# Mixed Layer Restratification 

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Collaborators:
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WHOI PO Seminar Tuesday 2/27/07, 15:00-16:00

## Upper Ocean in Climate Models

- Large-scale ocean circulation $(100-10,000 \mathrm{~km})=>$ resolved
- Submesoscale variability $(100 \mathrm{~m}-10 \mathrm{~km})=>$ ignored
- Turbulent mixing $(10 \mathrm{~cm}-100 \mathrm{~m}) \Rightarrow$ parameterized



## Upper Ocean in Climate Models

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## Ocean Mixed Layer



Pot'I Density measured by a Seasoar along a straight section from ( $32.5 \mathrm{~N}, 122 \mathrm{~W}$ ) to (35N, 132W) between the CA current and the subtropical gyre. (as in Ferrari \& Rudnick, 2000)

1) What does its stratification imply?
2) How does the stratification get set? 3) Why do we care?

The Stratification Permits
Two Types of Baroclinic Instability:

## and SubMesoscale (Boccaletti et al., 2006)



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> Mesoscale and
> SubMesoscale are Coupled Together:

ML Fronts are formed by

Straining.
Submesoscale eddies remove PE from those fronts.


## Observed:

## Strongest Surface Eddies= Spirals on the Sea?



Figure 1. A pair of interconnected spirals in the Mediterranean Sea south of Crete. This vortex pair has a clearly visible stagnation point between the two spirals, the cores of which are aligned with the preconditioning wind field. 7 October 1984.


Figure 12: Probability density function of relative vorticity divided by Coriolis parameter. (a) Results from the numerical simulation of a slumping horizontal density front. ( $z>100$ only to exclude bottom Ekman layer.) The PDF is estimated using surface velocity measurements at day 25 (see also Fig. 11). A positive skewness appears as soon as the baroclinic instability enters in the nonlinear stage, and it continues to grow. Note that the peak at $\zeta / f=0$ is due to the model's initial resting condition; that fluid has not yet been contacted by the MLI. (b) Results from ADCP measurements in the North Pacific. The PDF is calculated in bins of width 0.02.

## Observed:

ML Density varies in horizontal, only at scales larger than ML Def. Rad.

## $S$ \& $T$ vary at all scales.



Midlatitude Pacific near Hawaii: Hosegood et al. 06

## Vertical fluxes are Submesoscale and tend to restratify



Figure 1: Contours of temperature at the a) surface and b) below the mixed layer base in a simulation with both mesoscale eddies and MLEs $\left(0.2^{\circ} C\right.$ contour intervals). Shading indicates the value at the depth where $\overline{w^{\prime} b^{\prime}}$ (upper panel) and $\left|\overline{\mathbf{u}_{H}^{\prime} b^{\prime}}\right|$ (lower panel) take the largest magnitude.

## Horizontal fluxes are Mesoscale and tend to stir

## Having a Mixed Layer Counts!

## The vertical buoyancy flux in the ML ( $\left\langle w^{\prime} b^{\prime}\right\rangle$ )

## without diurnal cycle is

 than with cycle (ML)

Temperature Section along Channel Center




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Temperature Section along Channel Center




- 1.5 days, 5-6 Aug 2006
- Mixed layer restratifies under weakening wind forcing
- Characterized mixed layer evolution in Lagrangian (floatfollowing) frame.


## AESOP Observations

of Rapid Restratification near Monterey Bay


After one day


10 kt wind

## Prototype: Mixed Layer Front Adjustment



Note: initial geostrophic adjustment overwhelmed by eddy restratification

## Schematic of the overturning


R.W. Houghton et al. / Progress in Oceanography 70 (2006) 289-312

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## Parameterization of Finite Amp. Eddies: Ingredients



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## Eddies at Finite

 Amplitude
## Parameterization of Finite Amp. Eddies: Ingredients



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## Power Spectrum of KE

Eddies at Finite Amplitude

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At Finite Amplitude Horizontal Scale Unclear


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## Magnitude Analysis: Vert. Fluxes

Extraction of potential energy by submesoscale eddies:

$$
-\langle w b\rangle=\frac{\partial\langle P E\rangle}{\partial t} \approx \frac{\Delta P E}{\Delta t} \propto \frac{\Delta z \Delta b}{\Delta t}
$$



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\langle w b\rangle \propto \frac{\Delta z \Delta y \frac{\partial \bar{b}}{\partial v}}{\Delta t}
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$$
\langle w b\rangle \propto \frac{\Delta z \Delta y \frac{\partial \bar{b}}{\partial y}}{\Delta y / V}
$$

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$$
\langle w b\rangle \propto \frac{\Delta z H}{|f|}\left[\frac{\partial \bar{b}}{\partial y}\right]^{2}
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$$
\langle w b\rangle \propto \frac{H^{2}}{|f|}\left[\frac{\partial \bar{b}}{\partial y}\right]^{2}
$$

Eddies effect a largely adiabatic transfer: thus representable by a streamfunction

$$
\Psi \propto \frac{H^{2} \nabla \bar{b} \times \hat{\mathbf{z}}}{|f|} \longrightarrow \overline{\mathbf{u}^{\prime} b^{\prime}} \equiv \boldsymbol{\Psi} \times \nabla \bar{b}
$$

$$
\begin{aligned}
& \overline{w^{\prime} b^{\prime}} \propto \frac{H^{2}}{|f|}\left|\nabla_{H} \bar{b}\right|^{2} \\
& \overline{\mathbf{u}^{\prime} b^{b^{\prime}}} \propto \frac{-H^{2} \frac{\partial \bar{b}}{\partial b}}{|f|} \nabla_{H} \bar{b}
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For a consistently upward,

$$
\begin{gathered}
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For a consistently upward,

$$
\overline{w^{\prime} b^{\prime}} \propto \frac{H^{2}}{|f|}\left|\nabla_{H} \bar{b}\right|^{2}
$$

And horizontally downgradient flux.

$$
\overline{\overline{u^{\prime}} H^{b^{\prime}}} \propto \frac{-H^{2} \frac{\partial \bar{b}}{\partial z}}{|f|} \nabla_{H} \bar{b}
$$

## It works for Prototype Sims:

Red: No Diurnal
Blue: With Diurnal

$>2$ orders of magnitude!

Circles: Balanced Initial Cond.
Squares: Unbalanced Initial Cond.

## Better than the competition:



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## Better than the competition:



And, extends/agrees with Deep Convection Studies: Jones \& Marshall (93,97), Haine \& Marshall (98)

## What lengthscale dominates $\left\langle w^{\prime} b^{\prime}\right\rangle$ ?



## What lengthscale dominates $\left\langle w^{\prime} b^{\prime}\right\rangle$ ?



Stone fastestmode Soln OK!

$$
\mu(z)=\left[1-\left(\frac{2 z}{H}+1\right)^{2}\right]\left[1+\frac{5}{21}\left(\frac{2 z}{H}+1\right)^{2}\right]
$$

## What does it look like?

7d01h from 2d parameterization


7d01h from 3d MITgcm (smoothed)



## Vertical Structure: like

 <w'b'> from Eady solution.

Stone Solution $\mu(z)=\left[1-\left(\frac{2 z}{H}+1\right)^{2}\right]\left[1+\frac{5}{21}\left(\frac{2 z}{H}+1\right)^{2}\right]$
to $O\left(\mathrm{Ro}^{2}\right)$

## Summary so far:

- Ocean mixed layer isn't totally mixed
- Submesoscale vertical fluxes are important in setting mixed layer stratification
- Weak mixed layer stratification makes for submesoscale eddies by baroclinic instability
- Their overturning can be parameterized

Now we turn to their impact

## Where in the world are the fluxes?

(Equiv. Vert. Heat Flux from Satellite Altimetry)
Where convection makes ML deep.


## Where in the world are the fluxes?

Where convection makes ML deep, which is where the ocean talks to the atmosphere

Those are the biggest MLE fluxes, but elsewhere surface fluxes are weaker, too.

Overall, MLE estimates exceed:
$50 \%$ of monthly-mean surface flux climatology $25 \%$ of the time, and
$5 \%$ of monthly-mean surface flux climatology $50 \%$ of the time.

## Biological Impact?

Ocean color image showing submesoscale structure in chlorophyll concentration near Tasmania

submesoscale eddies:
> $20 \mathrm{~m} /$ day

## Underprediction of Biology/Chlorophyll near deep convection


[Chl]
$\mathrm{mg} / \mathrm{m} 3$


## Underprediction of Biology/Chlorophyll near deep convection



When Light-Limited: More Stratification -> More Biomass!


## What does the

new parameterization do in a GCM?

- It is already implemented in the Hallberg Isopycnal model.
- MITgcm, CCSM/POP are soon to come...


## Changes To Mixing Layer Depth in

 Eddy-Resolving Southern Ocean Model

## Changes To Mixing Layer Depth in Eddy-Resolving Southern Ocean Model



## Surf. Buoy. Gradients



## Known Deep Bias in Models

## MLD: MITgem data assim

## MLD from Obs.



Courtesy I. G. Fenty
Hydrography of the Labrador Sea during Active Convection

## Deep Bias Partly Convection, but also total absence of restratification,

(GM can't do it because of tapering)


Fenty/MITgcm


Pickart et al 02.

## Deep Bias Partly Convection, but also total absence of restratification,

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Pickart et al 02.

Equator ( $f \gg 0$ ) and coarse resolution (up to 1 deg) are manageable Improves Restratification after Deep Convection

Note: param. reproduces Haine\&Marshall $(98)$ and Jones\&Marshall $(93,97)$


# Conclusion: 

- Submesoscale features, and mixed layer eddies in particular, exhibit large vertical fluxes of buoyancy that are presently ignored in climate models.
- A parameterization of mixed layer eddy fluxes as an overturning streamfunction is proposed. The magnitude comes from extraction of potential energy, and the vertical structure resembles the linear Eady solution.
- Many observations are consistent, and model biases are reduced. Biogeochemical effects are likely, as vertical fluxes and mixed layer depth are changed.
- In HIM, soon to be in MITgcm and CCSM.
- How to add effects of frontogenesis and friction??


# Conclusion: 

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- A parameterization of mixed layer eddy fluxes as an overturning streamfunction is proposed. The magnitude comes from extraction of potential energy, and the vertical structure resembles the linear Eady solution.
- Many observations are consistent, and model biases are reduced. Biogeochemical effects are likely, as vertical fluxes and mixed layer depth are changed.
- In HIM, soon to be in MITgcm and CCSM.
- How to add effects of frontogenesis and friction?? Ask Leif and Mike!


## The Parameterization:

$$
\Psi=\frac{C_{e} H^{2} \mu(z)}{|f|} \nabla \bar{b} \times \hat{\mathbf{z}}
$$

$$
\mu(z)=\left[1-\left(\frac{2 z}{H}+1\right)^{2}\right]\left[1+\frac{5}{21}\left(\frac{2 z}{H}+1\right)^{2}\right]
$$

- The horizontal fluxes are downgradient:

$$
\overline{\bar{u}_{\mathrm{H}}^{\prime} b^{\prime}}=-\frac{C_{e} H^{2} \mu(z) \frac{\partial b}{\partial z}}{|f|} \nabla_{H} \bar{b}
$$

- Vertical fluxes always upward to restratify:

$$
\overline{w^{\prime} b^{\prime}}=\frac{C_{e} H^{2} \mu(z)}{|f|}|\nabla \bar{b}|^{2}
$$

- Adjustments for coarse resolution and $f \rightarrow 0$ are known


## More to come on this...



## Coupling to turbulence?

We saw little effect of KPP/diurnal on MLEs, but...

Plan View of T

A Blumen multi-SQG model allows an approximate coupled run to equilibrate.


Surface Temp


Bottom Temp

## WB With a ML

WB Without a ML


Spectra


## Taper to SML at Equator

$$
\Psi=\frac{C_{e} H^{2} \mu(z)}{|f|} \nabla \bar{b} \times \hat{\mathbf{z}}
$$

$$
\Psi=\frac{C_{e} H^{2} \mu(z)}{\sqrt{f^{2}+\tau^{-2}}} \nabla \bar{b} \times \hat{\mathbf{z}}
$$

Converges to Young (1994) Subinertial ML Approx.
 at equator, which is gravity
waves interrupted by mixing

## Coarse Resolution

## Adjustment


$1 / 6^{\circ}$ Model
$\|\nabla \rho\|^{2}$ low-pass filtered to $3^{\circ}$
$6 x\|\nabla \rho\|^{2}$ low-pass filtered to $3^{\circ}$



$$
\begin{gathered}
\overline{w^{\prime} b^{\prime}}=\frac{C_{e} H^{2} \mu(z)}{|f|}|\nabla \bar{b}|^{2} \\
C_{e} \rightarrow C_{e} \frac{\Delta x}{L_{d}}
\end{gathered}
$$

## Better than the Competition:



But, Agrees with Deep Convection Studies: Jones \& Marshall $(93,97)$, Haine \& Marshall (98)

## 'Diffusive' Corrections



- Horiz. gives leftovers (vb only).
- Vert. reduces ML base density jump (mostly wb)


## 'Diffusive' Corrections



- Horiz. gives difference in Streamfcts (vb only). - Vert. reduces ML base density jump (wb only).


## Zooming In



## How I got into ML Stuff

Layer $9, T=750.08$ yrs. Rho $=1026.6 \mathrm{~kg} \mathrm{~m}-3$


|  | 500 |
| :---: | :---: |
|  | 240 |
|  | 220 |
|  |  |
|  | 260 |
|  | 180 |
|  | 160 |
|  |  |
|  |  |
|  | 120 |
|  | 100 |
|  | 80 |
|  |  |
|  | 60 |
|  | 40 |
|  |  |
|  |  |
|  | 0 |

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