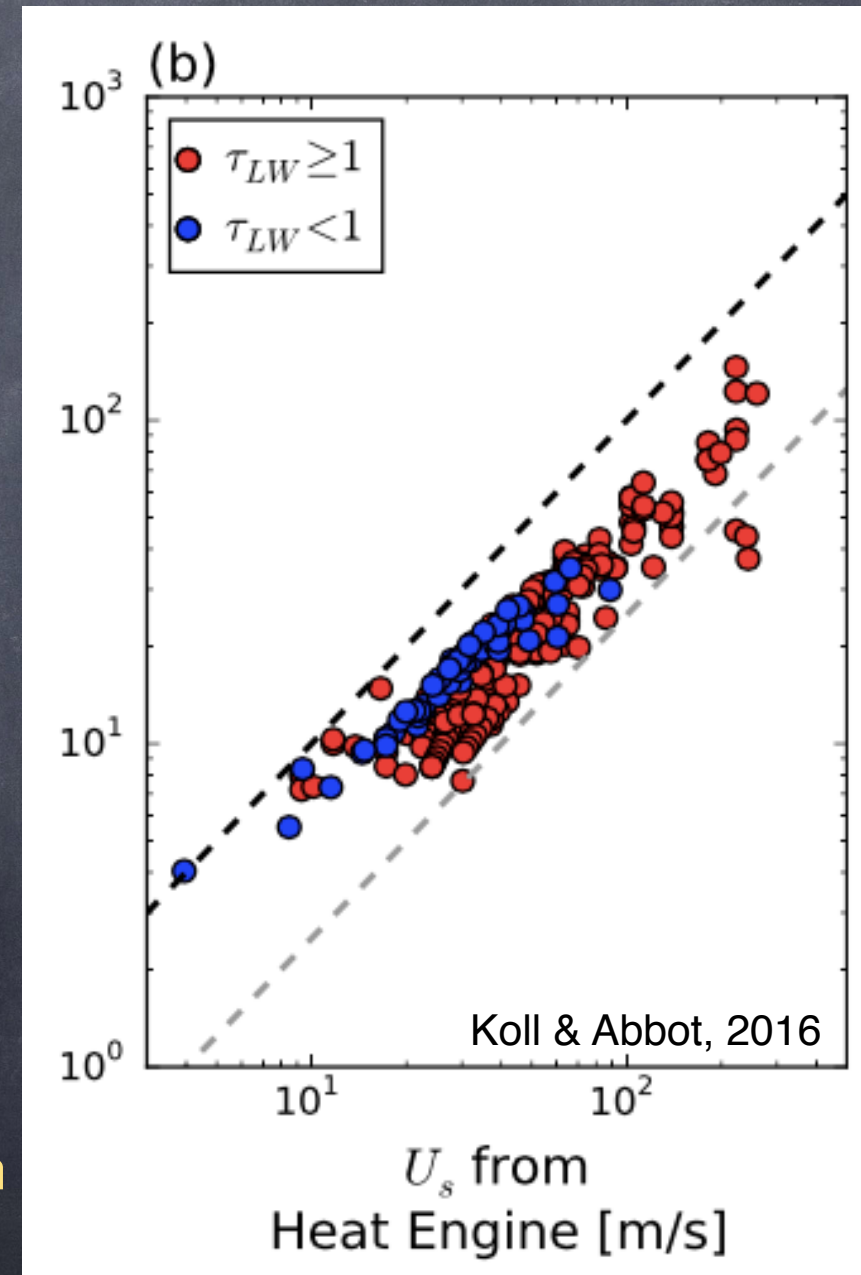
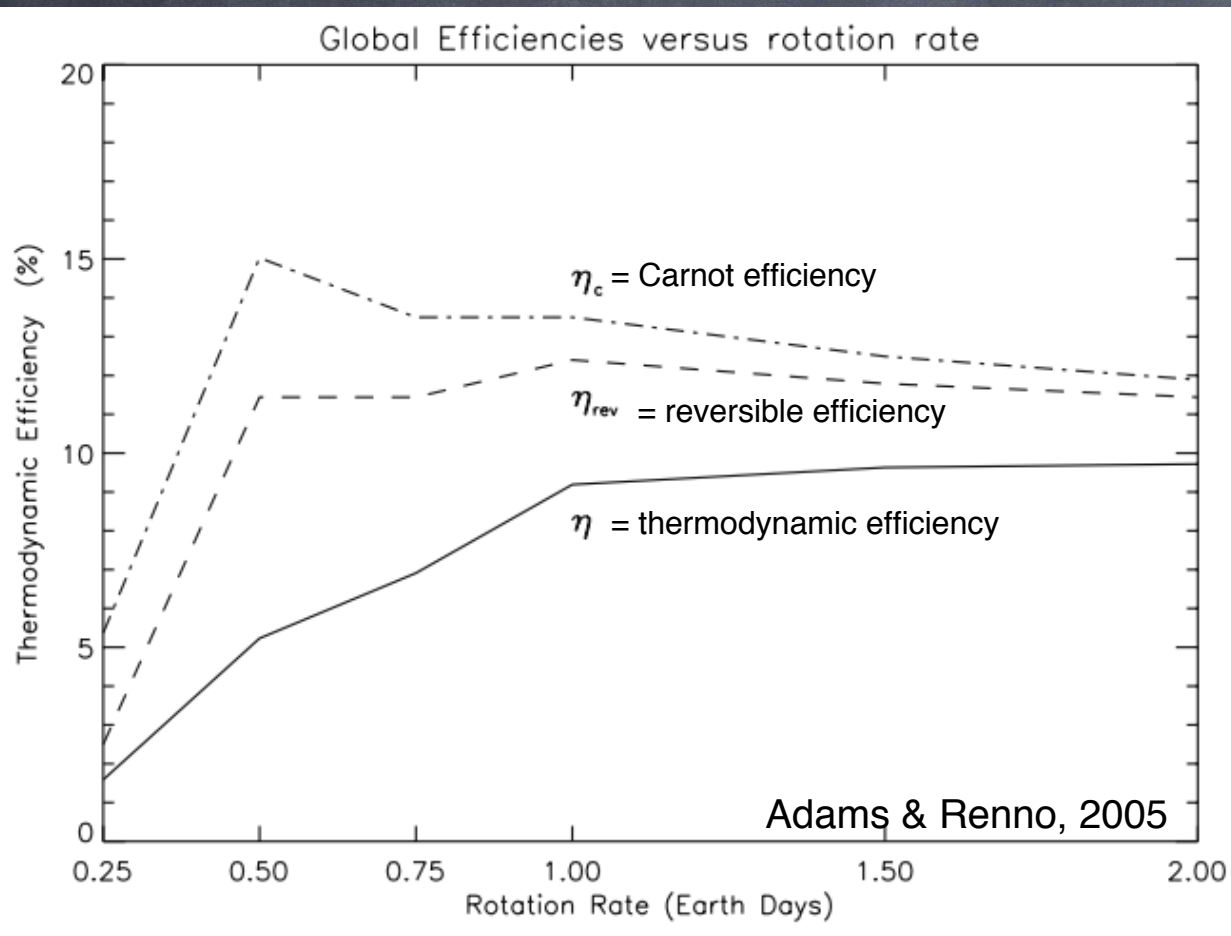
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Images from Garrison, Intro. To Oceanography

How is Mechanical Energy created?

Carnot Cycle with 342 W/m^2 ? No, but simplified (dry, no continents) atmospheres are proportionally so.



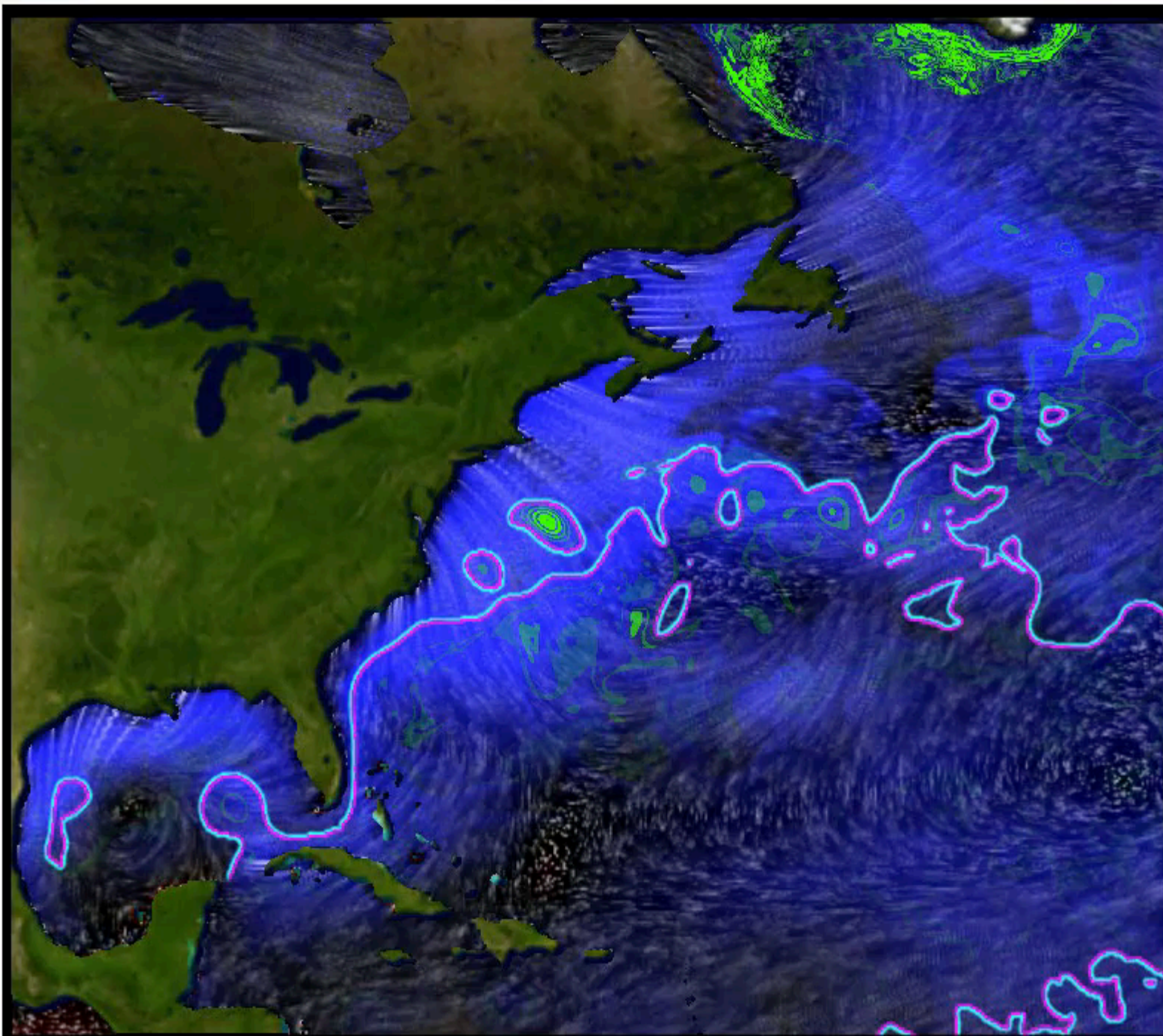
To a lesser degree, there is also energy from tides and radioactive decay, and residual energy from planetary accretion



Weather,
Atmosphere
Fast

Ocean,
Climate
Slow

3.4m of
ocean water
has same
heat capacity
as the
WHOLE
atmosphere



tau / qflux / theta200m / kppMLD

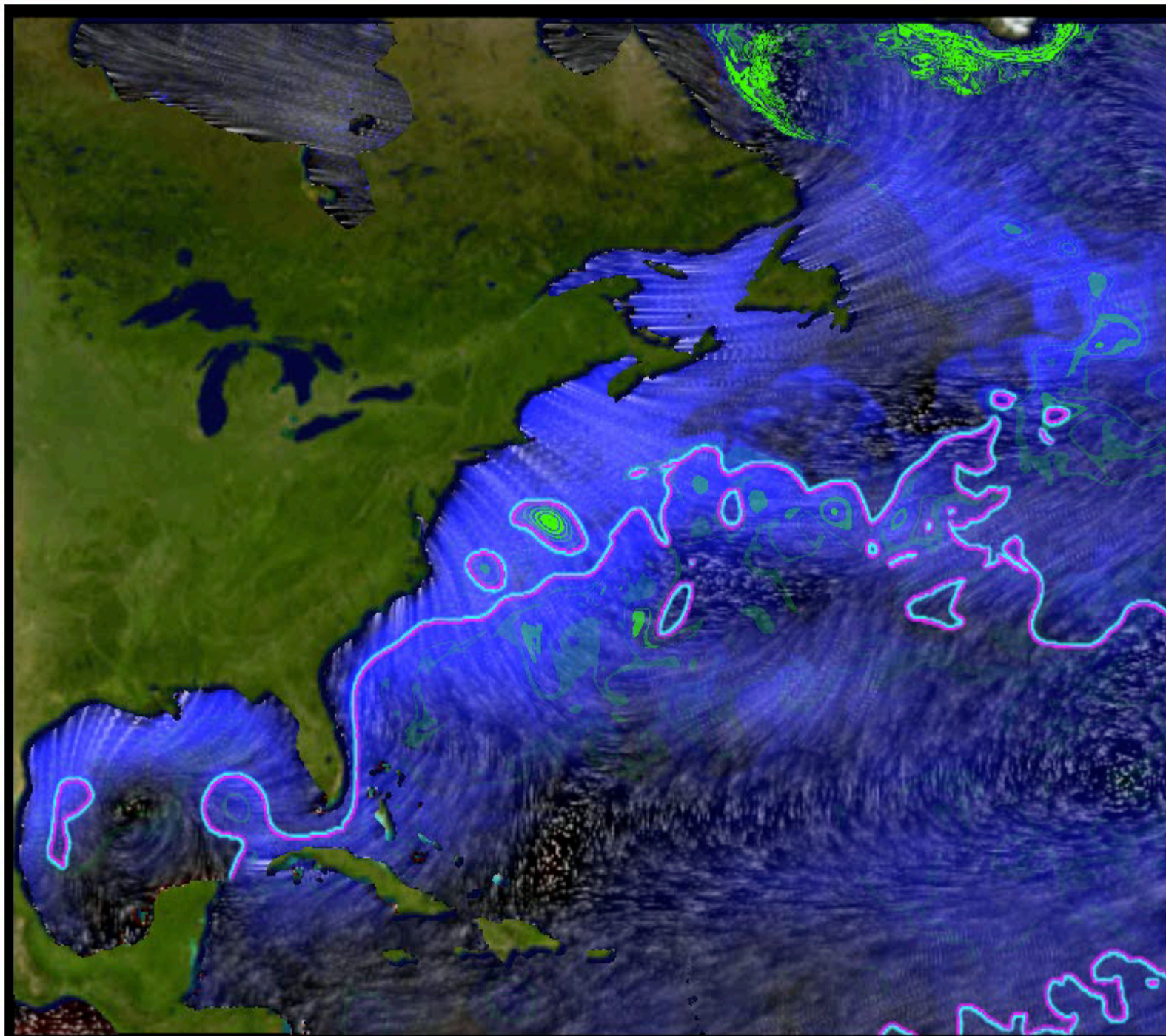
Jan 1 00:30 2001



Weather,
Atmosphere
Fast

Ocean, Climate
Slow

3.4m of ocean
water has
same heat
capacity as the
WHOLE
atmosphere



ECCO Movie: Chris Henze, NASA Ames

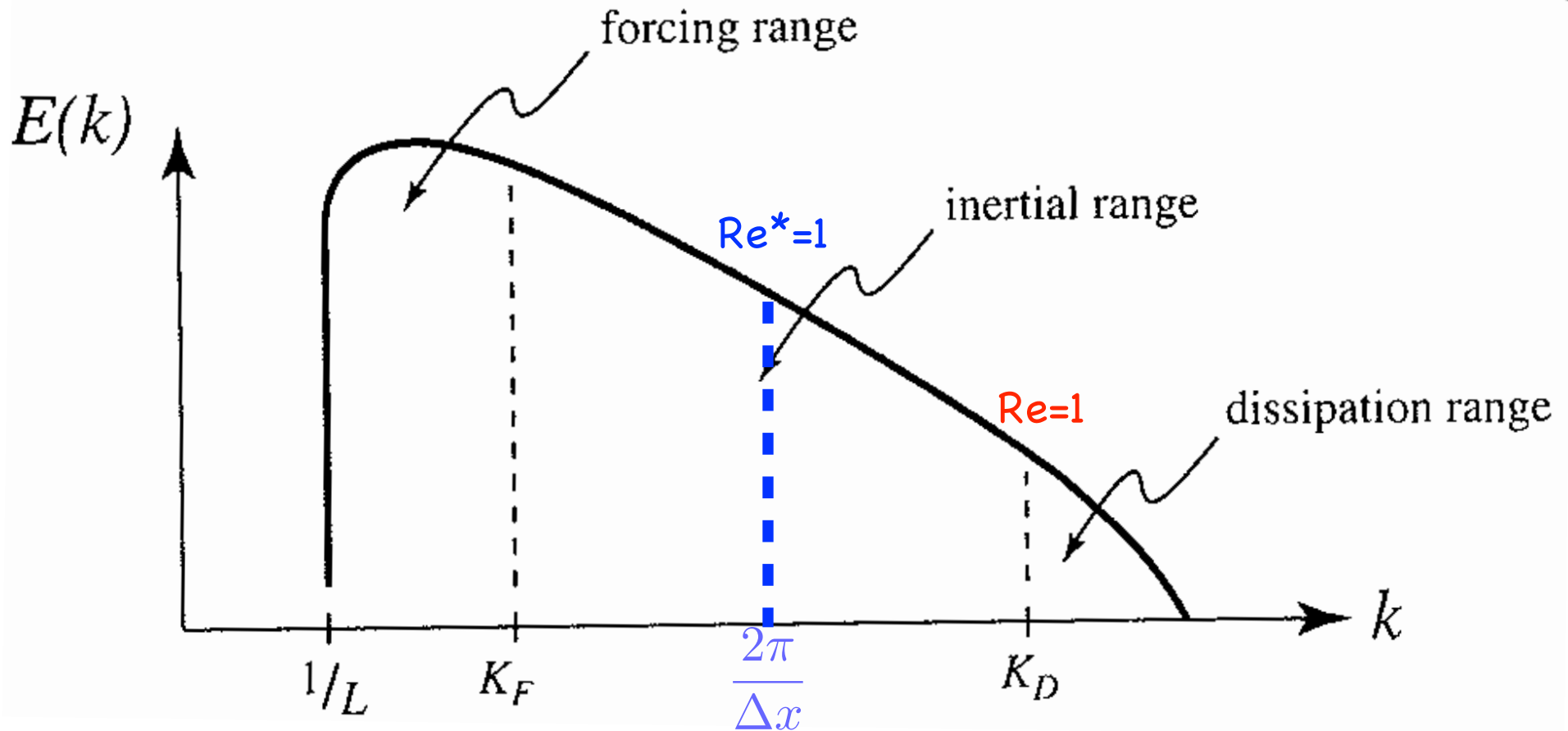
tau / qflux / theta200m / kppMLD

Jan 1 00:30 2001

So, if both ocean & atmosphere are turbulent...

- The classic statistical physics prob. is fully-developed, homogenous, isotropic turbulence.
- Richardson, Kolmogorov, Oboukhov, Monin, Yaglom, Kraichnan, Charney, Mandelbrot, Frisch, etc.
- The key idealization involves flows that are much larger than the damping scale and much smaller than the forcing scale—an inertial range.
- The challenge in applying this approach in the earth system is that new parameters (f , N) introduce other significant scales along the way.

Truncation of Cascades in models



1963: Smagorinsky Devises Viscosity Scaling,
Energy Flow is Preserved,

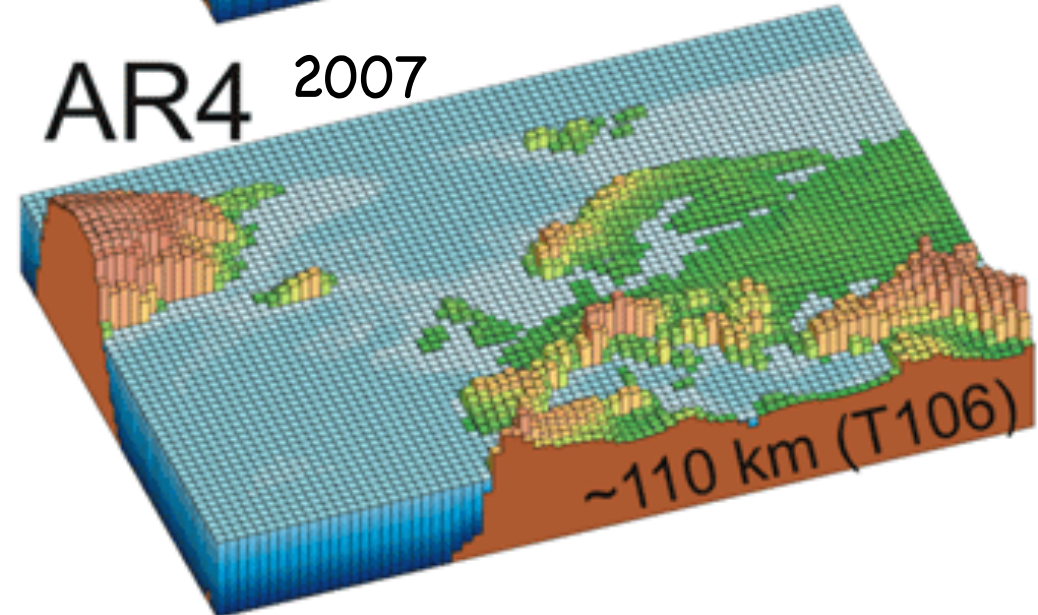
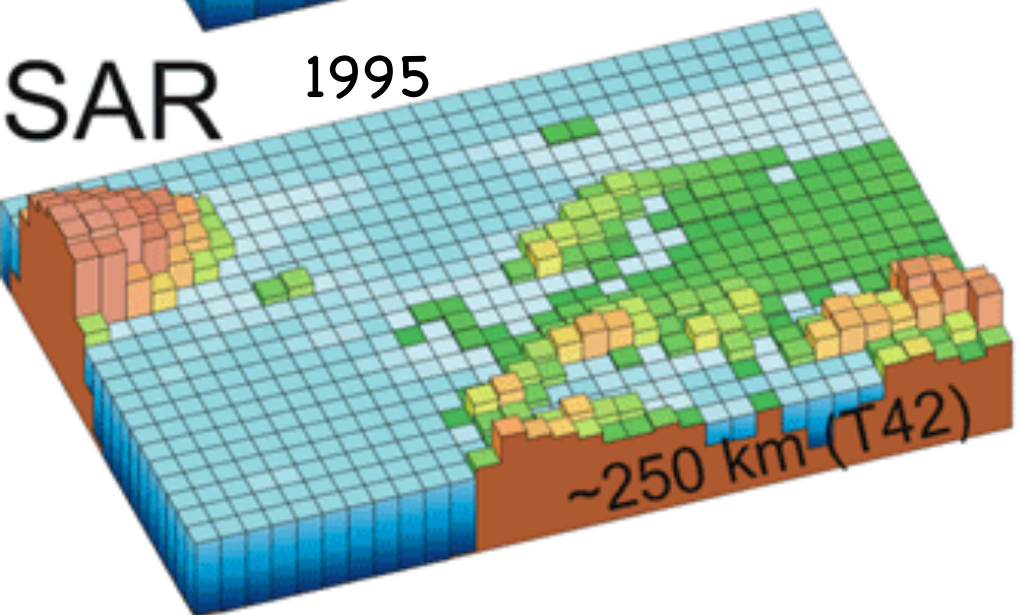
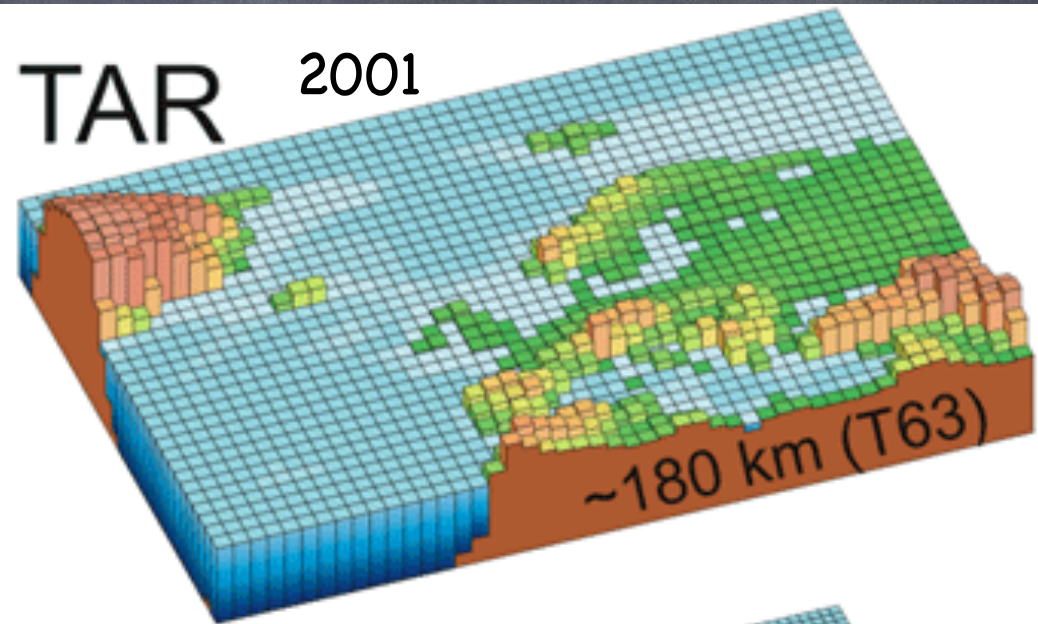
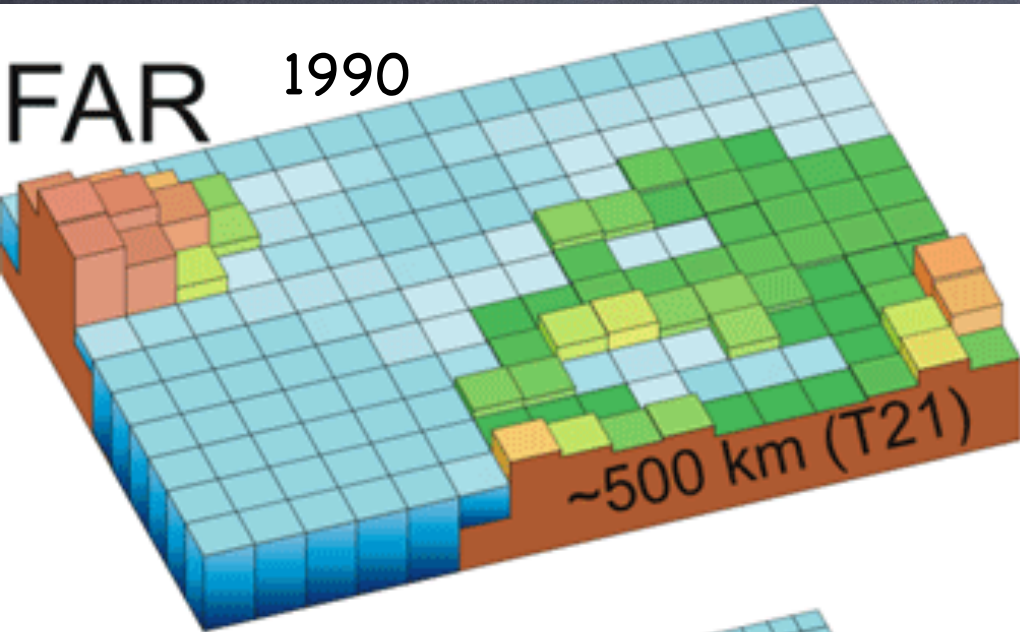
but order-1 gridscale Reynolds #: $Re^* = UL/\nu_*$

$$\nu_{*h} = \left(\frac{\Upsilon_h \Delta x}{\pi} \right)^2 \sqrt{\left(\frac{\partial u_*}{\partial x} - \frac{\partial v_*}{\partial y} \right)^2 + \left(\frac{\partial u_*}{\partial y} + \frac{\partial v_*}{\partial x} \right)^2}$$

Gridscale-
dependent

Climate model resolution introduces a scale...

Image: ipcc.ch



Can Atmospheric "turbulent mixing" do the meridional transport?

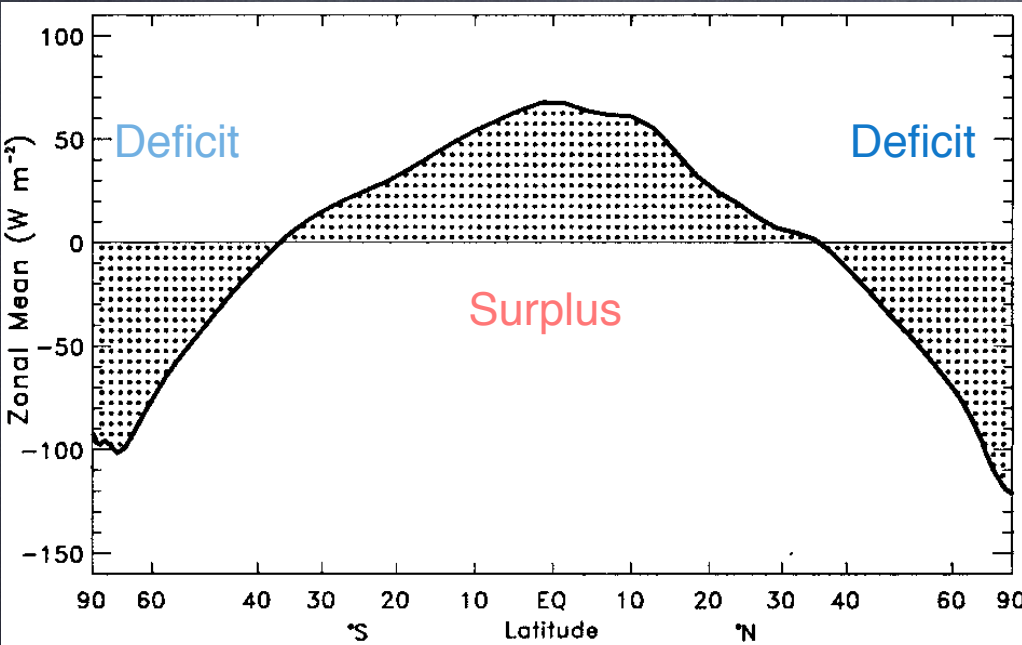


FIG. 1. TOA annualized ERBE zonal mean net radiation ($W m^{-2}$) for Feb 1985–Apr 1989.

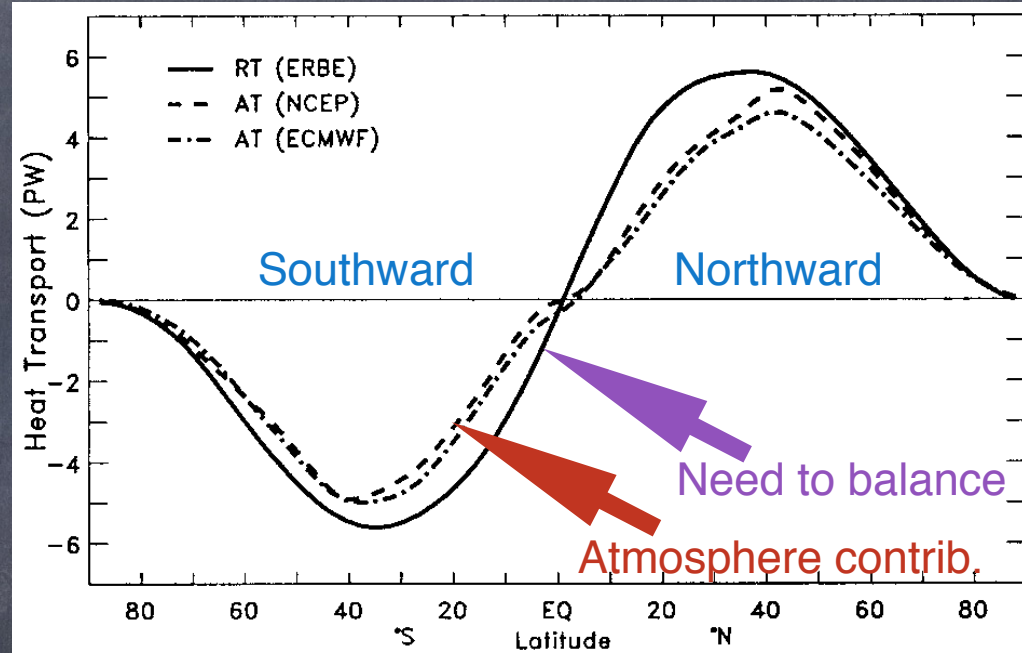


FIG. 2. The required total heat transport from the TOA radiation RT is given along with the estimates of the total atmospheric transport AT from NCEP and ECMWF reanalyses (PW).

What's
Left is
Ocean
Transport

Not just
mixing:
different
basins
differ in
direction
and
magnitude!

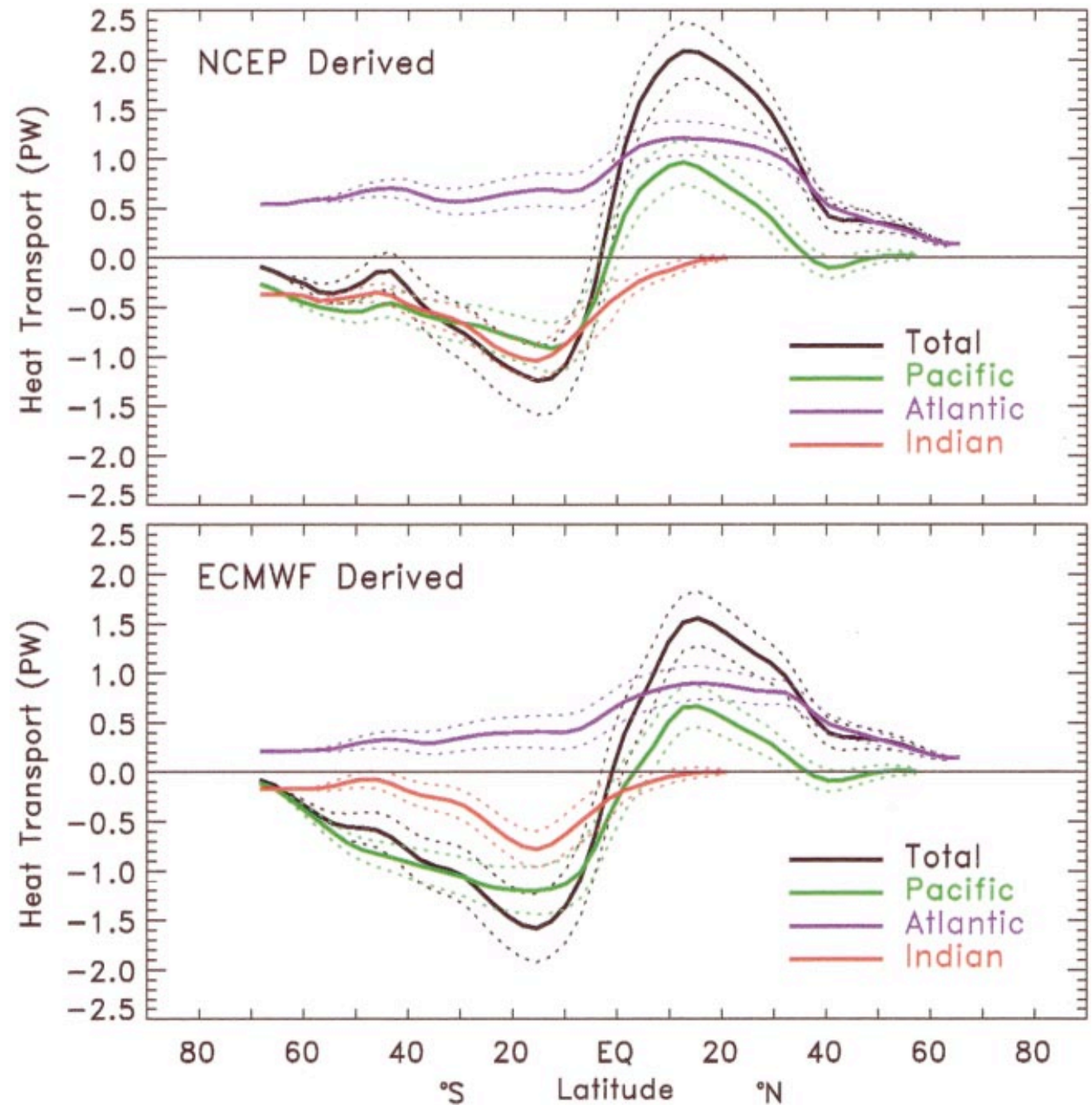


FIG. 5. Implied zonal annual mean ocean heat transports based upon the surface fluxes for Feb 1985–Apr 1989 for the total, Atlantic, Indian, and Pacific basins for NCEP and ECMWF atmospheric fields (PW). The 1 std err bars are indicated by the dashed curves.

Pot'l Temperature & Salinity of the Ocean

Thermocline-->

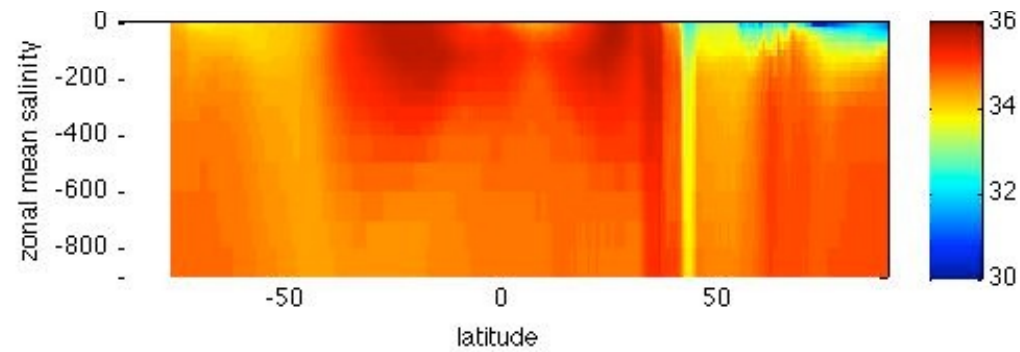
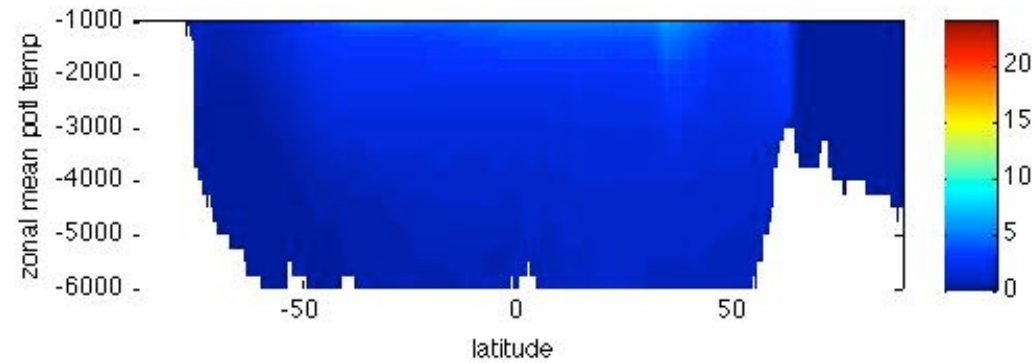
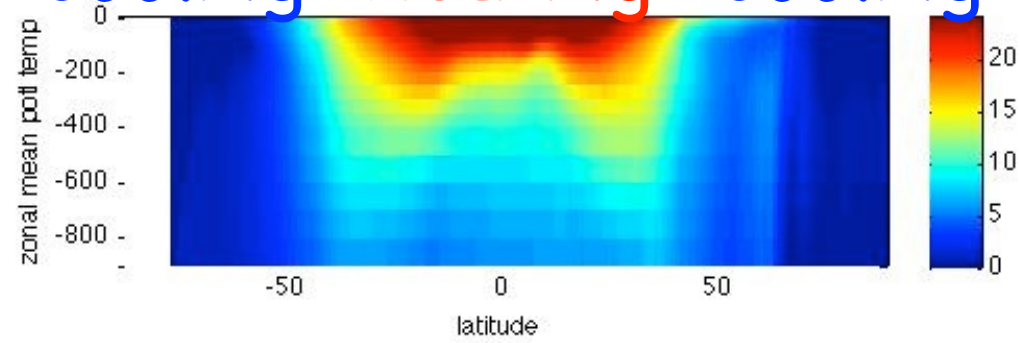
Seawater is fairly incompressible, pressure increases linearly w/ depth, and conversion from internal to mechanical is negligible

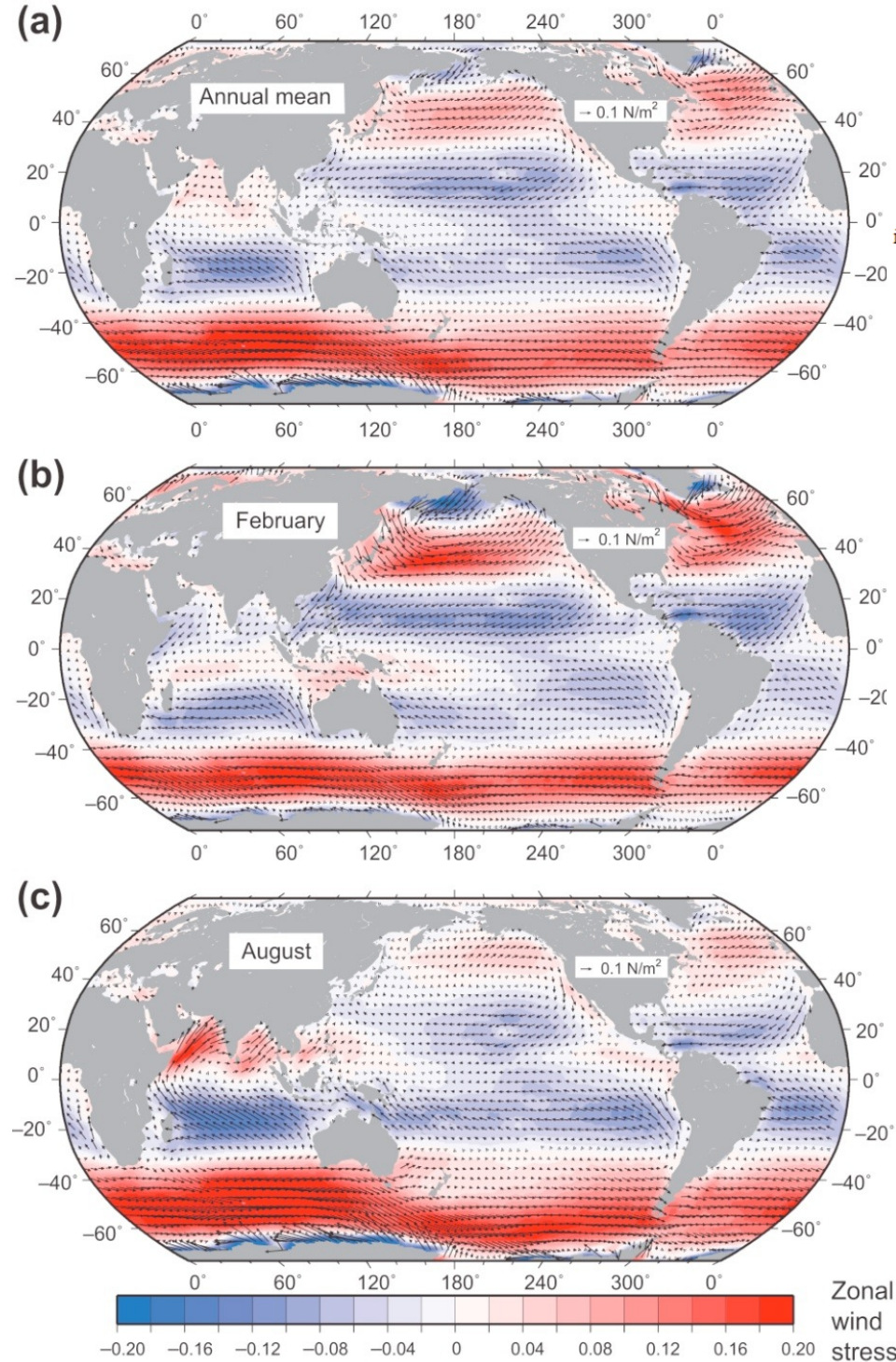
Halocline-->

Cooling & Heating at same pressure: Ocean is NOT a heat engine

Data from Gouretski & Kolterman 04

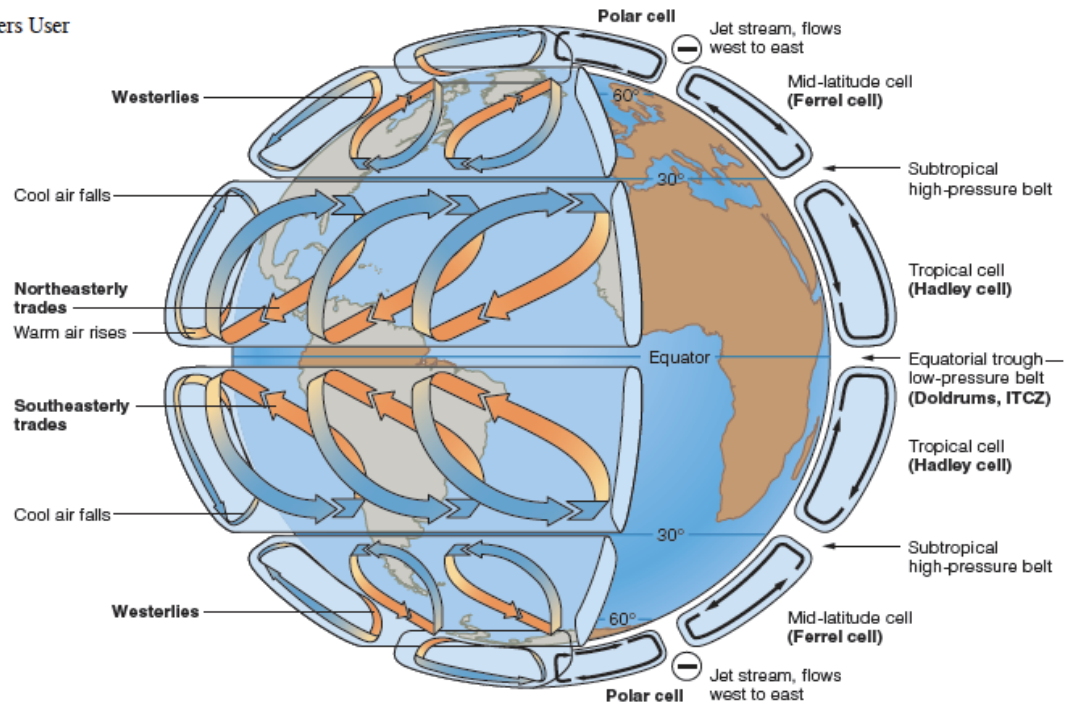
Cooling Heating Cooling





Mean wind stress (arrows) and zonal wind stress (color shading) (N/m^2): (a) annual mean, (b) February, and (c) August, from the NCEP reanalysis 1968–1996 (Kalnay et al., 1996).

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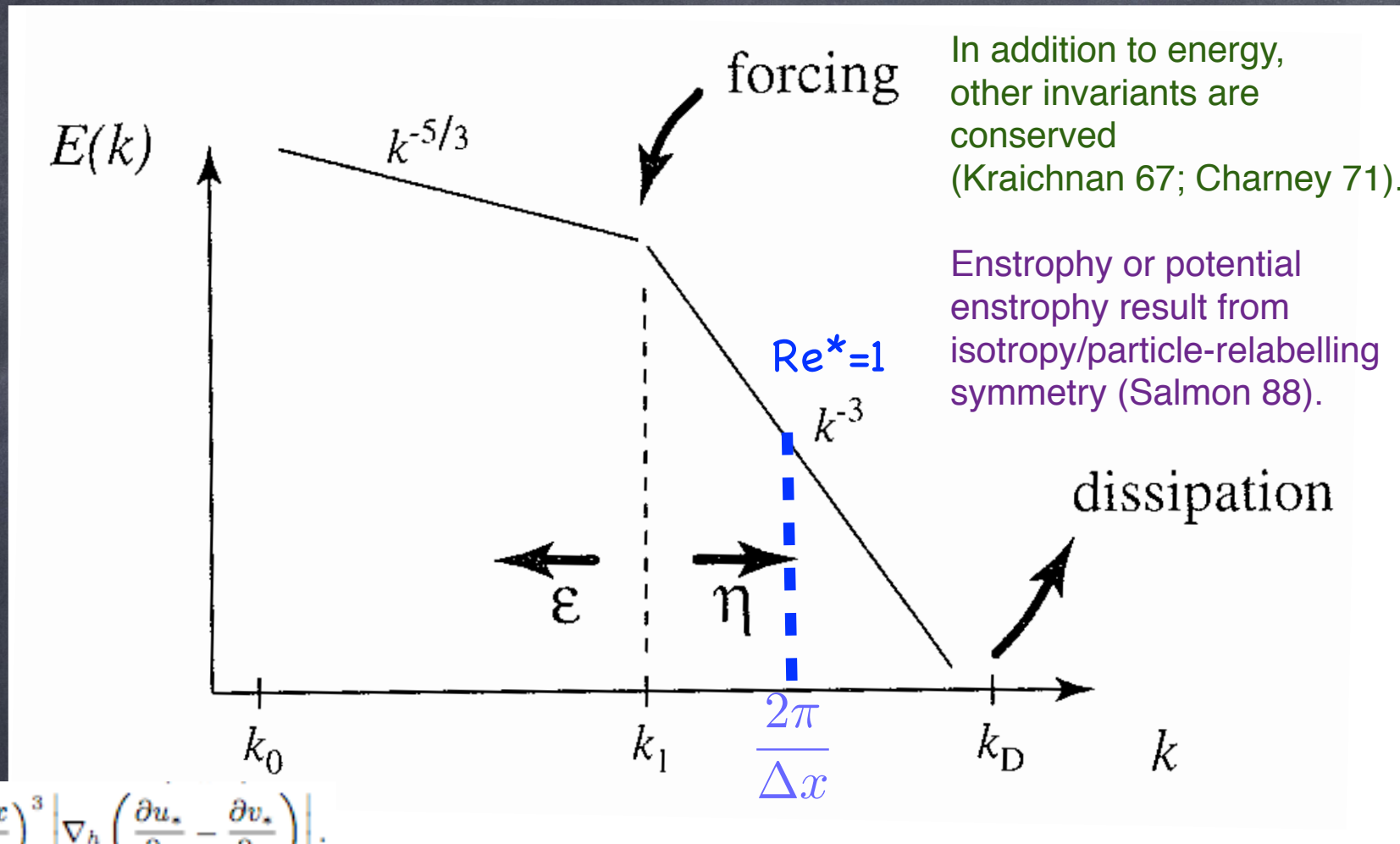
So, the ocean receives much of its mechanical energy from other more direct sources: winds and tides.

Another problem... Turbulence isn't 3d Turbulence at the 10-100km scale

- The ocean is wide (10,000km)
- But not deep (4km)
 - Motions in upper 1km
- The layer of blue paint on a globe has roughly the right aspect ratio!
- Atmosphere is a little taller (30km), but eddies are bigger (1000km)
- Motions are largely 2d



2d & QG Turbulence Differ



1996: Leith Devises Viscosity Scaling, 2D Enstrophy Flow is Preserved

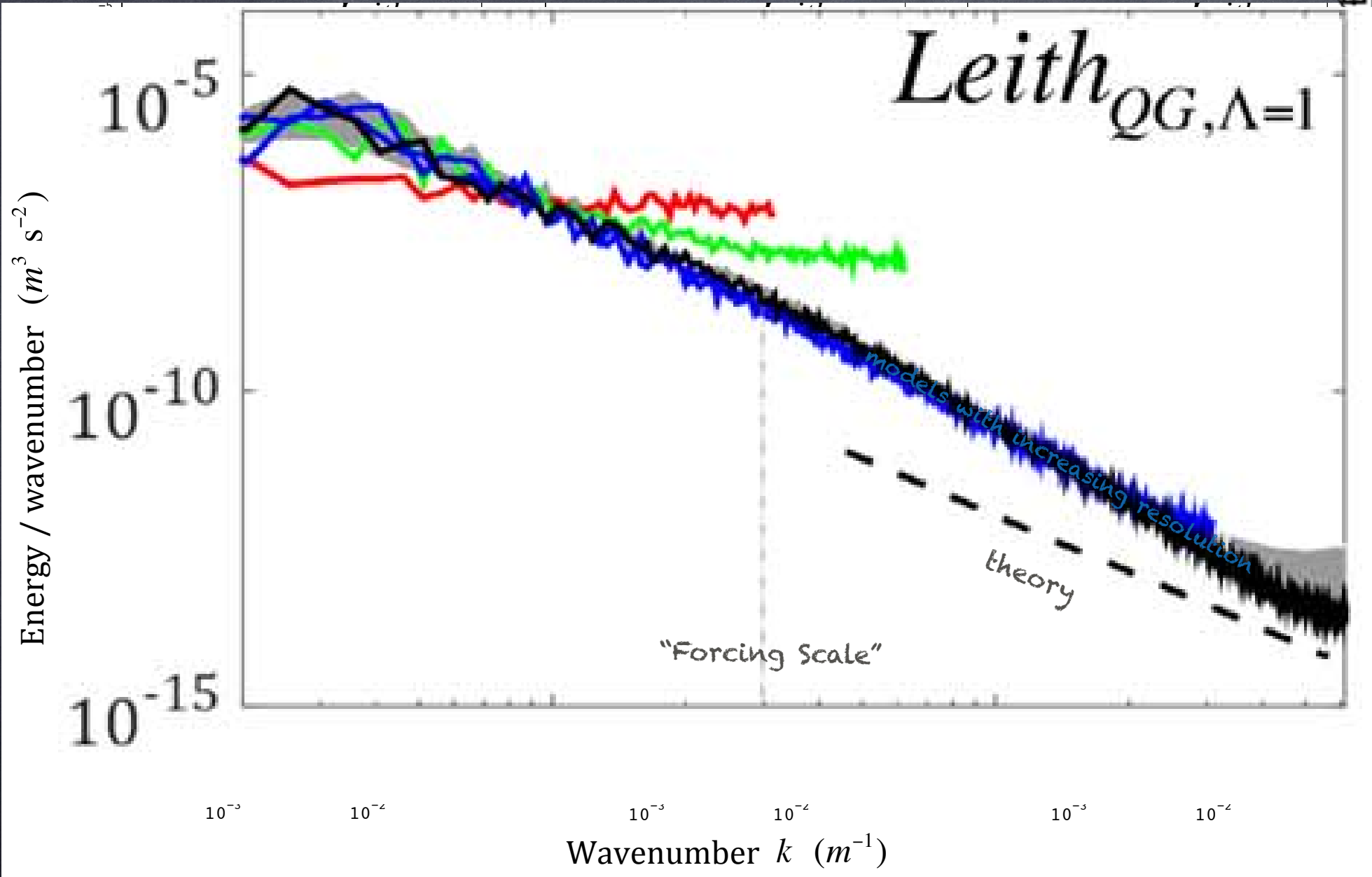
BFK and D. Menemenlis, 2008: Can large eddy simulation techniques improve mesoscale-rich ocean models? In M. Hecht and H. Hasumi, editors, *Ocean Modeling in an Eddy Regime*, volume 177, pages 319–338. AGU Geophysical Monograph Series.

S. D. Bachman, BFK, and B. Pearson, 2017: A scale-aware subgrid model for quasigeostrophic turbulence. *Journal of Geophysical Research—Oceans*, 122:1529–1554. URL <http://dx.doi.org/10.1002/2016JC012265>.

B. Pearson, BFK, S. D. Bachman, and F. O. Bryan, 2017: Evaluation of scale-aware subgrid mesoscale eddy models in a global eddy-rich model. *Ocean Modelling*, 115:42–58. URL <http://dx.doi.org/10.1016/j.ocemod.2017.05.007>.

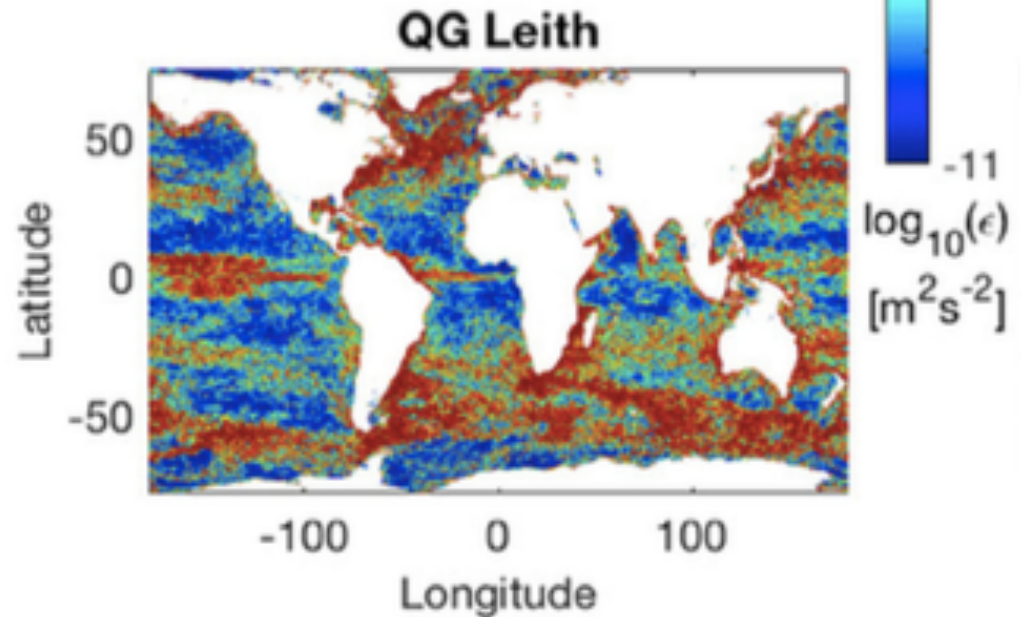
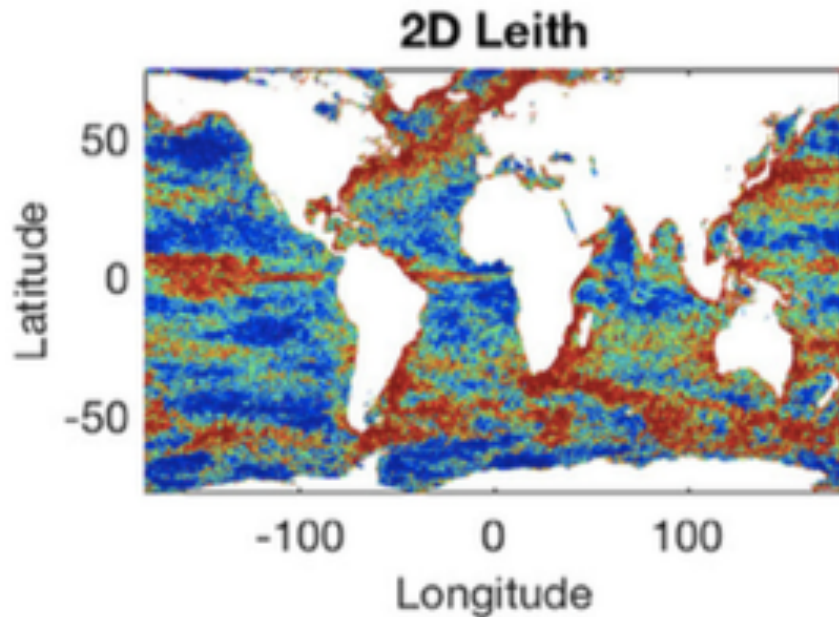
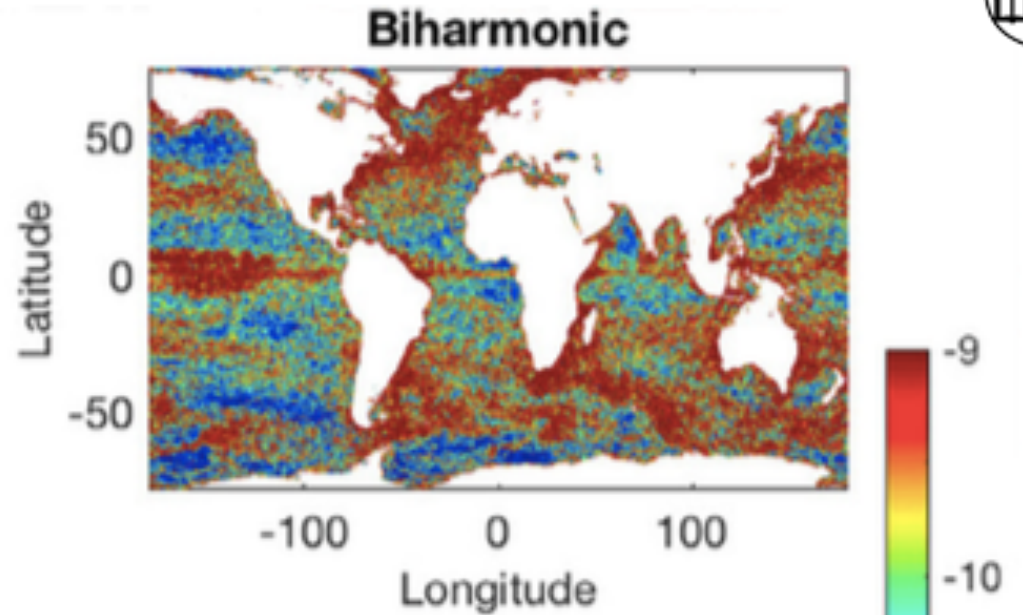
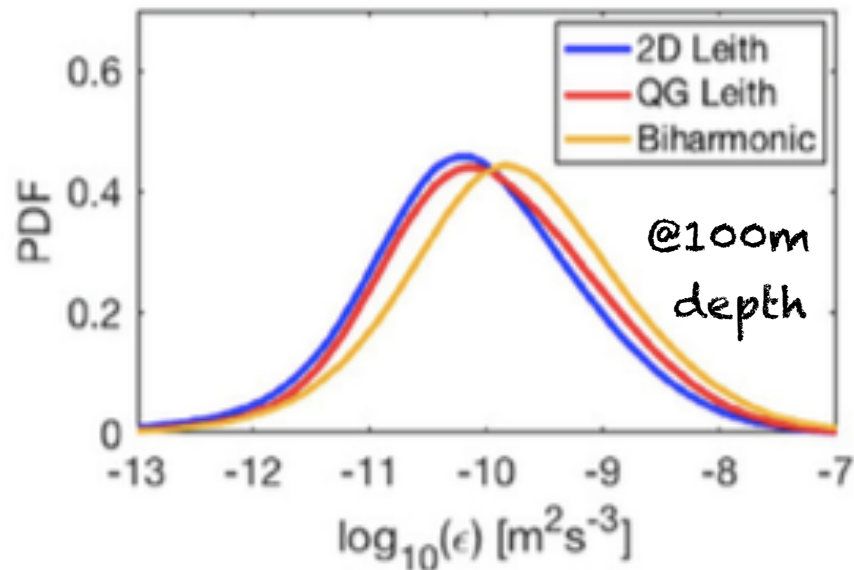
Where does ocean energy go?

Spectrally speaking



Where does ocean energy go?

Statistically & geographically speaking



Where does ocean energy go?

Phenomenologically speaking

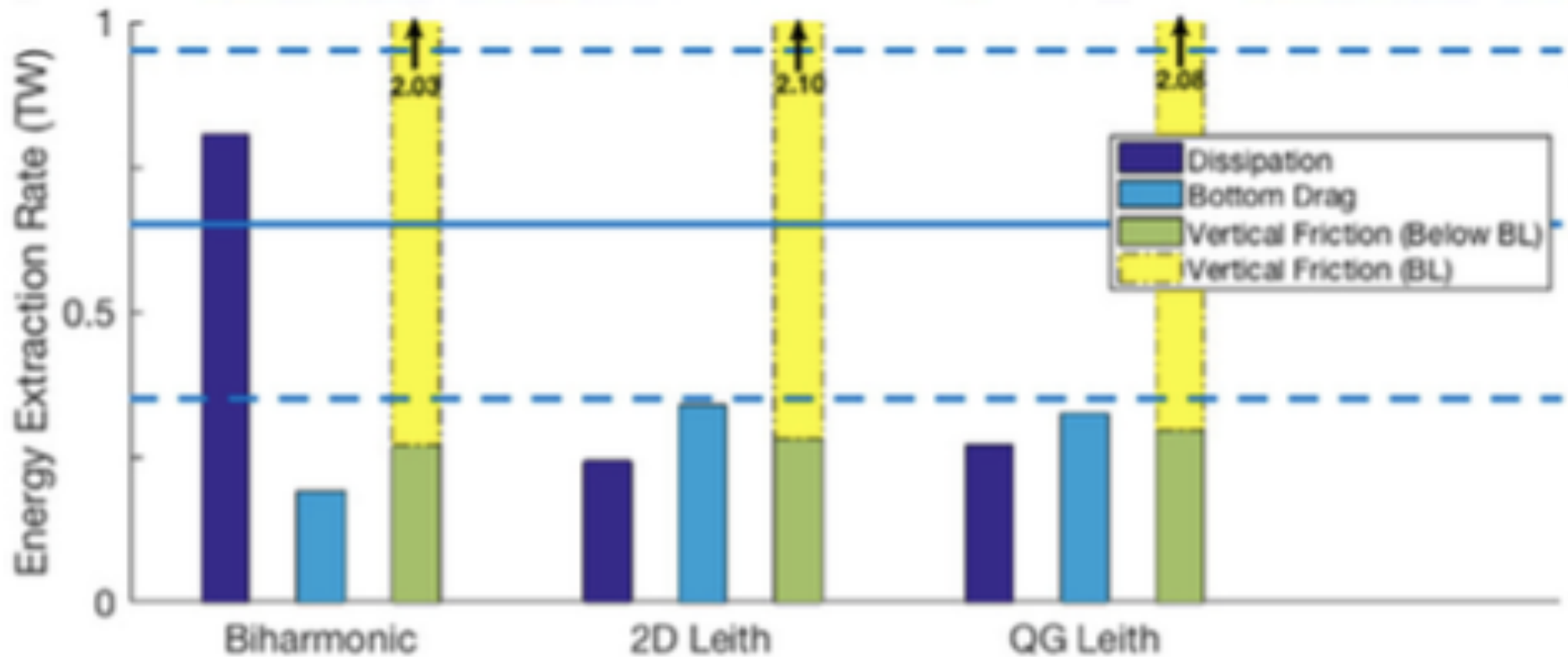
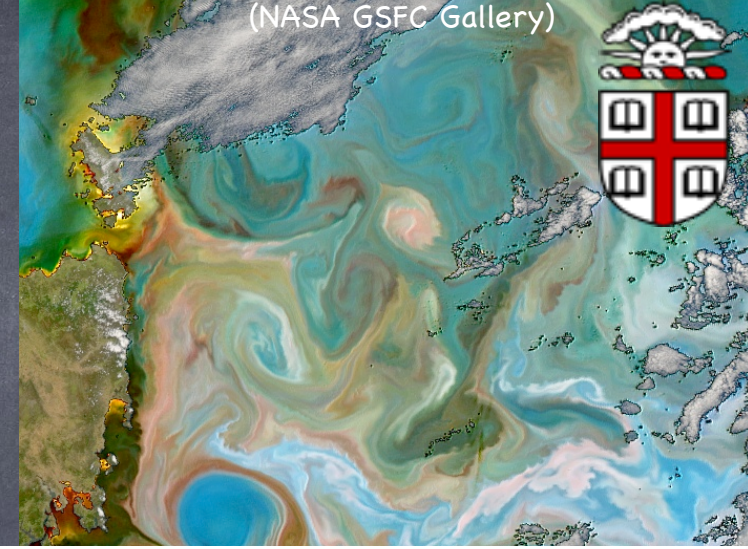


Fig. 9. Global energy extraction rates by dissipation, bottom drag, vertical friction in the boundary layer, and vertical friction below the boundary layer for each simulation. The solid line shows the observed global bottom drag energy extraction calculated by [Wright et al. \(2013\)](#), along with error bars (dotted lines). This figure uses a snapshot of the flow field. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

The Mesoscale

← 100 km



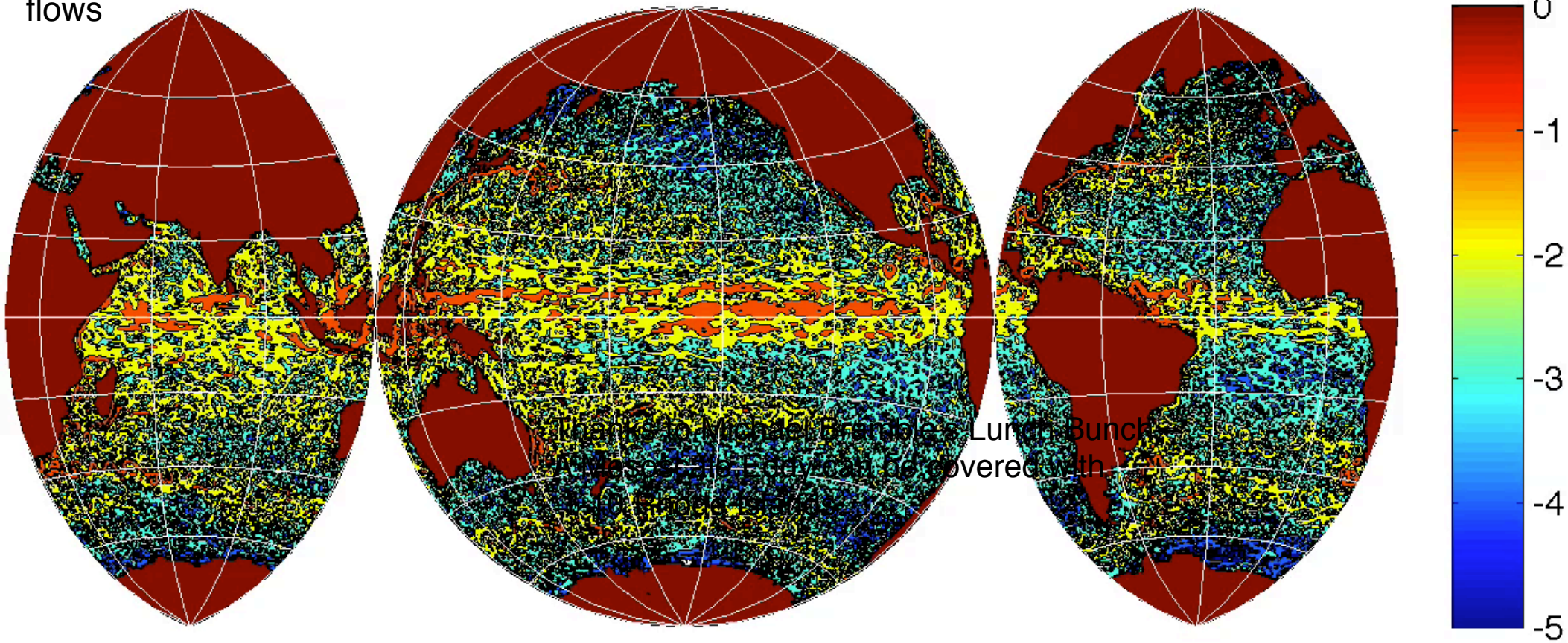
(Capet et al., 2008)



- Boundary Currents
- Eddies
- 100km, months

Satellite altimetry
view of mesoscale
flows

AVISO: $\log_{10}(0.5(u^2+v^2))$ on 19940101

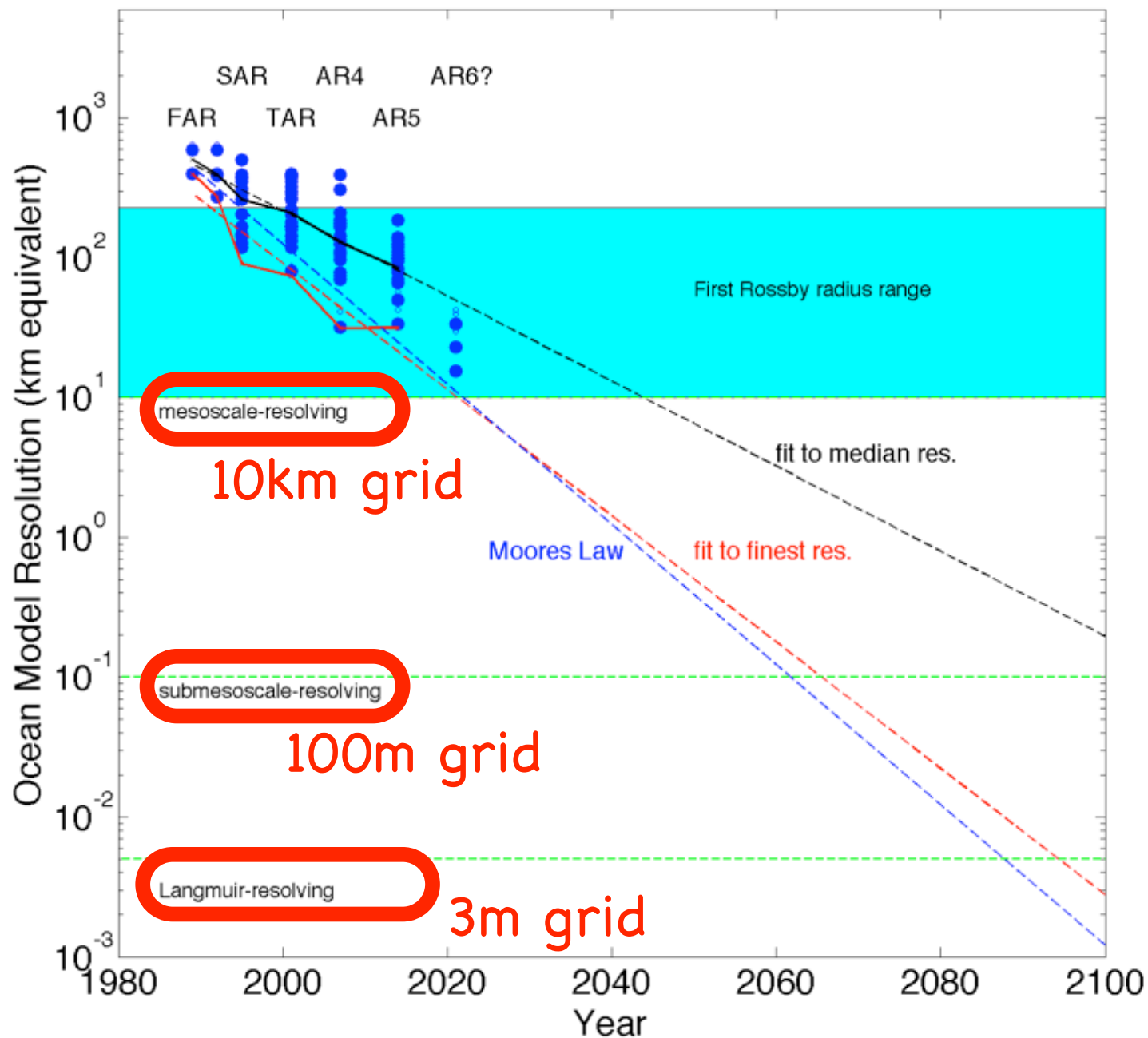


Too Simple: What about directly modeling processes in climate models?

Don't we have big enough computers? or won't we soon?



Resolution of Ocean Component of Coupled IPCC models



Here are the collection of IPCC models...

If we can't resolve a process, we need to develop a parameterization or subgrid model of its effect



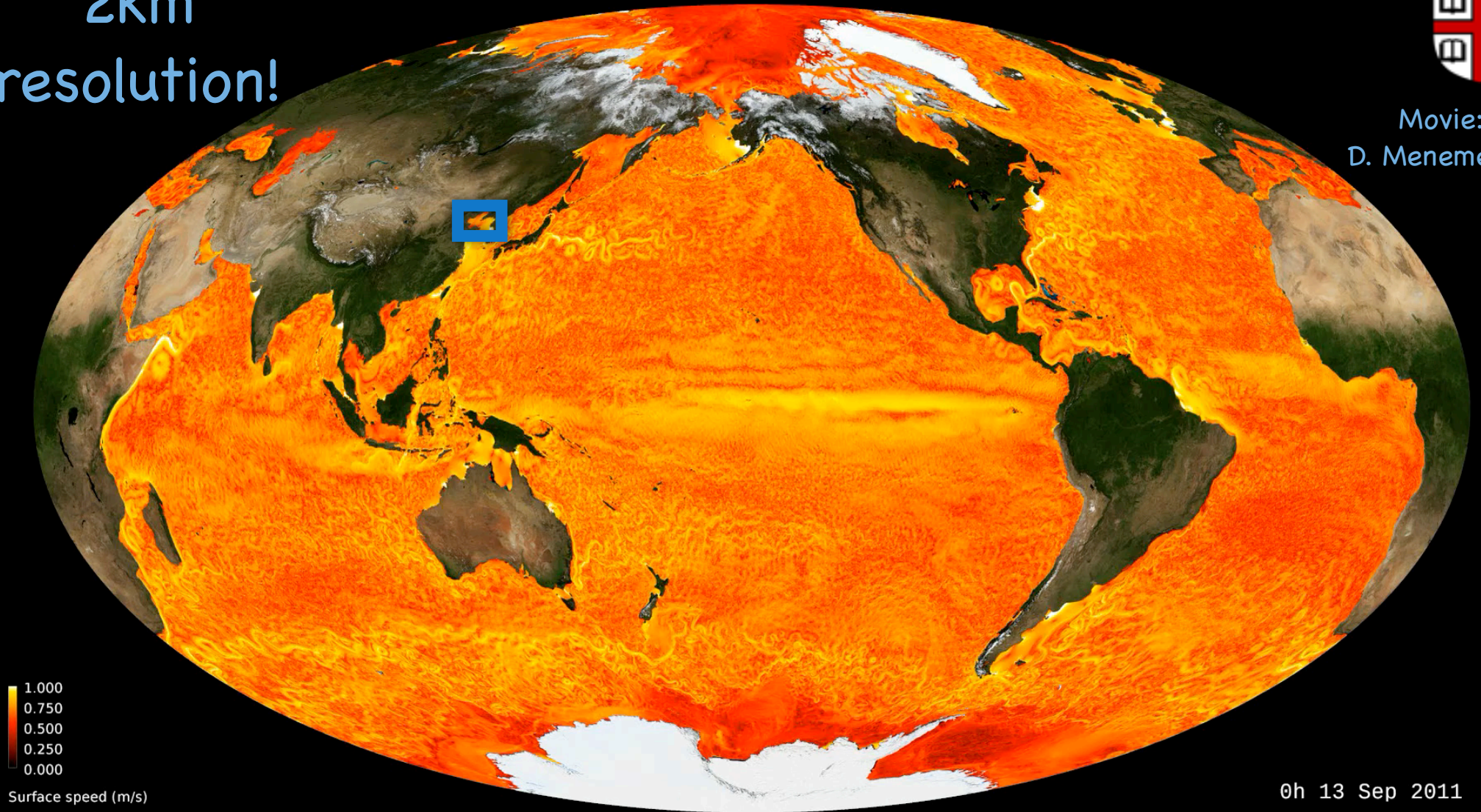
Viscosity Scheme: BFK and D. Menemenlis. Can large eddy simulation techniques improve mesoscale-rich ocean models? In M. Hecht and H. Hasumi, editors, *Ocean Modeling in an Eddying Regime*, volume 177, pages 319-338. AGU Geophysical Monograph Series, 2008.

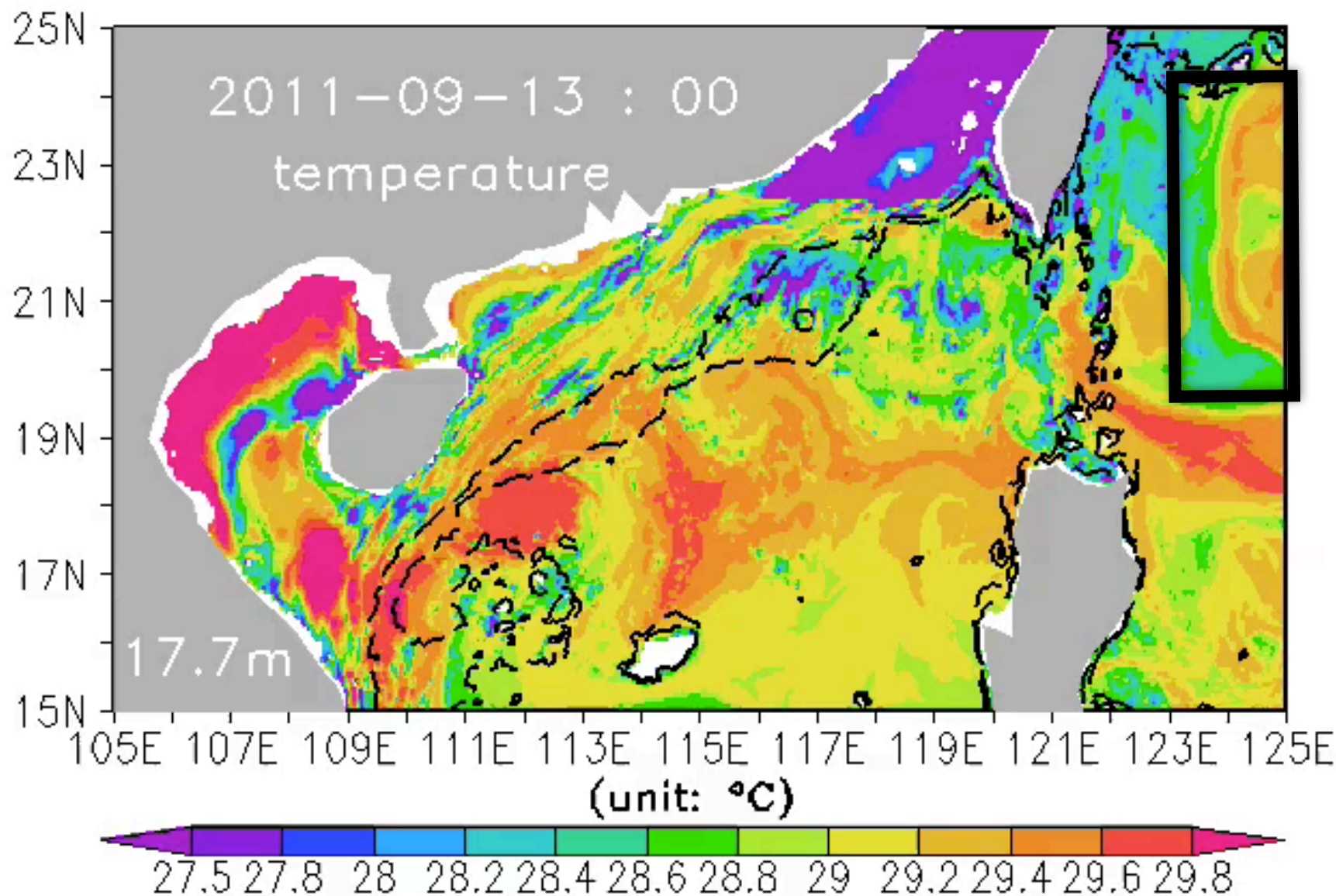
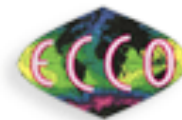


2km
resolution!



Movie:
D. Menemenlis





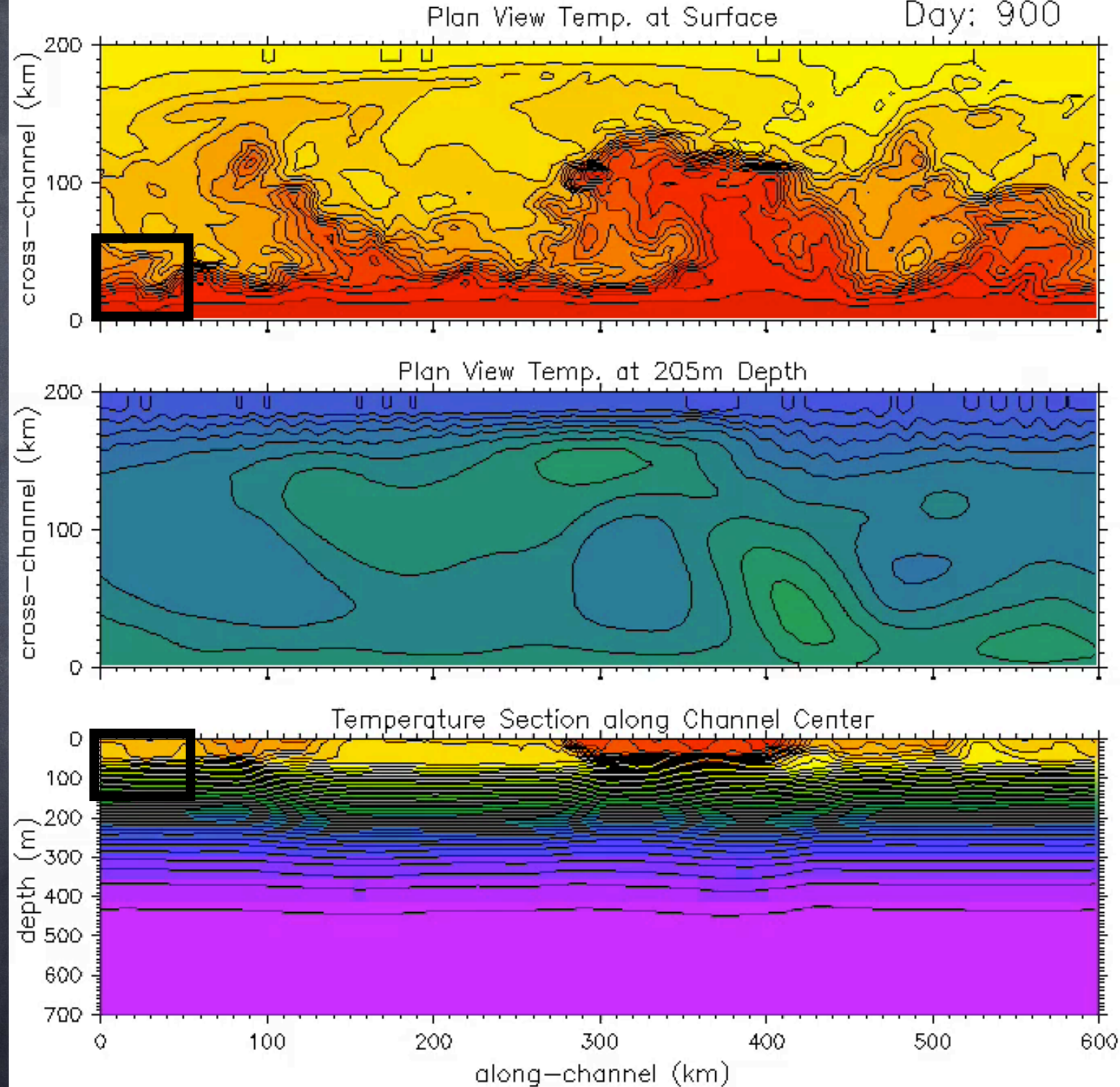
Movie:
Z. Jing

Brown Visitor
from
S. China Sea
Institute of Ocean.

Z. Jing, Y. Qi, BFK, Y. Du, and S. Lian. Seasonal thermal fronts and their associations with monsoon forcing on the continental shelf of northern South China Sea: Satellite measurements and three repeated field surveys in winter, spring and summer. *Journal of Geophysical Research-Oceans*, August 2015. Submitted.

200km x 600km
x 700m
domain

1000 Day
Simulation



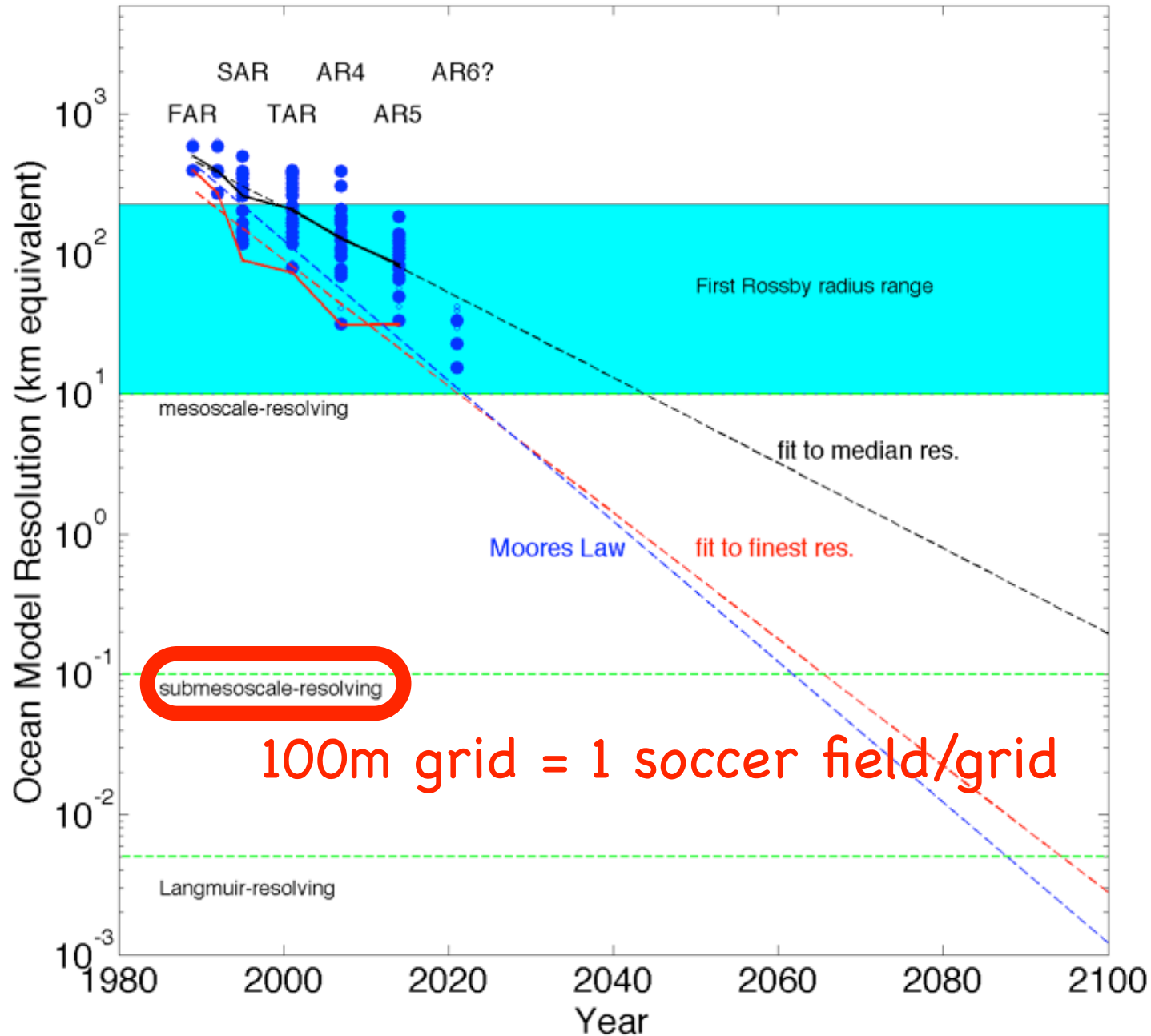
G. Boccaletti, R. Ferrari, and BFK. Mixed layer instabilities and restratification. *Journal of Physical Oceanography*, 37(9): 2228-2250, 2007.

What about modeling important processes in climate models?

Don't we have big enough computers? or won't we soon?



Resolution of Ocean Component of Coupled IPCC models



Here are the collection of IPCC models...

If we can't resolve a process, we need to develop a parameterization or subgrid model of its effect

The Character of the Submesoscale

(Capet et al., 2008)

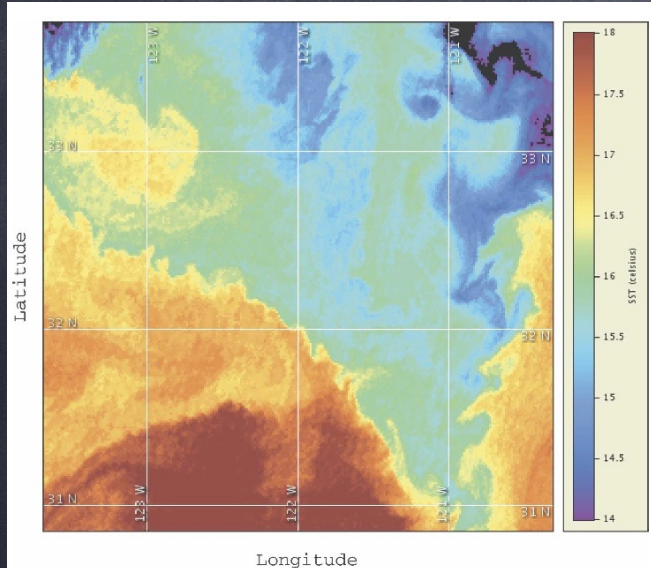
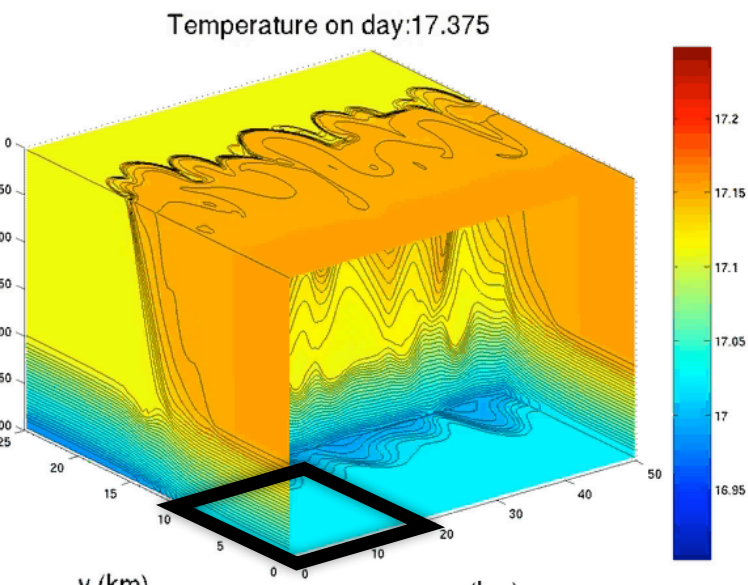


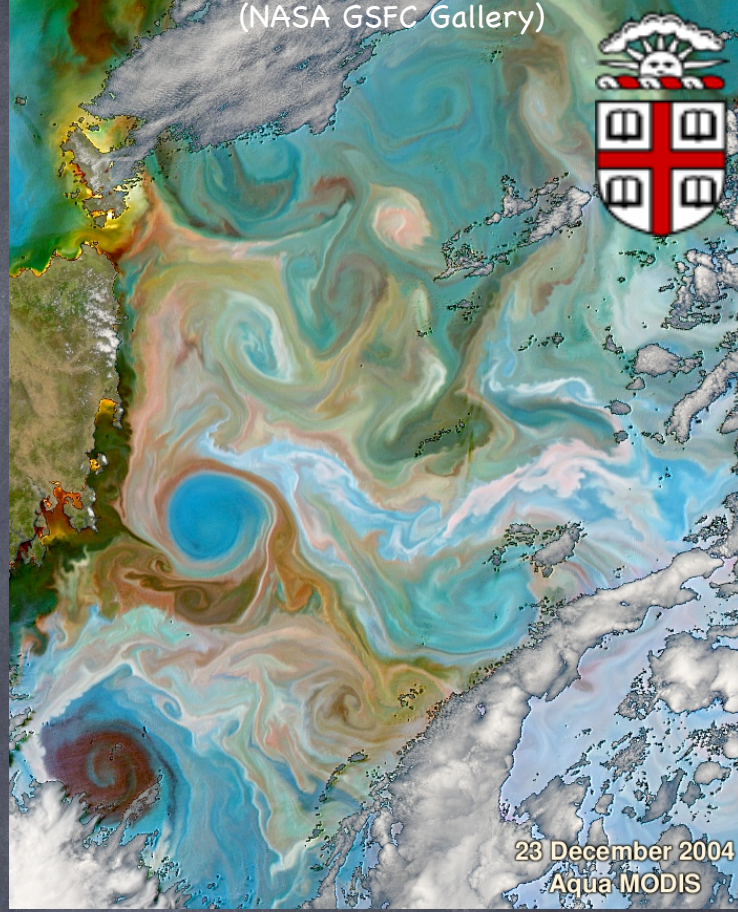
FIG. 16. Sea surface temperature measured at 1832 UTC 3 Jun 2006 off Point Conception in the California Current from CoastWatch (<http://coastwatch.pfeg.noaa.gov>). The fronts between recently



- Fronts
- Eddies
- $Ro=O(1)$
- $Ri=O(1)$
- near-surface ($H=100m$)
- 1-10km, days

Eddy processes often
baroclinic instability
 Parameterizations =
 BFK et al (08-11).

←
10
km



BFK, R. Ferrari, and R. W. Hallberg. Parameterization of mixed layer eddies. Part I: Theory and diagnosis. *Journal of Physical Oceanography*, 38(6):1145-1165, 2008

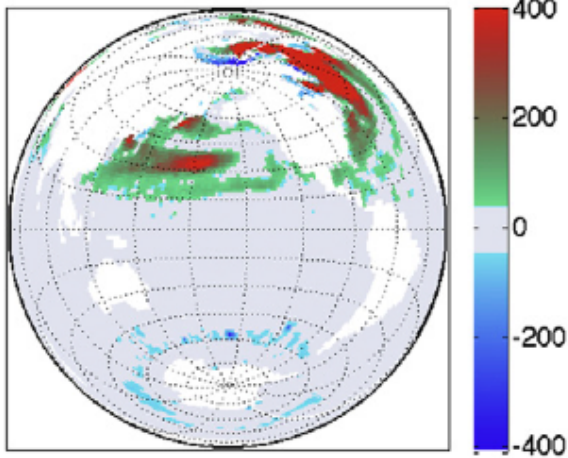
BFK, G. Danabasoglu, R. Ferrari, S. M. Griffies, R. W. Hallberg, M. M. Holland, M. E. Maltrud, S. Peacock, and B. L. Samuels. Parameterization of mixed layer eddies. III: Implementation and impact in global ocean climate simulations. *Ocean Modelling*, 39:61-78, 2011.

S. Bachman and BFK. Eddy parameterization challenge suite. I: Eady spindown. *Ocean Modelling*, 64:12-28, 2013

Global Ocean Climate is SENSITIVE to these Submesoscale Eddies! At least in parameterized form

Implemented in IPCC AR5 & 6: NCAR, GFDL, Hadley, NEMO,...

CM2M H_{ml} Control-deBM (m) FEB



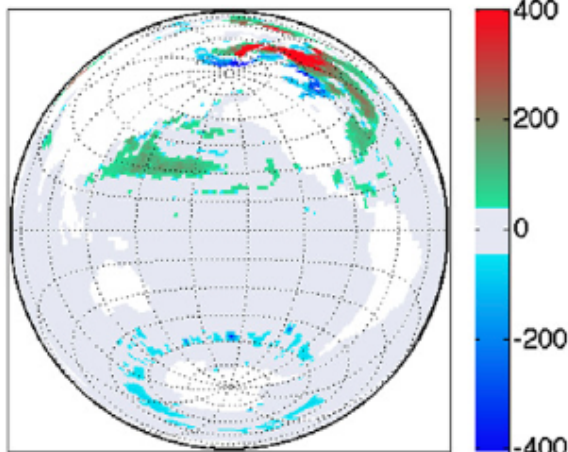
max=2528m, min=-1560m

February
Mixed layer
depth Bias w/o
MLE

Deep Mixed Layer
Bias reduced

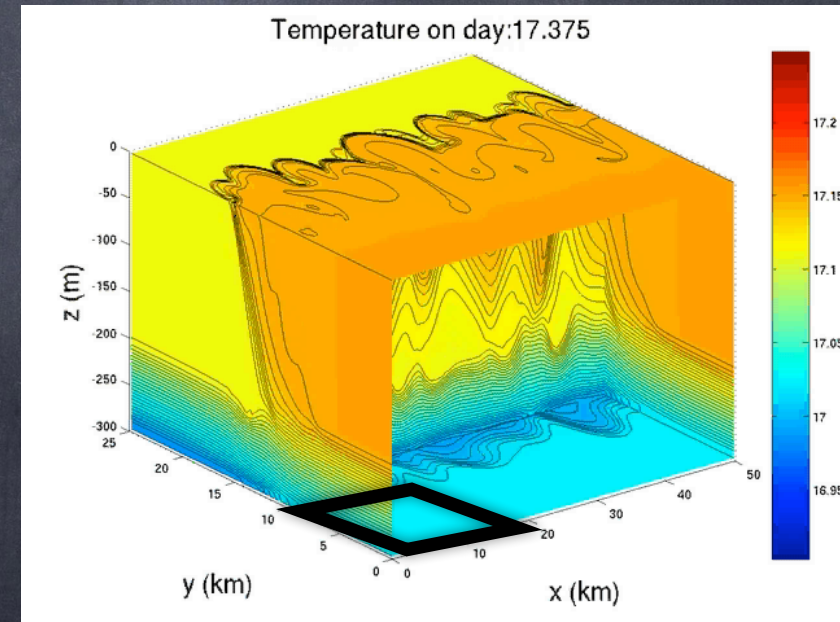
$O(0.1 \text{ W/m}^2)$ change to
global mean net fluxes,
Regional: 5 to 50 W/m^2

CM2M H_{ml} Submeso-deBM (m) FEB



max=1422m, min=-1600m

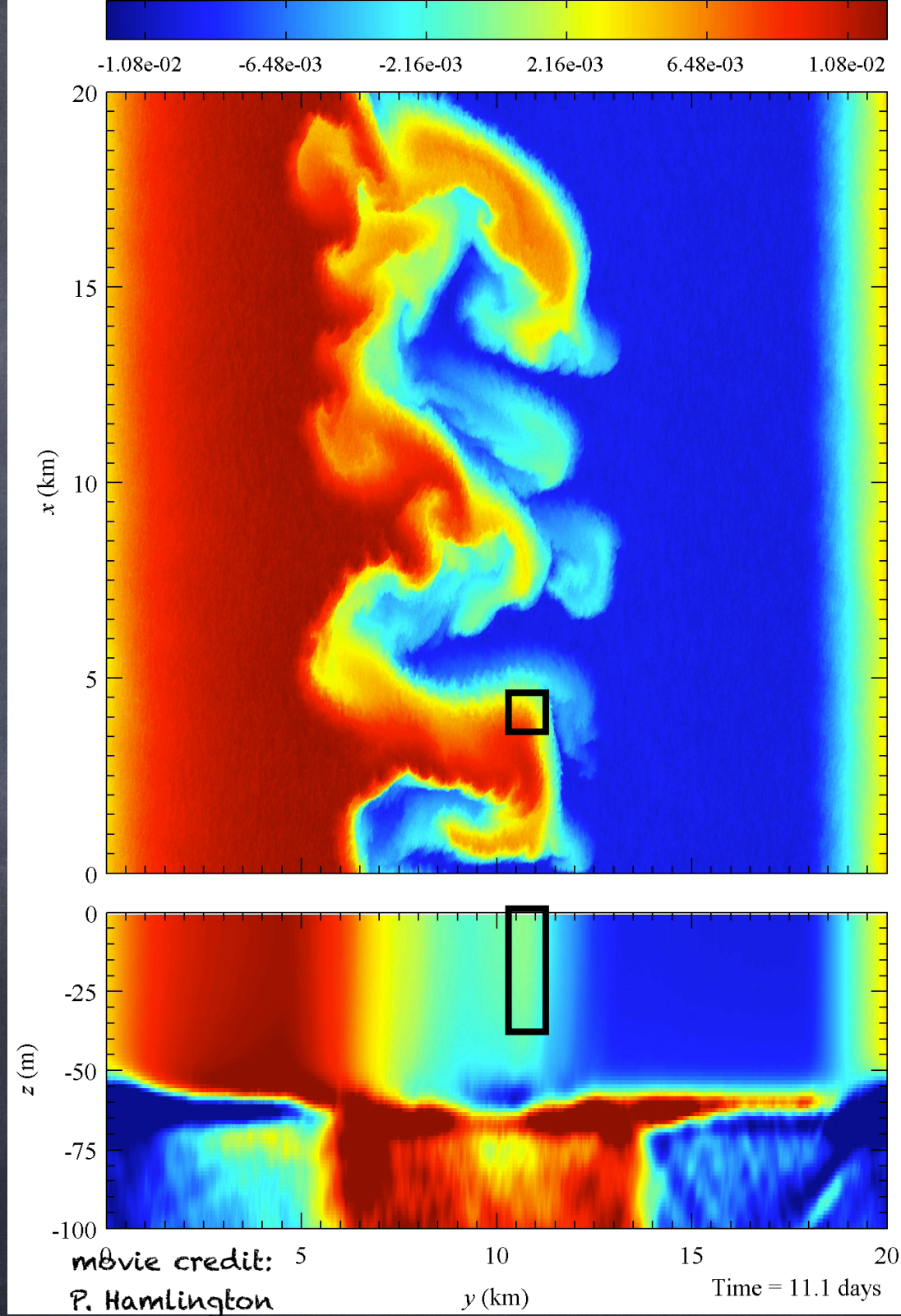
February
MLD Bias
With MLE
Parameterization



20km x 20km x 150m
domain

10 Day Simulation

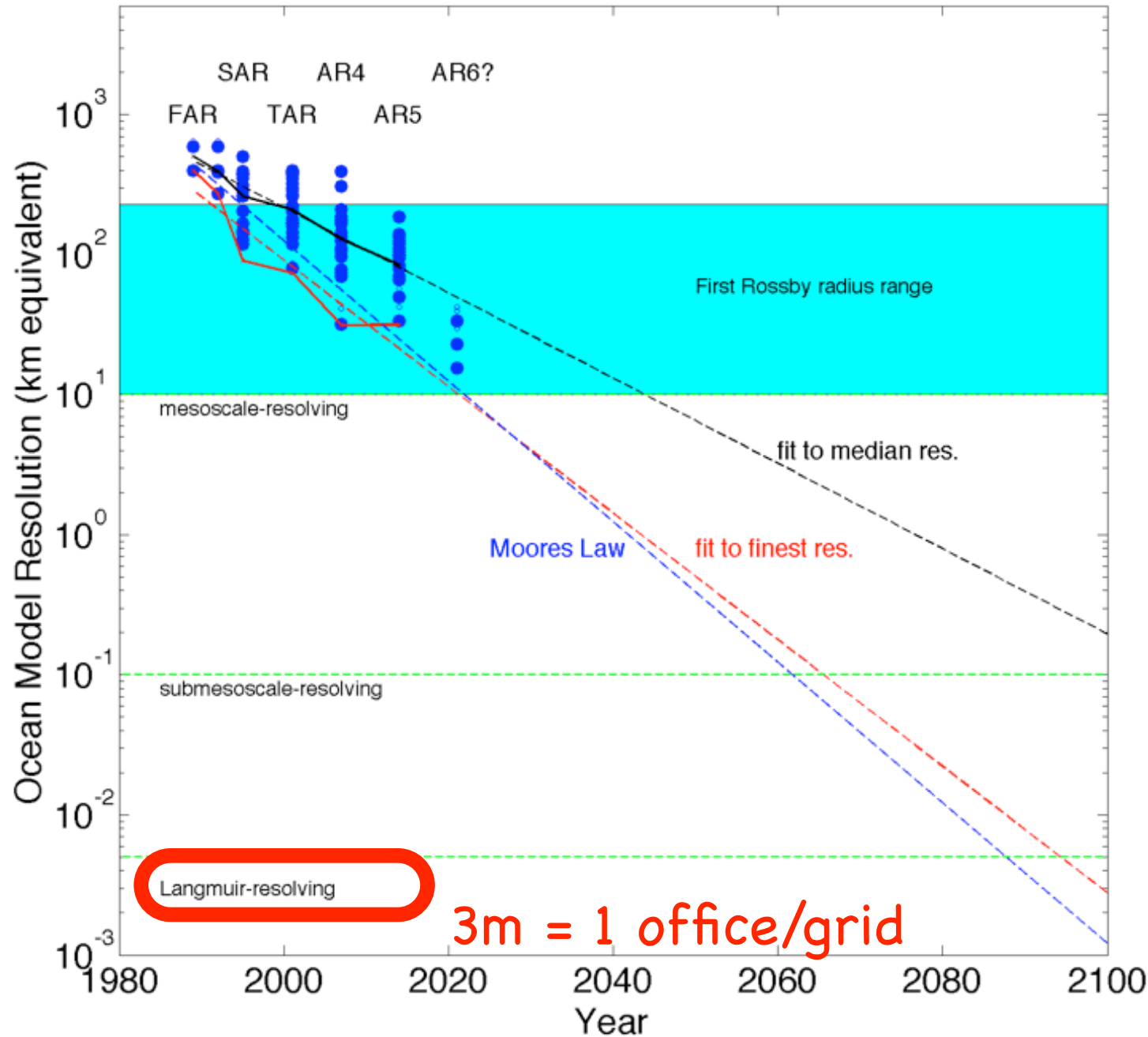
P. E. Hamlington, L. P. Van Roekel, BFK, K. Julien, and G. P. Chini. Langmuir-submesoscale interactions: Descriptive analysis of multiscale frontal spin-down simulations. *Journal of Physical Oceanography*, 44(9): 2249-2272, September 2014.



Climate Model Resolution: an issue for centuries to come!



Resolution of Ocean Component of Coupled IPCC models



Here are the collection of IPCC models...

If we can't resolve a process, we need to develop a parameterization or subgrid model of its effect

The Character of Langmuir Turbulence

- Near-surface
- Langmuir Cells & Langmuir Turb.
- $Ro \gg 1$
- $Ri < 1$: Nonhydro
- 1-100m ($H=L$)
- 10s to 1hr
- $w, u = O(10\text{cm/s})$
- Stokes drift
- Eqtns: Wave-Averaged
- Resolved routinely in 2170

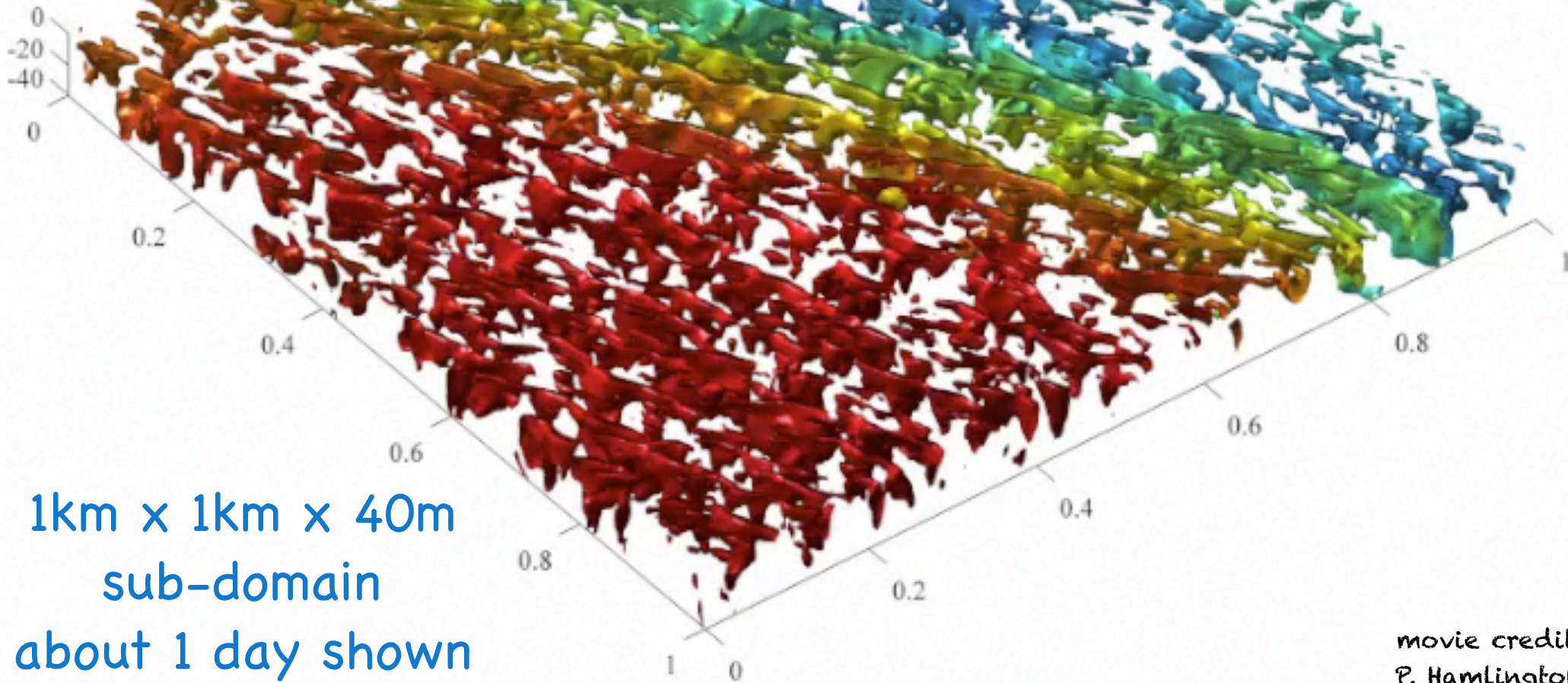
Image: NPR.org,
Deep Water
Horizon Spill

Langmuir Scale

Colors=Temp.
Surfaces on
Large w



20km x 20km x 150m domain
10 Day Simulation



1km x 1km x 40m
sub-domain
about 1 day shown

movie credit:
P. Hamlington

P. E. Hamlington, L. P. Van Roekel, BFK, K. Julien, and G. P. Chini. Langmuir-submesoscale interactions: Descriptive analysis of multiscale frontal spin-down simulations. *Journal of Physical Oceanography*, 44(9):2249-2272, September 2014.

Q. Li, A. Webb, BFK, A. Craig, G. Danabasoglu, W. G. Large, and M. Vertenstein, 2016: Langmuir mixing effects on global climate: WAVEWATCH III in CESM. *Ocean Modelling*, 103:145– 160.



Turbulence: what to do?

- Climate modelling requires that we truncate the model grid at coarse resolution (albeit improving slowly)
- Whatever resolution we can afford will leave some physics unresolved or partially-resolved, so we need subgrid closures!
- The vast & diverse scales of motion in the ocean suggest that we cannot use a one-size-fits-all approach, e.g., a turbulent cascade of 3d turbulence
- So, we have to invent new subgrid closures repeatedly, parameterizing processes important at each gridscale

Between Climate & Kolmogorov

Climate "Cells", "Gyres"
and "Modes"

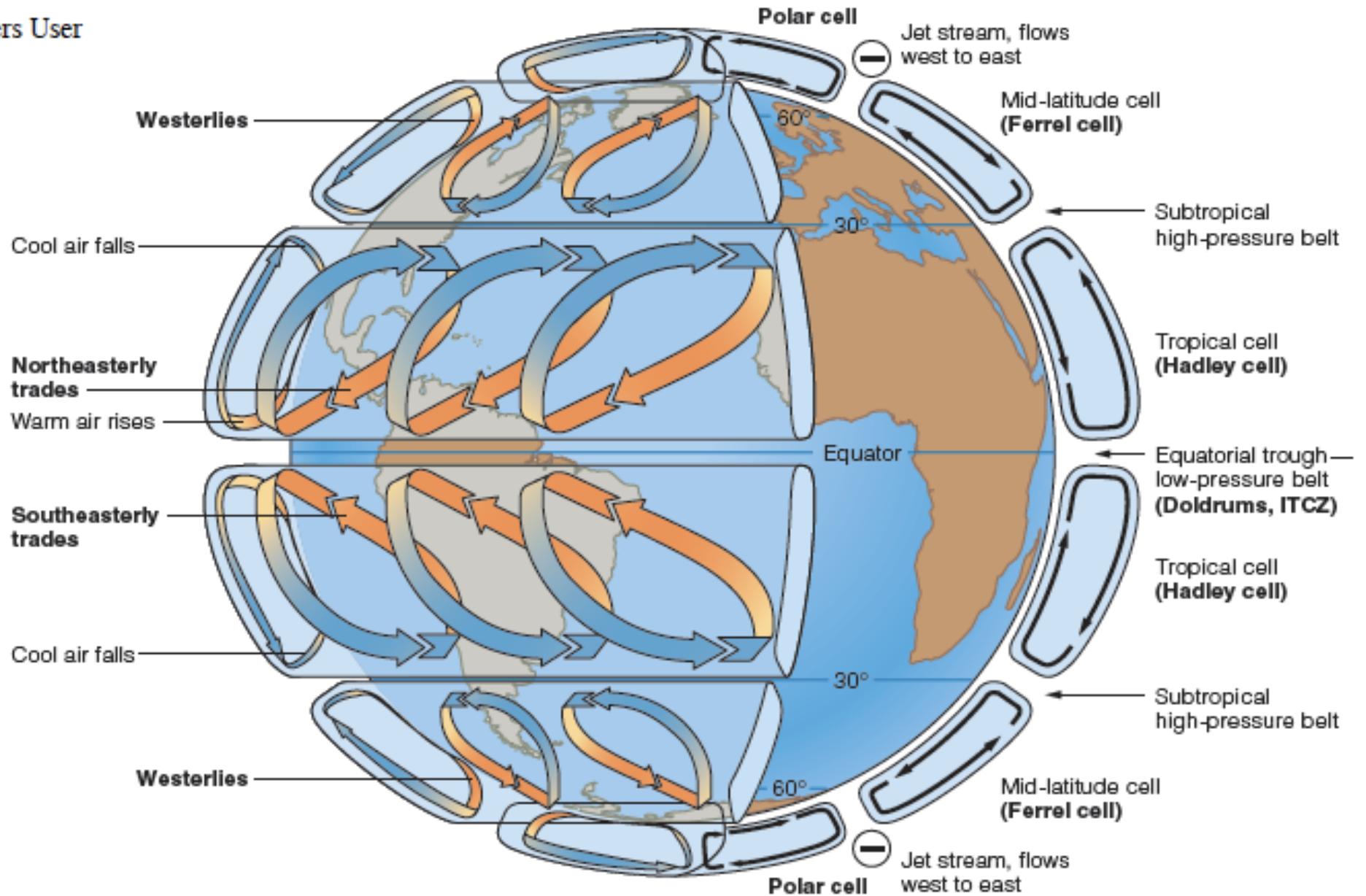
"Modes"=?="Fluctuations"?

Atmospheric Cells

Thermally direct, e.g., Hadley Cells, are heat engines.

Thermally indirect are rectification of turbulence (storms)

iChapters User



Oceanic Gyres

Flow along pressure contours (due to Coriolis)

These wind-driven features dominate thermal transport

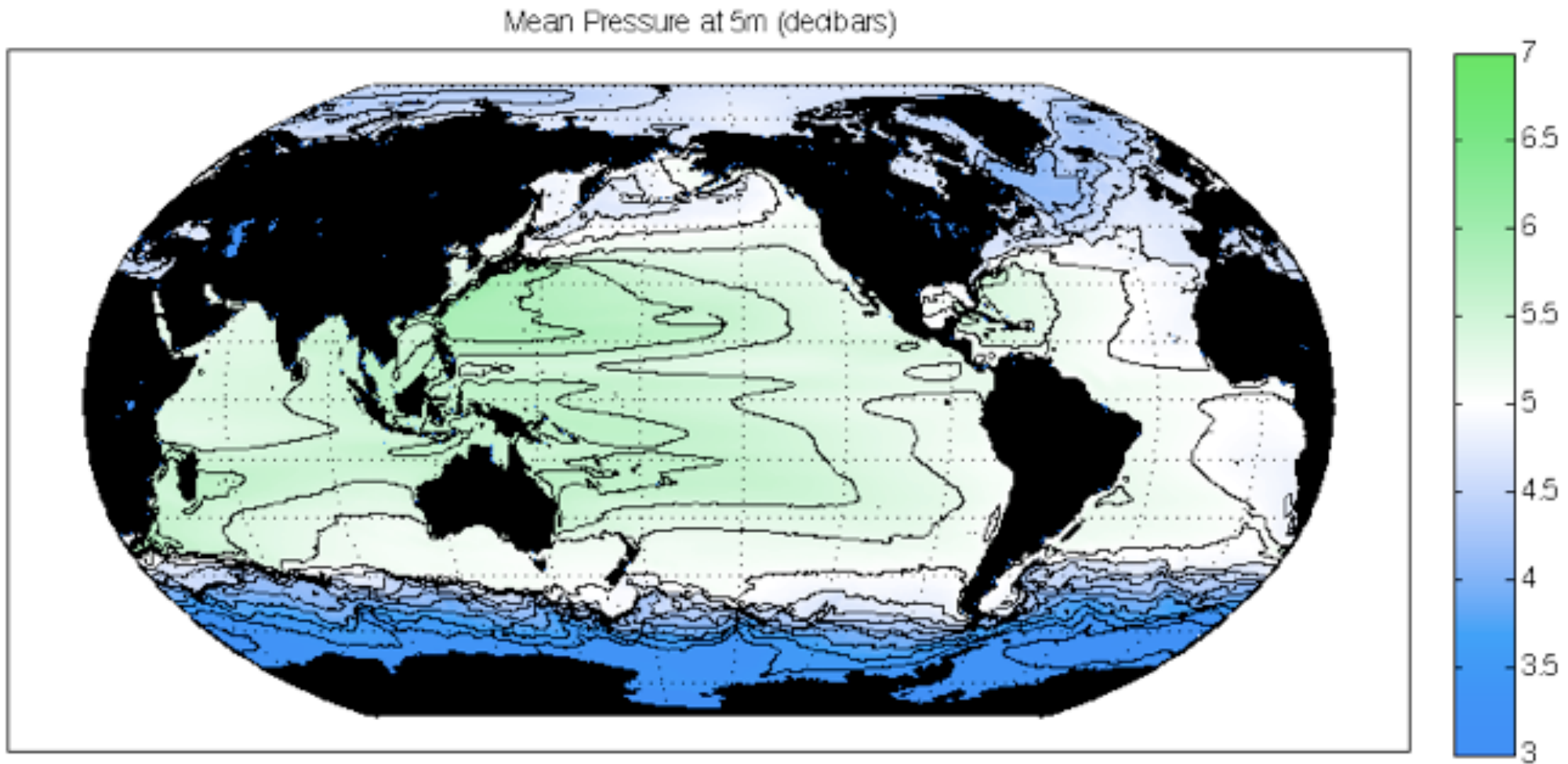
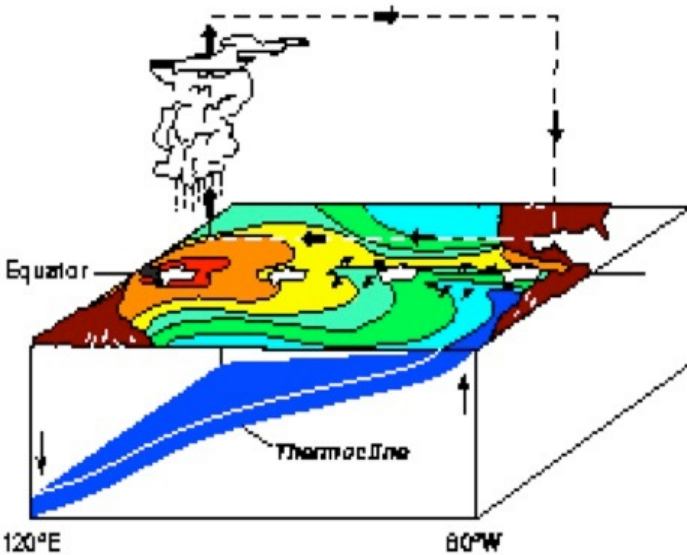


Figure 6: Pressure relative to atmospheric pressure just below the sea surface (5 meters depth) from the ECCO2 ocean data assimilating ocean model (Menemenlis et al. 2008, ecco2.org). Contour interval is 0.2 decibars.

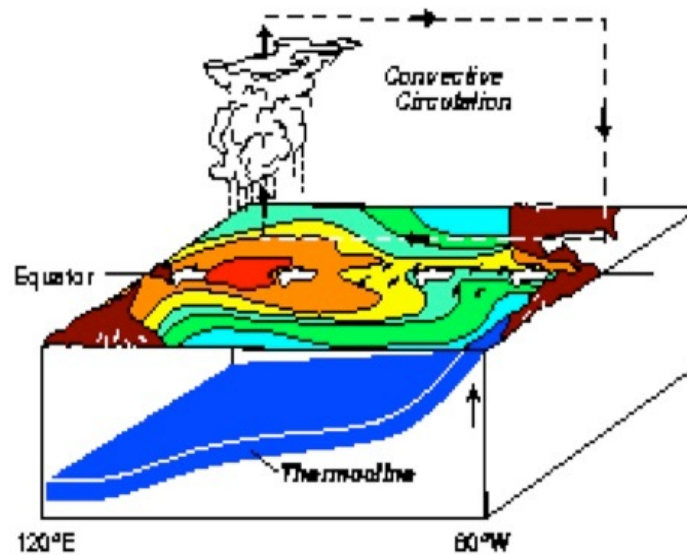
Climate Variability "Modes"

The most famous is El Niño/Southern Oscillation:
By most metrics, it is the largest mode of variability
on the Earth after seasonal & diurnal cycles.

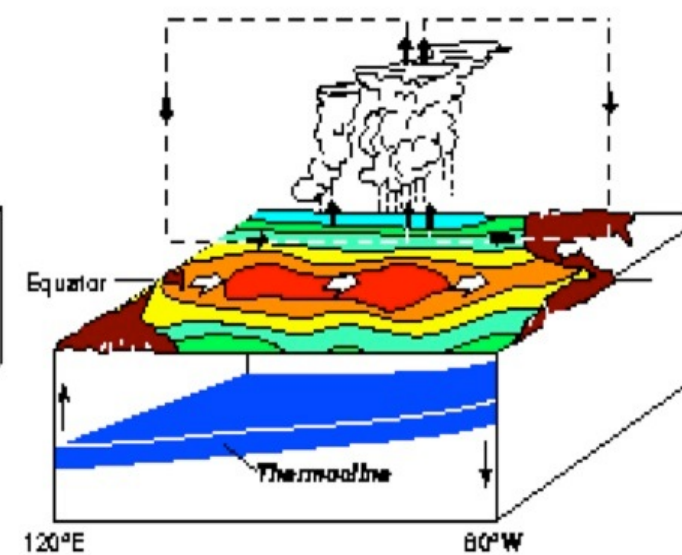
La Niña Conditions



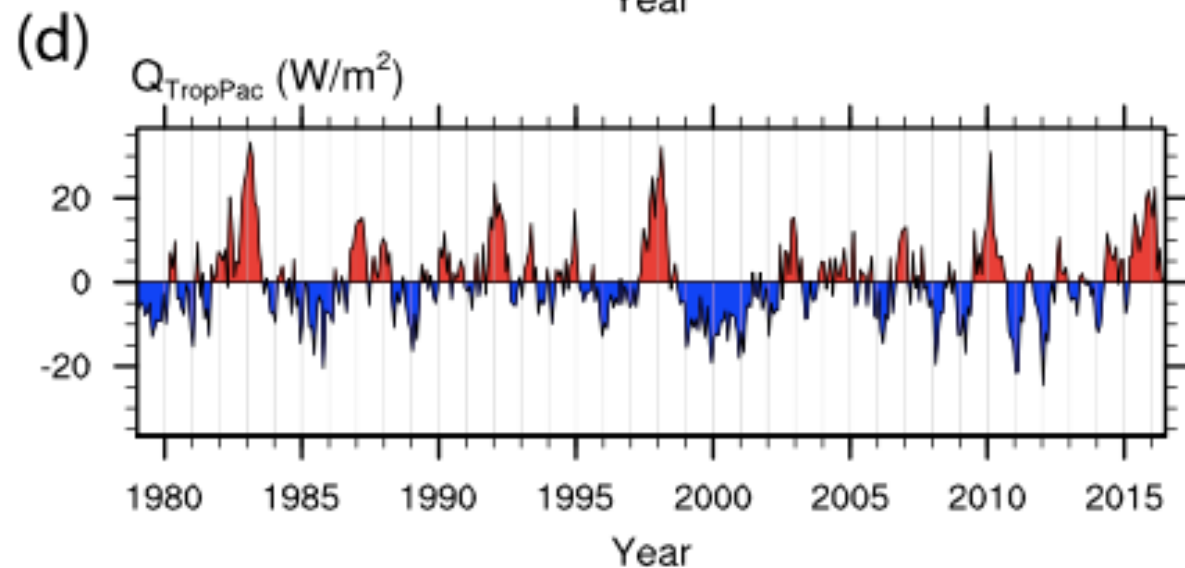
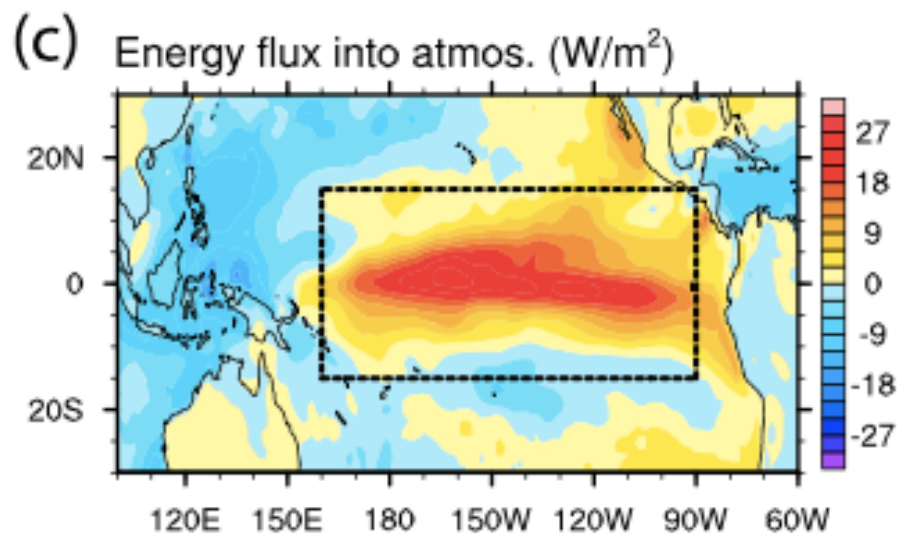
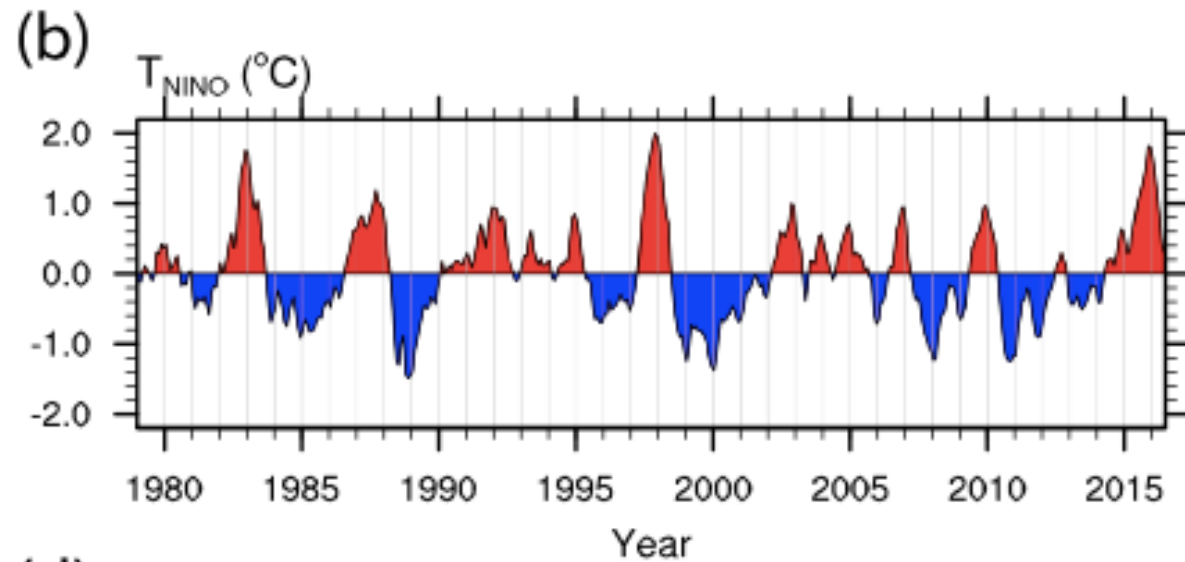
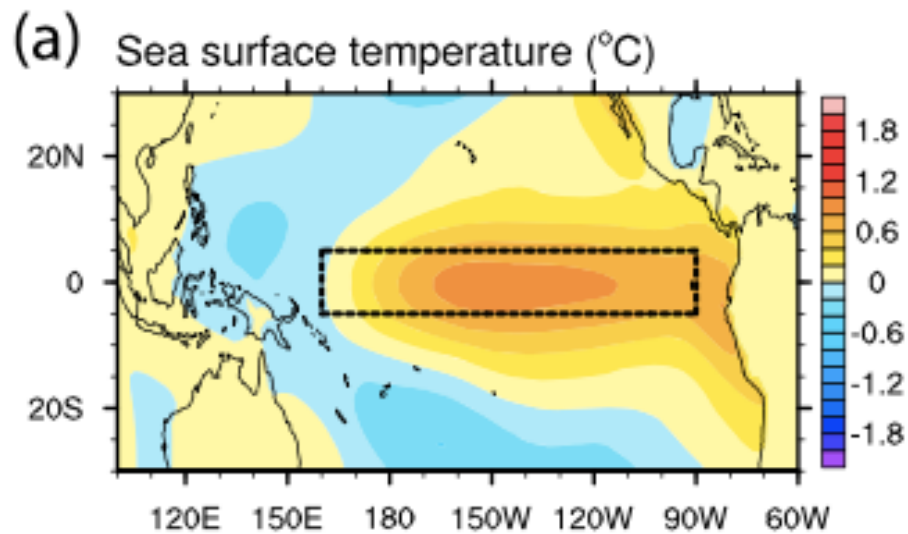
Normal Conditions



El Niño Conditions



Effect of Climate Modes, e.g., Hu & Fedorov (2017)

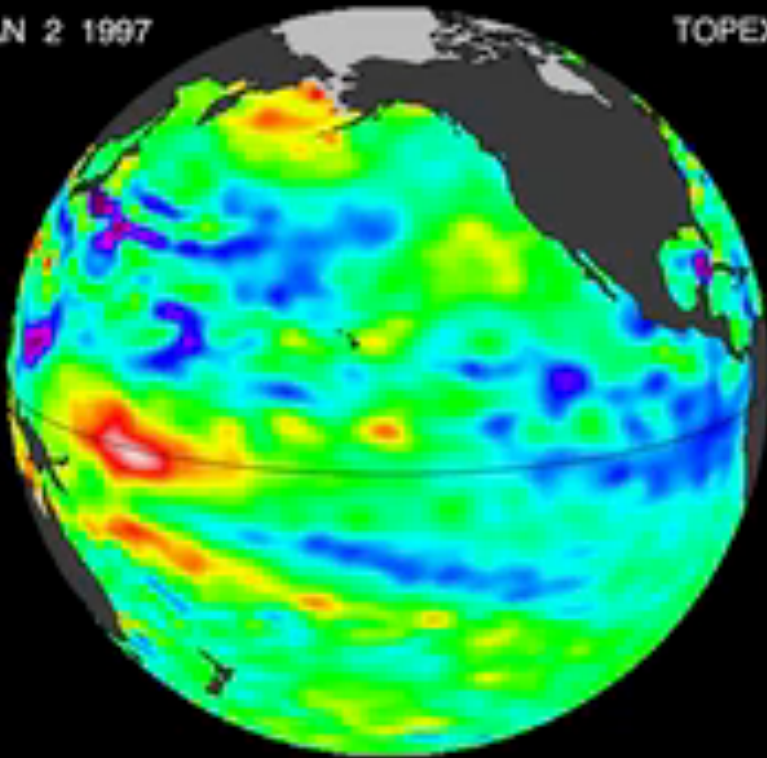


$$\frac{dT_g}{dt} = -\frac{T_g}{\tau} + a \cdot \log(\text{CO}_2/\text{CO}_{2,\text{ref}}) + b \cdot T_{\text{NINO}} + c \cdot \text{SAOD} + d,$$

El Nino: 1998 vs 2015

JAN 2 1997

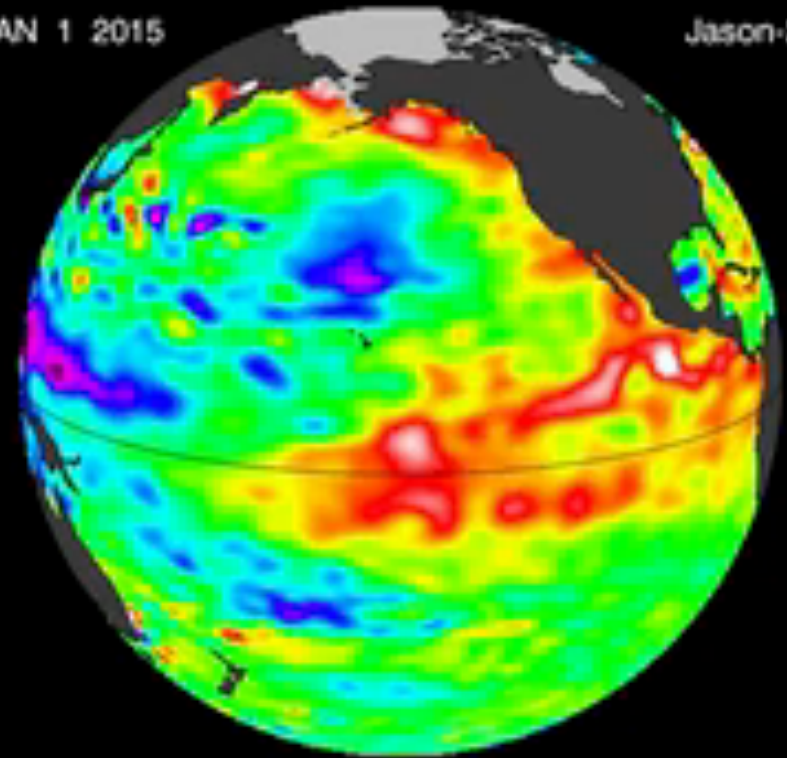
TOPEX/POS



TOPEX/Poseidon 1997-1998

JAN 1 2015

Jason-2



Jason-2 2015-2016

© SSH Movie Credit: NASA JPL

Observing & Prediction Challenges

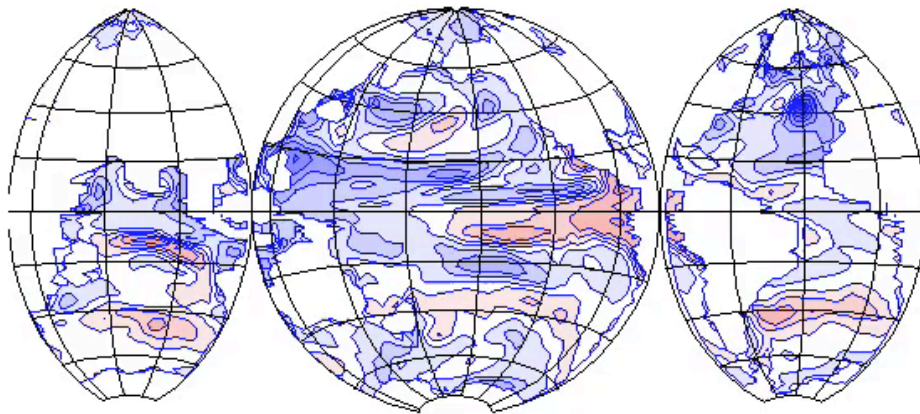
"Cells", "Gyres", "Modes",
& "Weather"

What does a climate model—WITHOUT WARMING—look like in Ocean Heat Content Variability?

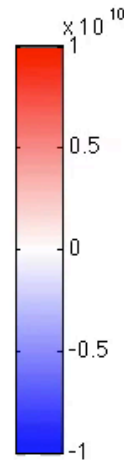


Doesn't even include mesoscale eddies

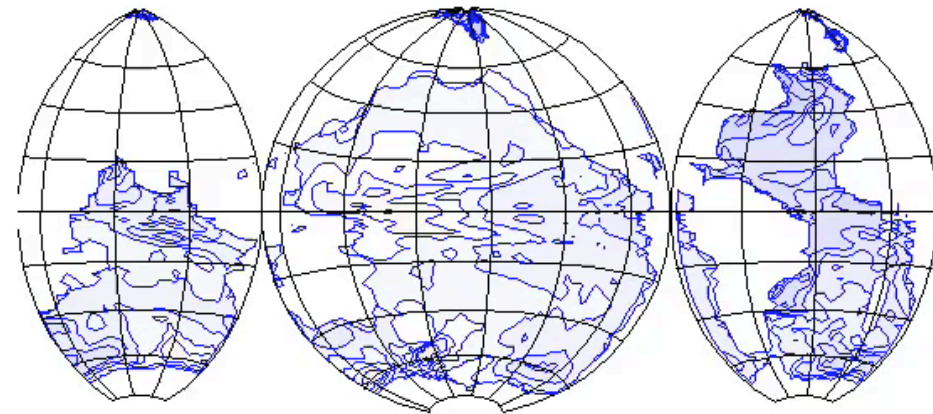
0-2km Depth Heat Content Anomaly (J) in year 200



Contours = 4 units



Below 2km Depth Heat Content Anomaly (J) in year 200



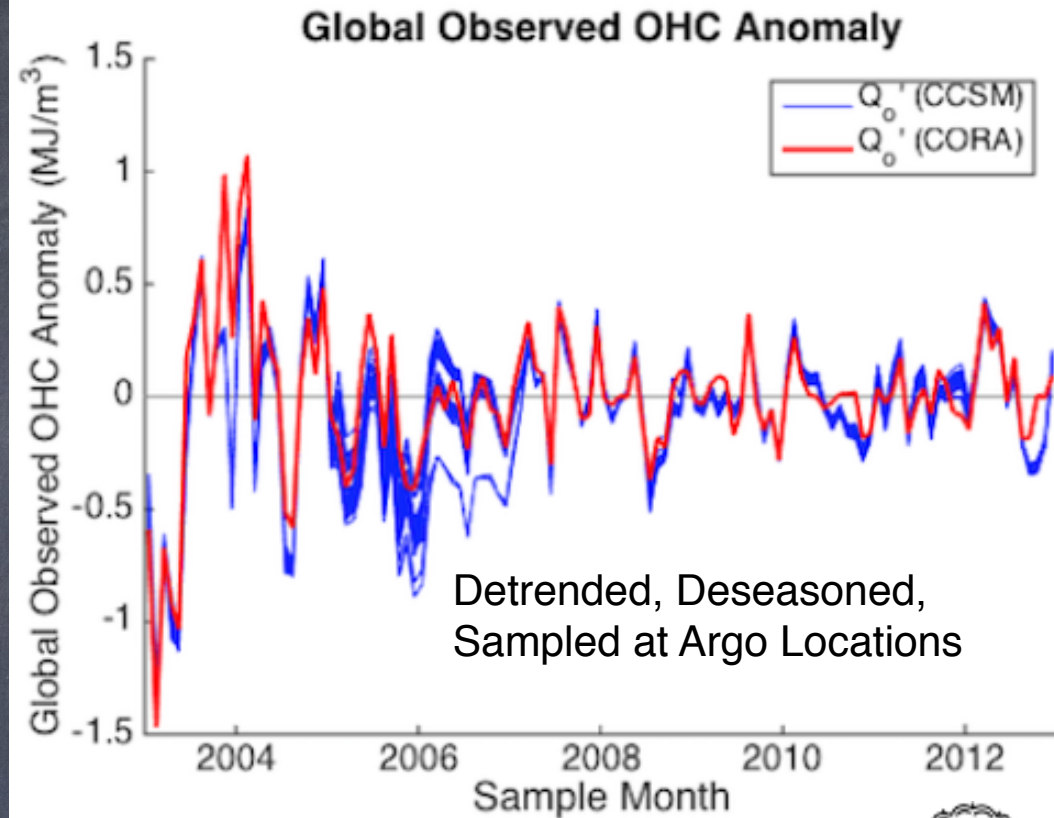
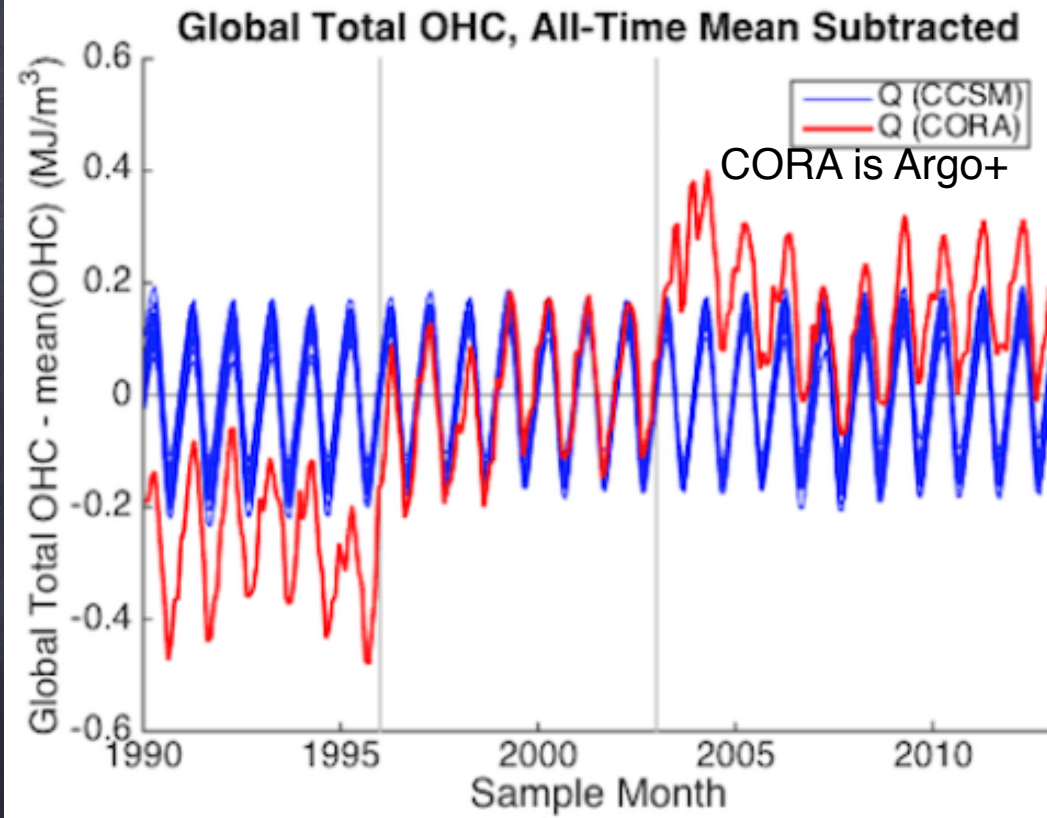
Contours = 1 unit

From the >1000yr steady forcing CCSM3.5 runs of Stevenson et al. 2012

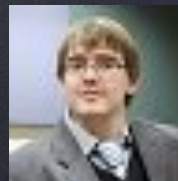
S. Stevenson, BFK, and M. Jochum, 2012: Understanding the ENSO-CO2 link using stabilized climate simulations. *Journal of Climate*, 25(22):7917–7936.



CU, now NCAR



Sophisticated analysis to overcome Ship & Argo sampling problems—inherent uncertainty, $O(0.2\text{W}/\text{m}^2)$, on interannual to decadal timescales in global average. $O(10\text{W}/\text{m}^2)$ without analysis.



CU, soon Brown

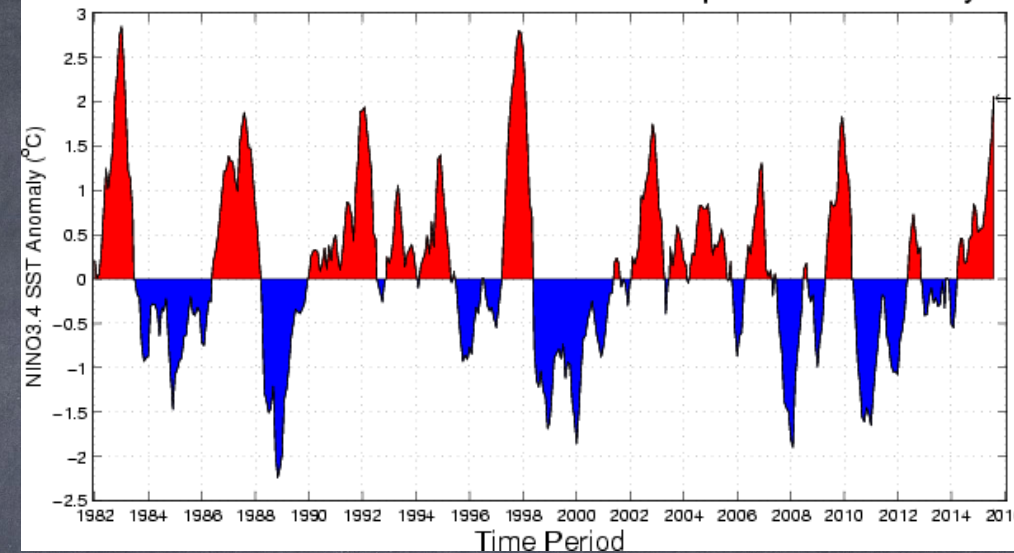


Prediction of variability

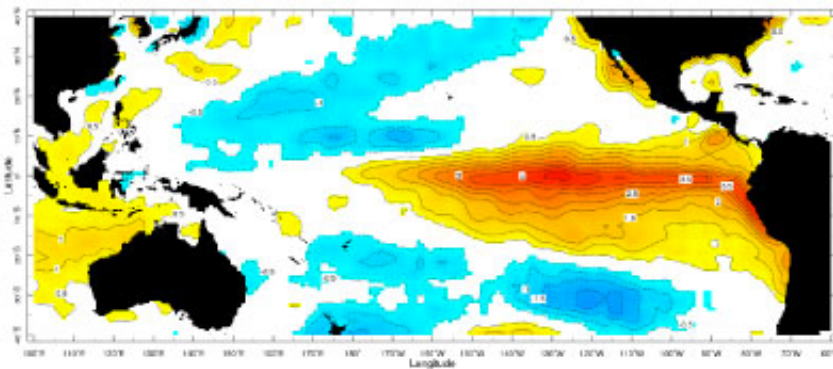
Predictability of ENSO events limited to < 1yr

ENSO statistics more predictable?

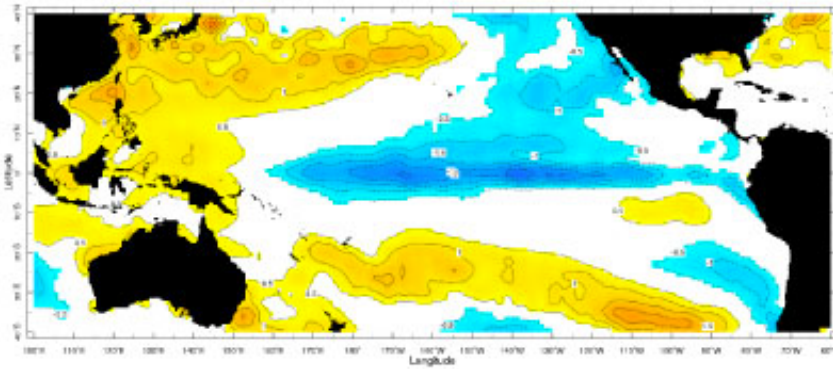
Historical NINO3.4 Sea Surface Temperature Anomaly



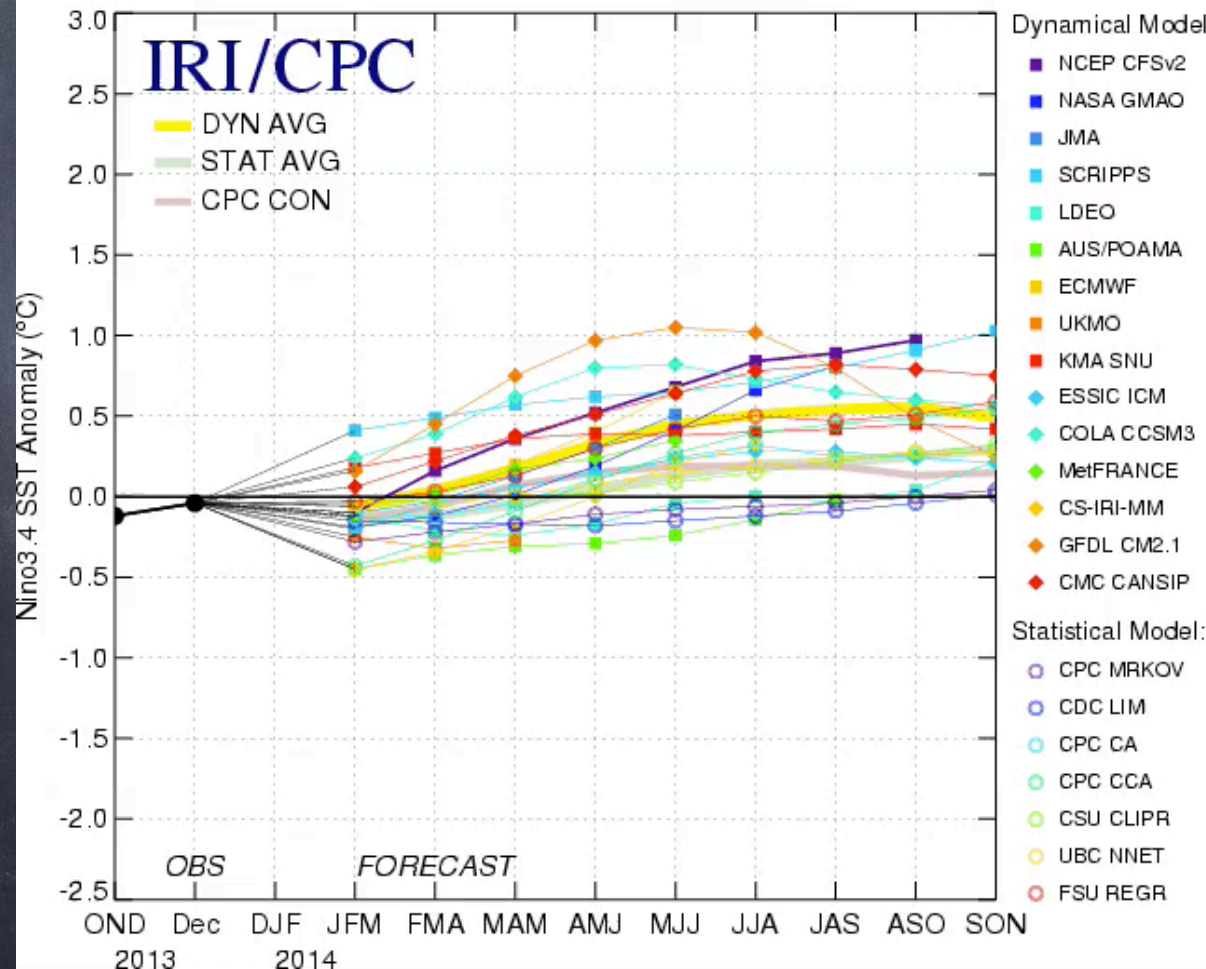
El Niño Episode Sea Surface Temperatures
 Departure from average in degrees Celsius
 Dec 1982 - Feb 1983



La Niña Episode Sea Surface Temperatures
 Departure from average in degrees Celsius
 Dec 1998 - Feb 1999



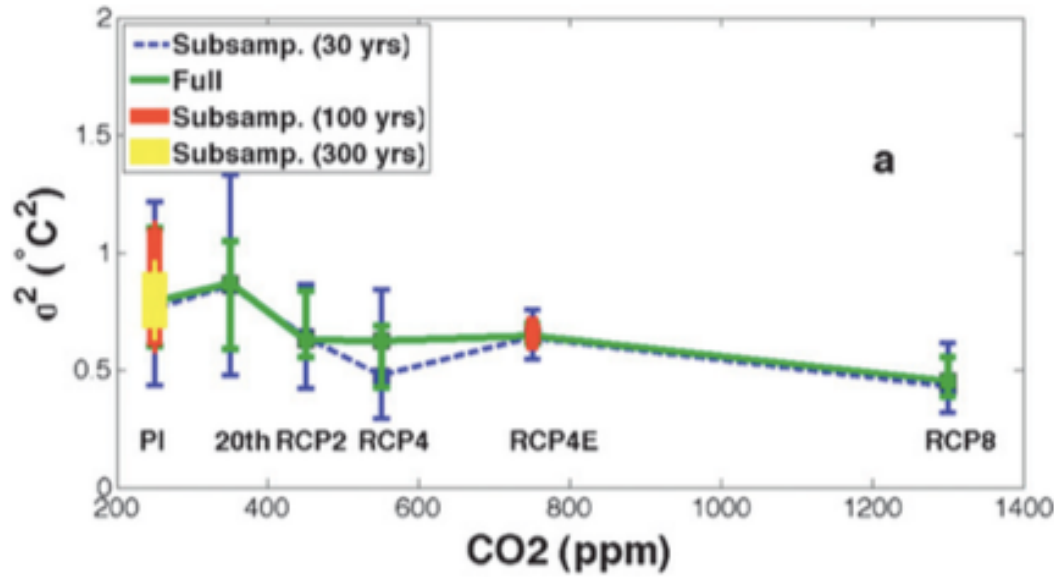
Mid-Jan 2014 Plume of Model ENSO Predictions



Does ENSO
variability
change with
climate?...
(>200 yr to detect)



CU, now UCSB



Big GHG Change
to ENSO impacts!

INDIRECT Proxy
Reconstructions
won't work!!!

S. Stevenson, BFK, M. Jochum, R. Neale, C. Deser, and G. Meehl.
Will there be a significant change to El Niño in the 21st century?
Journal of Climate, 25(6): 2129-2145, March 2012.

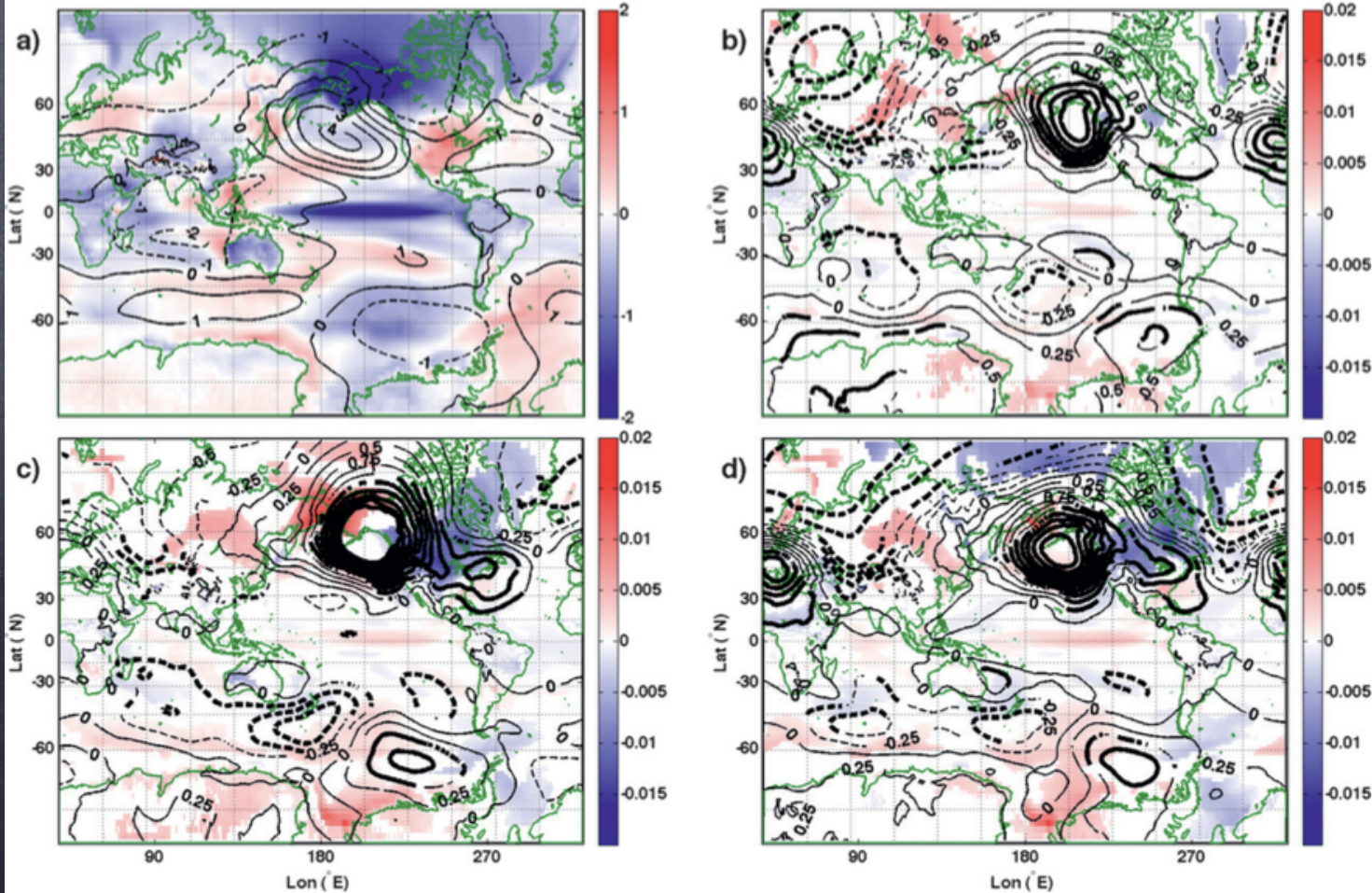


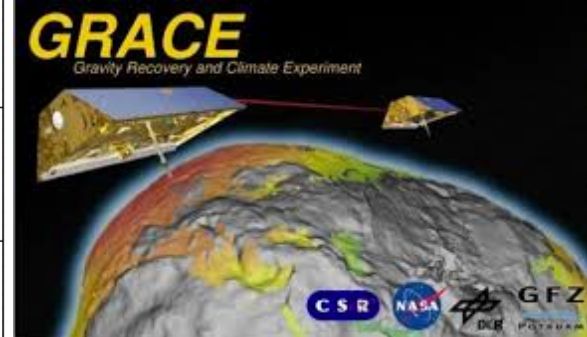
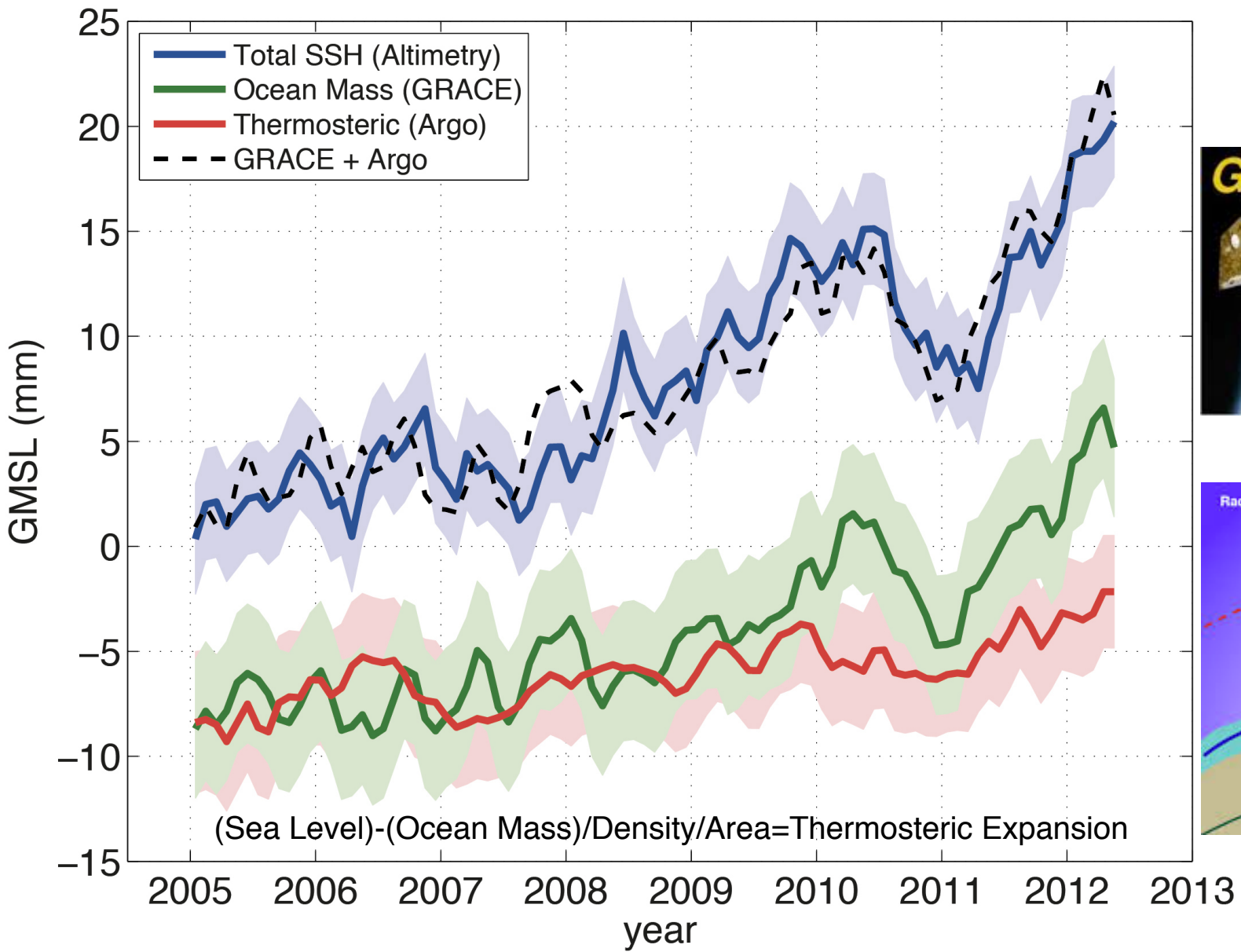
FIG. 6. As in Fig. 5 but for La Niña DIF

Climate: What is important?

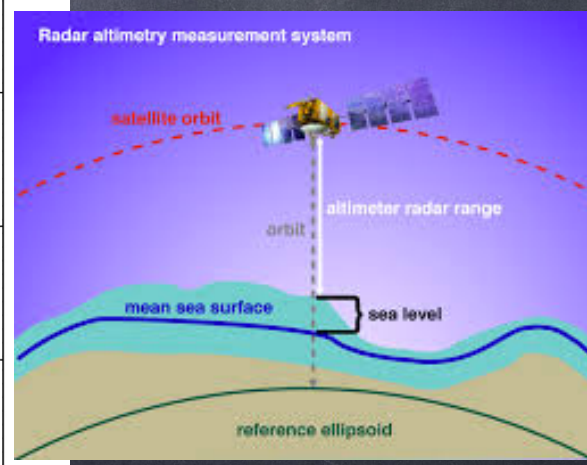


- To approximate absorption, reemission, and redistribution of the Sun's energy across the globe
- Need atmospheric, biological, & geological chemistry (greenhouse gasses) & clouds for absorption & reemission
- Need atmospheric & oceanic motions to redistribute
- Important motions are structured (cells, gyres, modes) and turbulent (weather, eddies, storms)
- Oceans are the relevant energy reservoir
- On longer timescales, changes to the lithosphere affect the cells, gyres, & modes.

Another reason to care about ocean warming—and to observe it (by subtraction): Sea Level Rise



podaac.jpl.nasa.gov



nesdis.noaa.gov