1	Evaluating Coupled Climate Model Parameterizations via Skill at
2	Reproducing the Monsoon Intraseasonal Oscillation
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ABSTRACT

Empirically generated indices are used to evaluate the skill of a global cli-15 mate model in representing the monsoon intraseasonal oscillation (MISO). 16 This work adapts the method of Suhas et al. (2013), an extended empirical or-17 thogonal function (EEOF) analysis of daily rainfall data with the first orthog-18 onal function indicating MISO strength and phase. This method is applied to 19 observed rainfall and Community Earth System Model (CESM1.2) simulation 20 results. Variants of the CESM1.2 including upper ocean parameterizations for 21 Langmuir turbulence and submesoscale mixed layer eddy restratification are 22 used together with the EEOF analysis to explore sensitivity of the MISO to 23 global upper ocean process representations. The skill with which the model 24 variants recreate the MISO strength and persistence is evaluated versus the 25 observed MISO. While all model versions reproduce the northward rainfall 26 propagation traditionally associated the MISO, a version including both Lang-27 muir turbulence and submesoscale restratification parameterizations provides 28 the most accurate simulations of the time scale of MISO events. 29

30 1. Introduction

Variability in the Indian monsoon on multiple time scales have been an area of intense research due to its significant societal and economic importance to the subcontinent and Indian Ocean periphery. Variations both year to year (interannual) and over the course of a single season (intraseasonal/subseasonal) are much harder to predict, and have been a topic of significant interest to researchers (Goswami et al. 2016; Kuppam and Mawsynram 2019). For the purposes of predictive skill, interannual and intraseasonal variability appear to be distinct phenomena, allowing—perhaps requiring—weather models to account for them separately (Krishnamurthy and Shukla 2000).

One primary mode of variability is the Indian monsoon intraseasonal oscillation (MISO), which 38 causes brief periods of especially intense rainfall during the Asian monsoon on the Indian subcon-39 tinent and over the Bay of Bengal. At the most basic level, the MISO is defined as a deviation 40 from the seasonal monsoon rainfall trend, which gradually increases over the course of the sum-41 mer, peaks around late July, then decreases to its off-season intensity (Krishnamurti and Ardanuy 42 1980). This is generated in part by the annual north-south movement of the monsoonal intertropi-43 cal convergence zone (Goswami and Mohan 2001). As a result, MISO events occur in an extremely 44 complex circulation context, making them difficult to predict more than a few weeks in advance 45 (Mo 2001). Nonetheless, they exhibit a northward propagation and some predictability, and they 46 can be isolated using the empirical pattern recognition techniques of Suhas et al. (2013) as shown 47 in Fig. 1. The MISO has significant marine influences and impacts, involving ocean-atmosphere 48 heat and freshwater exchange, and is extremely dependent on the particular geometry and physical 49 characteristics of the Bay of Bengal (Goswami et al. 2016). Li et al. (2016b, 2018) demonstrate 50 important mixed layer-related biases in the simulations of the Bay of Bengal in the Coupled Fore-51

⁵² cast System (CFSv2), and speculate that improving mixed layer physical process representation
 ⁵³ may help. The Indian monsoon is a known source of error in CMIP5 models (Li et al. 2015).

Previous work has looked at the relationship between the interannual and intraseasonal variations 54 in the Indian monsoon. Goswami and Mohan (2001) found that while the two behaviors act on 55 different time scales, they are not independent phenomena. Since they exhibit similar spatial 56 patterns, the interannual variation in monsoons can be viewed as an anomaly in intraseasonal (i.e., 57 MISO) activity. The authors inferred that the chaotic nature of intraseasonal oscillations therefore 58 spelled defeat for researchers trying to predict year-to-year monsoon trends. Empirical methods 59 offer a way to circumvent this limitation by isolating modes of variation in chaotic data, and here 60 they are extended to use in model evaluation. Through this combination of models and pattern 61 recognition, skill in reproducing the MISO statistics can be assessed, which in turn may be used 62 to improve forecast systems. 63

Not only are MISOs important to the intensity of the monsoon overall, but positive oscillation 64 phases (indicated by red shading of the timeseries in Fig. 1 upper panel) have been shown to be 65 correlated with a greater frequency of tropical cyclones forming in the Bay of Bengal (Akter and 66 Tsuboki 2014). Moreover, those storms associated with a positive MISO phase tend to form at a 67 central point in the northern Bay of Bengal and travel northwest across India, steered by the low 68 pressure border known as the monsoon trough. The place where the storms form is a relatively 69 small region associated with the point of greatest MISO variation in the Bay, meaning that the 70 movement and change of the MISO over time may affect the origin and path of weather events in 71 that region of the subcontinent (Goswami et al. 2003). A key result here is that the connectivity of 72 rainfall over the subcontinent to the MISO variability over the Bay of Bengal is sensitive to upper 73 ocean physics in a coupled model. Additionally, the Bay is particularly important as MISOs form 74 in the Indian Ocean to the south and move northward, and previous studies have found a zone 75

⁷⁶ of peak variation to be centered on the bay (Goswami et al. 2003; Goswami and Xavier 2003;
⁷⁷ Sengupta et al. 2001).

The Community Earth System Model version 1.2 (CESM1.2: Hurrell et al. 2013) is a global 78 coupled modeling system. The particular variants being used for this study use the standard at-79 mosphere, sea ice, and land components, but differ in key ocean model parameterizations (Table 80 1). The goal in studying the MISO in these configurations was to determine if its statistics are 81 sensitive to the upper ocean physics (as shown with less direct attribution to specific upper ocean 82 processes in Li et al. 2016b, 2018; Samanta et al. 2018; Zhang et al. 2018), and whether op-83 timization of these physical parameterizations might usefully improve skill in coupled forecast 84 systems (e.g., Pattanaik et al. 2012). The specific upper ocean physical processes being evaluated 85 are wave-induced mixing, or Langmuir turbulence, as parameterized by Li et al. (2016a) and sub-86 mesoscale mixed layer eddy restratification as parameterized by Fox-Kemper et al. (2008, 2011). 87 As of CESM1.2 the submesoscale parameterization is standard, but the Langmuir turbulence pa-88 rameterization, built upon the KPP scheme (Large et al. 1994), was only included as a default 89 setting in CESM2 (Danabasoglu et al. 2020). The CESM1.2 variants being evaluated here are 90 prototypes including both parameterizations that preceded CESM2, but are similar in terms of the 91 ocean model setup. 92

The potential importance of oceanic processes in the Bay of Bengal in setting the phasing and intensity of the MISO has been shown recently in closely related studies. Zhang et al. (2018) found a quadrature relationship between SST and precipitation in smoothed observations, indicating that these two quantities share a relationship which they presume involves warm SSTs triggering atmospheric convection. This study highlights a potential role for sea surface temperature–and the ocean mixing and restratification processes that affect it–in the phasing of monsoon active cycles. Additionally, in an atmospheric model-ocean mixed layer forecast system, the geographic distribution of mixed layer depth (held constant in time) was shown to improve forecast skill by Samanta
 et al. (2018), therefore processes affecting spatial distributions of mixed layer depth are likewise
 linked to monsoon dynamics. Therefore it is reasonable to hypothesize that processes that impact
 boundary layer turbulence temporally and spatially will influence monsoon variability.

Upper ocean mixing in the Bay of Bengal is set by processes that inhibit mixing, such as 104 buoyancy input from warming and freshwater fluxes, and those that enhance mixing such as wind 105 driven mixing or convection. In addition to surface forcing at the air-sea interface, other processes 106 are known to be leading order at influencing upper ocean turbulence. In particular, this work 107 focuses on the restratifying effects of submesoscale baroclinic instability and enhanced mixing 108 due to Langmuir circulation and turbulence, a variety of mixing that derives some of its energy 109 from surface waves (McWilliams et al. 1997; Li et al. 2019). Submesoscale restratification plays 110 an essential role in the upper ocean buoyancy budget where there are strong horizontal density 111 gradients. Large freshwater input into the Bay of Bengal from river runoff (e.g., from the Brama-112 putra River) is stirred into the interior of the bay and creates sharp buoyancy fronts and filaments 113 (MacKinnon et al. 2016; Ramachandran et al. 2018; Spiro Jaeger and Mahadevan 2018; Sarkar 114 et al. 2016). Instabilities that occur at submesoscale fronts act to slump horizontal buoyancy gra-115 dients to create vertical stratification and inhibit upper ocean mixing (Boccaletti et al. 2007; Fox-116 Kemper et al. 2008). Conversely, Langmuir turbulence results from wind-wave interaction which 117 creates parallel rotating cells $\sim 10^1$ m deep and is known to enhance turbulence in the ocean sur-118 face boundary layer (Langmuir 1938; Leibovich 1983; McWilliams et al. 1997; McWilliams and 119 Sullivan 2000; Li et al. 2019). The shoaling/deepening effects of these processes have been pa-120 rameterized for coarse-resolution models such as global circulation models and coupled weather 121 forecast models that cannot simulate these processes directly. 122

Previous studies have defined MISOs using a variety of indices, including atmospheric vorticity at 850 hPa (Goswami et al. 2003), zonal wind (Goswami and Mohan 2001), and sea surface temperature at a stationary buoy (Sengupta et al. 2001). These choices reflected authors' assumptions about MISO dynamics; for instance, Goswami and Mohan (2001)'s use of zonal wind in the Bay of Bengal as a metric reflected their view that MISOs were an expression of breaks in the prevailing monsoon winds.

The methodology presented here is different in two ways. First, it uses rainfall data, meaning 129 MISOs are measured by their effects, not their causes, insulating the analysis from discussions 130 of the mechanisms of individual MISO phases. While increased rainfall alone does not define a 131 MISO, it is a well-established relationship (and the most impactful on human activity). Second, 132 this work expands on the technique of Suhas et al. (2013), using an extended empirical orthogonal 133 function (EEOF) analysis to identify the oscillatory signal of the MISO rainfall data. Empiri-134 cal orthogonal function (EOF) analysis decomposes complex data sets into their primary modes 135 of variability, revealing which geographic and temporal patterns are most significant to the over-136 all variability (Thomson and Emery 2001). This allows spatially-stationary oscillatory patterns 137 (e.g., standing waves) to be revealed (Fox-Kemper 2004). Extended empirical orthogonal function 138 (EEOF) analysis takes this a step further, using in this case multiple snapshots over a short time 139 window as the "pattern" being recognized constructed to reveal propagating modes of variability 140 (Eshel 2012; Weare and Nasstrom 1982). The EEOFs tend to isolate the northward propagation 141 characteristic of the classical MISO phase progression (Suhas et al. 2013). 142

This work will use an EEOF methodology to isolate MISO events and compare different formulations of upper ocean parameterizations within CESM with observations. The comparison provides insight into how much of a difference upper ocean processes have on MISO events, as well as more generally how well the CESM1.2 simulates the MISO. CESM is a climate rather than

a weather forecast model, so the issue of model skill is focused on the model's ability to simulate
a realistic MISO with reasonable magnitude and recurrence, rather than its ability to produce good
forecasts from observed initial conditions. However, as the National Center for Environmental
Predictions (NCEP) Coupled Forecast System (CFS) is often used in this region shares significant code and capabilities with the CESM, implications for what constitutes a skillful CESM is
expected to resemble what constitutes a skillful CFS.

153 2. Methods

154 a. Observational Data

¹⁵⁵ Following Suhas et al. (2013), the observational data set used for model comparison is the Global ¹⁵⁶ Precipitation Climatology Project (GPCP), a reanalysis based on both satellite and historical ob-¹⁵⁷ servations (Huffman et al. 1997; Adler et al. 2003; Huffman et al. 2009). This data set in 1×1 ¹⁵⁸ degree resolution was obtained for Oct. 1, 1996 to Sept. 30, 2015. This data was regridded onto ¹⁵⁹ the 1.9×2.5 grid of the CESM atmospheric model for comparison.

160 *b.* CESM

This work uses the the National Center for Atmospheric Research (NCAR) Community Earth 161 System Model, version 1.2 (CESM1.2). Previously, CESMv1 was found to have the smallest bias 162 in simulating the monsoon compared to other CMIP5 models (Anand et al. 2018). The model con-163 figuration includes a fully coupled atmosphere (CAM4) and land (CLM4.0) on a 1.9×2.5 degree 164 nominal grid, and ocean (POP2) along with sea-ice (CICE4) on the gx1 version 6 grid (1 degree 165 nominal resolution), and waves (WAVEWATCH III v3.14) on a coarser grid (Li et al. 2016a). The 166 model is run for 100 years with steady preindustrial conditions. This analysis uses the last 30 years 167 of integration after which the model is assumed to be sufficiently equilibrated in the upper ocean, 168

as mixed layer depths are stable when different decades at the end of the simulation are compared. Boundary layer turbulence is parameterized using the K-profile parameterization (KPP) mixing scheme (Large et al. 1994), and the additional effects of restratification by submesoscale mixed layer eddies (Fox-Kemper et al. 2011) and enhanced vertical mixing through Langmuir turbulence (Li et al. 2016a) can be switched on or off. The different simulations for comparison are all forced with the same conditions and from the same initial conditions, they differ only in this aspect (Table 1).

The effects of submesoscale baroclinic instability is parameterized as an overturning streamfunction (Fox-Kemper et al. 2008, 2011),

$$\Psi_o = \frac{\Delta s}{L_f} C_e \frac{H^2 \nabla_h b \times \hat{\mathbf{z}}}{|f|} \mu(z) \tag{1}$$

$$\mu(z) = \left[1 - \left(\frac{2z}{H} + 1\right)^2\right] \left[1 + \frac{5}{21}\left(\frac{2z}{H} + 1\right)^2\right]$$
(2)

Where C_e is a constant set to 0.06, H is mixed layer depth as determined by a density difference 178 from the surface, b is the buoyancy formed from the density ρ and background density ρ_0 by b =179 $g(\rho_0 - \rho)/\rho_0$, $\nabla_h b$ is the grid scale horizontal buoyancy gradient and the factor $\Delta s/L_f$ includes the 180 horizontal grid scale and a frontal scaling factor that accounts for the course horizontal resolution 181 of the model (Fox-Kemper et al. 2011). The typical effect of this parameterization is to shoal 182 the mixed layer by overturning lateral fronts wherever they are present to increase the vertical 183 stratification, at a rate consistent with simulations and observations of mixed layer eddy processes. 184 The Langmuir turbulence parameterization developed by Li et al. (2016a) accounts for the ad-185 ditional vertical boundary layer mixing that occurs when Stokes drift from surface waves (which 186 is extracted from the WaveWatch III component model across the globe and depends on the winds 187 and ocean currents of the other model components) interacts with near-surface boundary layer 188 turbulence resulting in downward accelerations by a wave-current interaction called the Stokes 189

¹⁹⁰ shear force (Suzuki and Fox-Kemper 2016). The rate of additional mixing beyond wind-driven ¹⁹¹ mixing is estimated in Large Eddy Simulations resolving Langmuir turbulence (Van Roekel et al. ¹⁹² 2012) and included in KPP following the parameterization form suggested by McWilliams and ¹⁹³ Sullivan (2000). The parameterization mostly increases the vertical turbulent velocity scale within ¹⁹⁴ the boundary layer by an enhancment factor \mathscr{E} :

$$W = \frac{ku^*}{\phi} \to W = \frac{ku^*}{\phi} \mathscr{E},\tag{3}$$

$$\mathscr{E} = |\cos\alpha| \sqrt{1 + (c_1 L a)^{-2} + (c_2 L a)^{-4}}$$
(4)

The angle α is the predicted angle between the Langmuir cell orientation and the surface wind orientation, $c_1 = 1.5, c_2 = 5.4$ are dimensionless constants, and *La* is the surface layer-averaged, turbulent Langmuir number formed from projecting both the wind stress and Stokes drift into the Langmuir cell orientation (Van Roekel et al. 2012; Li et al. 2016a), or

$$La = \sqrt{\frac{u^* \cos \alpha}{|\langle u_s \rangle| \cos(\theta_{ww} - \alpha)}}$$
(5)

¹⁹⁹ Here θ_{ww} is the angle between the wind and the wave direction, $\langle u_s \rangle$ is the Stokes drift averaged ²⁰⁰ over the surface layer –i.e., the upper 20% of the mixed layer (Harcourt and DAsaro 2008)–and ²⁰¹ α is found from application of the Law of the Wall as derived in Van Roekel et al. (2012). The ²⁰² additional effects of Langmuir mixing on entrainment at the mixed layer base (Li and Fox-Kemper ²⁰³ 2017) were not used for this study.

In summary, the submesoscale restratification depends on the horizontal buoyancy gradient and mixed layer depth and acts to shoal the ML. Conversely, Langmuir turbulence depends on waves and wind direction and strength, and acts to deepen the mixed layer. The combinations of paramterizations and cases are outlined in Table 1. These parameterizations rely on different resolved variables and therefore have different temporal and geographical influences over the Bay of Bengal and globally. It should be noted that both of these parameterizations are the default in CESM2 ²¹⁰ (Danabasoglu et al. 2020), so the sensitivity under study is the effect of turning each of or both of ²¹¹ them off.

Each model with its own parameterization set was initialized identically for 30-year runs. For analysis of the MISO, the annual mean and first three harmonics of the precipitation fields were removed, so that only sub-seasonal precipitation anomaly variations were retained. Then, a zonal average of precipitation data between 12.5S–30.5N and 60.5–95.5E isolated the region of interest. This choice has the advantage of eliminating any topography from the analysis region.

217 c. EEOF Analysis

Empirical orthogonal functions (EOFs) are an application of singular value decomposition (SVD) which treats the decomposed values as representations of the temporal and spatial variability of a data set (Thomson and Emery 2001). The following equation shows the archetypal SVD in matrix notation,

$$\mathbf{M} = \mathbf{U}\mathbf{S}\mathbf{V}^{T} \tag{6}$$

where \mathbf{M} is a spatiotemporal data set organized with rows and columns as spatial grid locations and 222 time steps, **U** and **V** are its left and right singular vectors, and **S** is the matrix of singular values. **V** is 223 a square matrix with the same dimensions as the spatial grid of the original data matrix and each of 224 its columns is a normalized pattern or mode of spatial variability that repeats in the anomaly data. 225 The different patterns are guaranteed to be orthogonal. The left matrix \mathbf{U} is a square matrix the size 226 of the number of time steps in the data matrix, and each of its columns captures the normalized time 227 series of each corresponding spatial mode, respectively. The time series are also orthogonal. S is a 228 diagonal matrix capturing the amplitude and relative importance of each mode, typically ordered 229 from the largest amplitude to the smallest. Note that orthonormality of U and V implies that the 230 sum of the diagonals of S^2 equals that of the original data matrix times its transpose, indicating 231

that the spatiotemporal variance explained by each mode is captured by the corresponding singular value squared. The fraction of the variance represented by a particular mode is captured by the corresponding diagonal element squared divided by the sum of the squares of all of the diagonal elements of **S**. Similarly, (6) implies that the original data can be reconstructed from **U**,**S**,**V**, or approximated by retaining only a limited number of modes with the largest entry on the diagonal of **S**.

A temporal extended EOF (EEOF) involves expanding the original **M** matrix by concatenating 238 a duplicate of the data set which is offset (or "lagged") in time. Thus, the lagged data follows 239 the same form as (6) has for a dataset with more spatial grid points. By simultaneously perform-240 ing EOF analysis on the same data from slightly different starting times, a mode in a temporal 241 EEOF captures not a single spatial pattern, but a sequential pattern of two consecutive days of 242 evolving features (Weare and Nasstrom 1982). Here, an EEOF with lags ranging from 1-16 days 243 (17 total days) is used to recognize patterns in the short-term evolution of the precipitation-i.e., 244 the range of time expected for the MISO development. Terminology for EOFs and EEOFs varies 245 widely:extended empirical orthogonal functions with a number indicating their relative importance 246 in terms of the corresponding **S** entry (e.g., EEOF1, EEOF2) and the time series describing the 247 evolving amplitude of each set of lagged patterns are called principal components again numbered 248 by importance (e.g. PC1, PC2). If the **S** values are all distinct, then each EEOF and PC are unique 249 and distinct. 250

EOF analysis in general is purely statistical and lacks dynamical cause-and-effect (Dommenget and Latif 2002), so the decomposed modes may not have any physical significance unless independently shown to do so. EOFs may produce apparent order in data beyond what is present. EOF analysis is particularly troubling if the real modes of variability are not orthogonal in time or space. EOF analysis can also be confusing when representing propagating patterns (Fox-Kemper ²⁵⁶ 2004), but the EEOF approach makes rapidly propagating patterns simple to describe with a sin-²⁵⁷ gle EEOF. In this case, the MISO is well understood to be a north-south phenomenon, making it ²⁵⁸ more natural to apply an EEOF method than in the case of, for instance, a spatial data set with ²⁵⁹ no a priori assumptions about modes of variability. The method is not being used here to identify ²⁶⁰ unseen patterns but to evaluate one already identified.

As shown by Suhas et al. (2013) the EEOFs produced in this manner agree with other indices 261 of MISO variability. Fig. 1 shows the variation in PC1 over a few positive and negative phases 262 of EEOF1, and the corresponding zonal-mean precipitation over the region below. It is clear 263 that the northward-propagating precipitation pattern is captured by the PC1 time series, and the 264 EEOF spatial pattern of propagation similarly matches the precipitation propagation (not shown). 265 Following Suhas et al. (2013), EEOF1 and EEOF2 are normalized by their standard deviations, 266 and are hereafter referred to as MISO1 and MISO2. For the purposes of this work, MISO maxima 267 and minima are identified here as peaks and troughs in MISO1 (delineated by the 5th and 95th 268 percentiles over the whole record). Other EOF-based definitions are common, e.g., for evaluating 269 the Madden-Julian Oscillation (such as Kim and North 1999) or other climate variability signals 270 (Weiss et al. 2019). In this case, MISO1 isolates the primary north-south mode of oscillation. 271 The meaning of the PCA1 appears clearly by plotting MISO1 alongside zonal precipitation 272

(Figure 1). The precipitation data show clear northward-moving phenomena associated with peaks
and valleys in PC1.

275 *d. Composite Maps*

²⁷⁶ Composite maps of the difference in regional rainfall anomaly between active and break phases ²⁷⁷ of the MISO are a complementary metric to the MISO1 pattern once the maximum and minimum ²⁷⁸ MISO stages are found (Fig. 2). While the EEOF is formulated based only on rainfall in the Bay of Bengal, composite plots of these time periods show a wider region, illustrating how the MISO phases defined by the EEOF manifest in the Indian Ocean as a whole. Furthermore, the composite precipitation averages are not limited by orthogonality of spatial patterns, or the fact that the linear construction of the EEOFs ensures symmetries that may not be present: e.g., EEOF1 in a positive phase is exactly the same as the negative of EEOF1 in a negative phase. Fig. 3 illustrates that the composites over positive and negative phases indeed differ in spatial pattern.

3. Results and Discussion

Solely matching the timescale of simulated MISO phenomenon identified by the EEOF analysis to that previously observed for the MISO does not indicate a complete model success, but together with a good spatial structure of the EEOFs and the patterns of the composite maps (Figure 2) alternative mechanisms become increasingly unlikely. The short lag interval (1-16 days) chosen for EEOF-based MISO detection is insufficient to cover a full repetition of a MISO event followed by another, but it does capture the characteristic northward trend of the precipitation maximum within an individual event (Figure 1).

The composite maps (Figure 2) of the difference in precipitation anomaly between MISO posi-293 tive and negative phase peaks (MISO1 maxima and minima) show clear regions of strong variabil-294 ity throughout the Bay of Bengal and the surrounding region. The GPCP data has a strong positive 295 center stretching from the Bay of Bengal across India to the Arabian Sea. Closer to the equator, 296 there is a diffuse precipitation minimum during the MISO positive phase. These precipitation pat-297 terns are not an input to the detection algorithm for EEOF1, but are consistently correlated with it. 298 The models do a fair job of capturing the Bay of Bengal center of activity, but tend to either over-299 estimate the precipitation anomaly over Indonesia or underestimate the precipitation anomaly over 300 western India. None of them show a positive anomaly region stretching as far west as in the GPCP 301

data. Conversely, in all of the models, the opposing precipitation anomaly near the equator is too strong compared to the observations. Overall, the CESM control run including both Langmuir and mixed layer eddy parameterizations tends to have the closest pattern to the GPCP observations.

The EEOFs for all of the data sets have very broad singular value distributions, meaning the first 305 few EEOFs account for only a modest portion of the variance which captures many other sources 306 of precipitation variability. In GPCP, the first two EEOFs explain 9.80% and 8.97% of the total 307 variance respectively. For the CESM control run with both Langmuir and submesoscale turbu-308 lence, the first two EEOFs explain 7.83% and 6.87% of the variance. Removing Langmuir turbu-309 lence leaves 7.73% and 6.24%, while removing submesoscale turbulence gives a greater spread of 310 7.86% and 6.03%. Removing both gives 8.01% and 6.89% (Figure 4). Thus, the MISO is stronger 311 as a fraction of total precipitation variance in the real world than in the simulations, which tend 312 to spread precipitation variance more evenly among modes. In absolute terms, the first 2 singular 313 values for all CESM versions are weaker than those for GPCP data, consistent with the MISO1 314 index accounting for more of the variation in the observations than in the model runs. 315

Active, or positive, MISO period identified in observations by the EEOF method have an average 316 period of 31 days (Figure 5 top row), which is consistent with previous descriptions of the MISO 317 as approximately 30-60 days long (Goswami et al. 2016). This recurrence time exceeds the lag 318 interval used to formulate the EEOF. The control model version exhibits the most similar behavior, 319 with active periods on average 37 days long. The two model versions without Langmuir turbulence 320 show the greatest difference difference from the observations: the noLT version has active phases 321 on average 52 days long, while the noLTSM version has 123 days. This trend is similarly evident 322 in the distribution of negative MISO phases (right column). Note the difference in sample size 323 caused by the longer time span of the model runs. 324

Figure 6 shows that while the CESM simulations including parameterizations of mixed layer 325 eddies and Langmuir turbulence do have the most similar MISO statistics to the GPCP, the mixed 326 layer depth in the Bay of Bengal, and the north-south gradient of mixed layer depth differ signif-327 icantly from an observations for this simulation, here drawn from the Monthly Isopycnal Mixed 328 Layer Climatology (MIMOC, Schmidtko et al. (2013)). The definition of mixed layer used in the 329 CESM and in MIMOC is consistent, so the distinctions are not semantic. MIMOC has shallower 330 mixed layer depths, and less seasonal variation in mixed layer depth than CESM. Furthermore, 331 the simulation that performs best in the MISO (mixed layer eddies and Langmuir mixing: yellow 332 line) does *not* have the mixed layer depth closest to observations. This comparison of mixed layer 333 depths indicates that 1) the CESM can still be improved, and 2) under the coarse vertical resolution 334 and numerics of the CESM a "good" mixed layer depth may not select for the best MISO variabil-335 ity, and 3) there are likely other model biases (e.g., clouds, precipitation, or atmospheric boundary 336 layer parameterizations) that are providing additional errors beyond those being assessed here by 337 altering the upper ocean parameterizations. Alternatively, it is possible that it is changes to the 338 mixed layer *outside* of the Bay of Bengal that are having a beneficial effect on dynamics within 339 the bay-an issue that cannot be addressed with the global model design used here. Thus, a variety 340 of diagnostics, such as the method of Suhas et al. (2013) chosen here, are needed to fully assess 341 the MISO and models' ability to predict it. 342

4. Conclusions

The EEOF method of Suhas et al. (2013) captures local modes of variability like the MISO. In this analysis, the MISO statistics are significantly sensitive to upper ocean parameterizations, here Langmuir turbulence and mixed layer eddy parameterizations, even when all other aspects of the model are unchanged. Thus, upper ocean physics nontrivially impacts the MISO. The upper ocean turbulence plays a large role in ocean-atmosphere interactions and the MISO is an inherently marine weather phenomena. However, most numerical weather prediction system analyses tend to focus on simulation of sea surface temperature, not mixed layer depth. The models here differ in both SST anomaly statistics and mixed layer depth, but these are not easily separated as both effects stem from substituting among self-consistent parameterizations. If solely the SST warming of submesoscale restratification was included without altering the mixed layer depth, it would not be physically meaningful.

The composite maps shown for CESM (Figure 2) show that it is not only persistence of the MISO phenomena that is affected by upper ocean physics, but also the spatial patterns can be made more or less realistic. The effects near the equator, where all of the simulations have too little coherent precipitation with the positive MISO phase, indicates that there are likely other biases to address, e.g., the double ITCZ bias (Zhang et al. 2019).

Interestingly, the Bay of Bengal mixed layer depths of the model most successful in simulating the MISO are not the most accurate in comparison to observations. Thus, the mechanisms at play in the model to simulate the MISO are different than those in the real world–a fact that is not surprising given the complexity of the cloud formations in a real MISO (Kumar et al. 2017) versus the simplified MISO in the CESM. It is not at all clear if the model improvements shown here are a vindication of the particular set of parameterizations chosen, or just a coincidental set of factors combining into an improved MISO.

³⁶⁷ What is clear however, is that the simulated MISO is sensitive to upper ocean physics that con-³⁶⁸ tributes to mixed layer balances, not just prescribed mixed layer depths (Samanta et al. 2018). ³⁶⁹ Furthermore, in this particular model, the most realistic MISO did not occur in the model with the ³⁷⁰ most accurate mixed layer depth, revealing that the whole of the model, including other inaccura-³⁷¹ cies, need to be taken into account when assessing forecast skill potential.

Methods like EEOF analysis can help identify such phenomena and define a rigorous way to 372 extract targeted skill tests from observations and climate models in such a way that they can be 373 directly compared. Measuring precipitation alone without the added perspective of the EEOF 374 framework significantly decreases the clarity of the connection between the upper ocean physics 375 and the MISO, since upper ocean physics also affects other aspects of the precipitation patterns 376 that conceal the MISO impact. On the other hand, EEOFs hold the potential to indicate modes of 377 oscillation where there may be none, so patterns and temporal progression and persistence need to 378 be evaluated as done here. 379

EOFs (and EEOFs) can also provide the basis for an empirical prediction system (Penland and Magorian 1993; Weiss et al. 2019) which can offer comparable forecast skill to full process-based modeling systems (Newman and Sardeshmukh 2017). Thus, the results here that upper ocean processes affect MISO EEOF statistics is likely to impart an impact on the potential forecast skill of process-based models.

The independence of EEOF analysis from model physics is both a strength and a weakness of the methodology. On the one hand, by making no assumptions about the dynamics of MISO events an EEOF can focus purely on their observed empirical behavior. Additionally, here we compound this agnosticism by using precipitation as our base variable, focusing on an effect of a MISO rather than a theorized mechanism. However, a more detailed look into the changing coupled air-sea mechanisms triggered by the different upper ocean physics is an important next step to better understand the nature of the sensitivity found here.

³⁹² Comparing versions of a GCM with and without various forms of turbulence has significant ³⁹³ value from the perspective of climate mechanisms and model physics. Since the precipitation ³⁹⁴ patterns associated with MISOs form in the Indian Ocean and move North through the Bay of ³⁹⁵ Bengal, this model comparison provides an opportunity to test how important ocean turbulence is

to such synoptic scale phenomena. However, as the perturbed physics in this CESM ensemble was 396 perturbed *globally*, it is not clear if the local effects on the upper Bay of Bengal was the key change, 397 or if other regions affected the initiation of the MISOs elsewhere, for example. The mismatch 398 between model MISO accuracy and Bay of Bengal mixed layer depths would be natural if the 399 improved skill descended from changes elsewhere rather than local changes. Using perturbed Bay 400 of Bengal physics in a regional climate model forced with identical remote forcing can distinguish 401 between the impacts of local and remote physics, as can better understanding of the perturbed 402 mechanisms underlying these changes to the MISO. 403

The importance of intraseasonal behavior to global climate predictions has become clear over the 404 last decade. The most significant mode of East-West tropical intraseasonal variation, the Madden-405 Julian oscillation (MJO), has been shown in GCMs to nearly double in simulations with quadru-406 pled atmospheric CO₂ levels. The precipitation anomalies associated with the MJO are projected 407 to increase by 10% with every degree C of surface temperature warming, partly due to increases 408 in surface heat flux, but primarily due to a significant increase in vertical atmospheric circulation 409 (Arnold et al. 2015). Since MISOs exhibit a similar mechanism, their response to climate change 410 should be studied once a climate model is vetted for adequacy. 411

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⁴¹⁹ Isopycnal Mixed Layer Climatology (MIMOC, Schmidtko et al. (2013)) may be accessed at ⁴²⁰ http://www.pmel.noaa.gov/mimoc/.

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	KPP	Langmuir	Submesoscale
CTRL	x	Х	x
noLT	x		х
noSM	x	Х	
noLTSM	x		

TABLE 1. List of CESM case studies used in this study.

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FIG. 1. Example of EEOF index method for Summer 2007 observed precipitation. EEOF1 index (top) is calculated from zonally averaged precipitation data (bottom) using method described in Section 2c. Diagonal areas of high precipitation correspond to northward-propagating rain bands, which in turn correspond to periods of positive EEOF1 (portions of the top plot in red).



FIG. 2. Average difference in precipitation anomaly between positive and negative MISO1 phases. Maps show the difference between the average precipitation anomalies at all times for MISO1 > 95th percentile and all times for MISO1 < 5th percentile for the observations (top plot - GPCP) and for the cases (Table 1): CTRL = both Langmuir and submesoscale, noLT = submesoscale only, noSM = Langmuir only, noLTSM = neither parameterization, and GPCP = observations.



FIG. 3. Average positive and negative precipitation phases. Maps show the average precipitation anomalies at all times for MISO1 > 95th percentile (top row) and all times for MISO1 < 5th percentile (bottom row). Shown are the cases (Table 1): CTRL = both Langmuir and submesoscale, noLT = submesoscale only, noSM = Langmuir only, noLTSM = neither parameterization



FIG. 4. Comparison of the relative importance of the first 10 EEOFs for GPCP observations and all model 646 configurations. Method for calculating the percent of variance explained by each EEOF discussed in text. The 647 first EEOF value corresponds to the percent variance represented by the MISO1 index. From Baylor: EEOF 648 1 and 2 of CESM represent a smaller fraction of the total variance when compared to EEOF 1 and 2 of the 649 observations, but the precipitation variance in CESM is higher in (mm/day)², which may mean that the rainfall 650 anomalies explained by EEOFs 1 and 2 of CESM matches that of the observations. Shown are the cases (Table 651 1): CTRL = both Langmuir and submesoscale, noLT = submesoscale only, noSM = Langmuir only, noLTSM = 652 neither parameterization, and GPCP = observations. 653



FIG. 5. Distribution of length in days of positive (left column) and negative (right column) phases of the MISO1 index for GPCP observations and all model configurations. Shown are the cases (Table 1): CTRL both Langmuir and submesoscale, noLT = submesoscale only, noSM = Langmuir only, noLTSM = neither parameterization, and GPCP = observations.



FIG. 6. Monthly climatology of spatially averaged mixed layer depth (MLD) in the Bay of Bengal from observations and for each model configuration. Observational data set from the Monthly Isopycnal & Mixedlayer Ocean Climatology (MIMOC) (Schmidtko et al. 2013)